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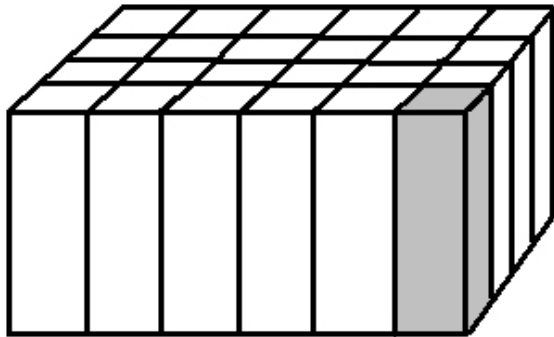
# **Towards petascale simulation of atmospheric circulations with soundproof equations**

**Institute for Meteorology and Water Management, Warsaw,  
Poland**

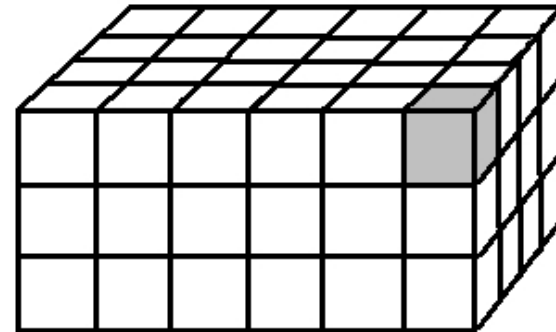
**National Center for Atmospheric Research, Boulder, CO**

# Extending MPI parallel formulation of multiscale anelastic model Eulag for geophysical flows

Traditional 2D decomposition



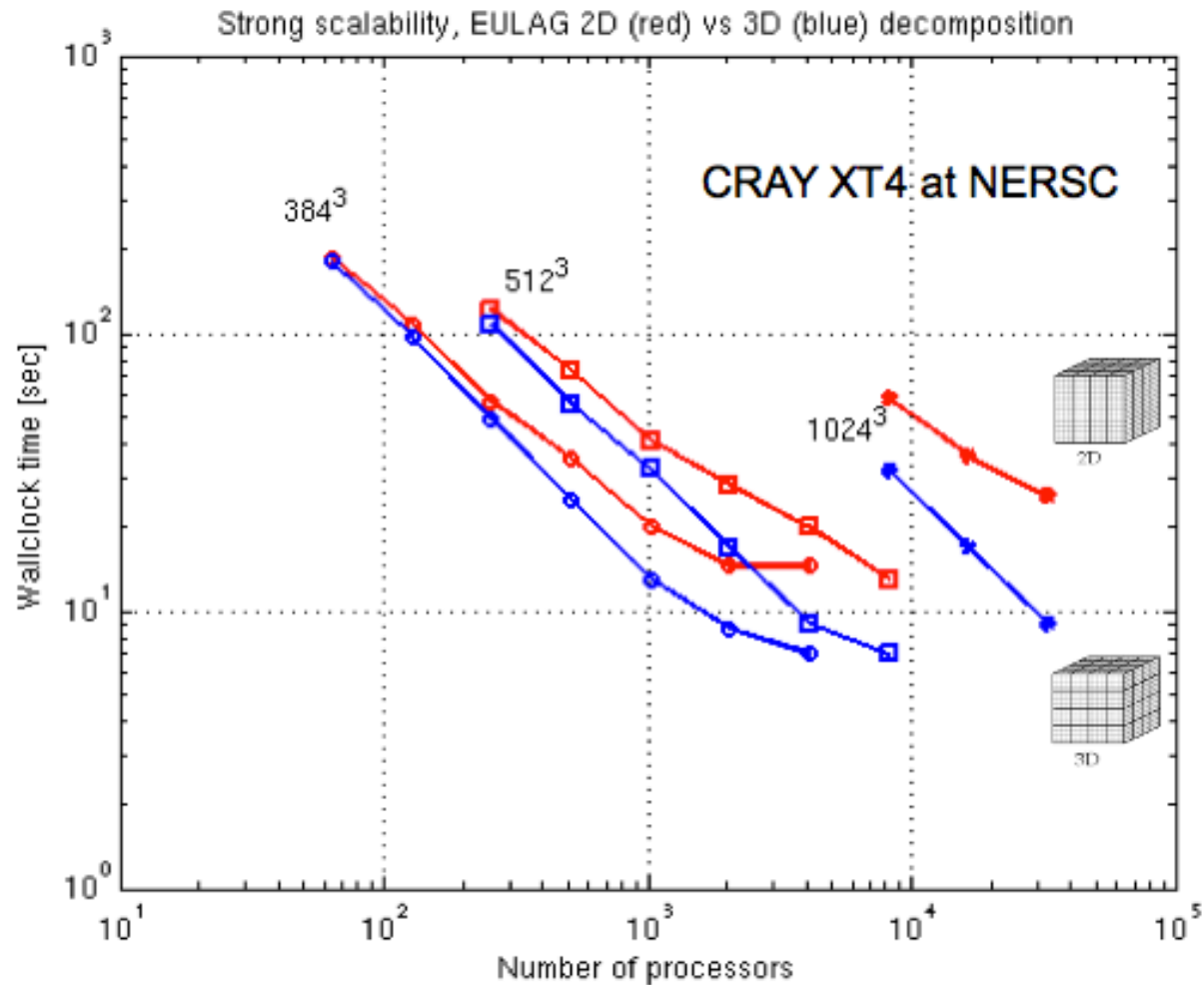
Newly developed  
3D decomposition



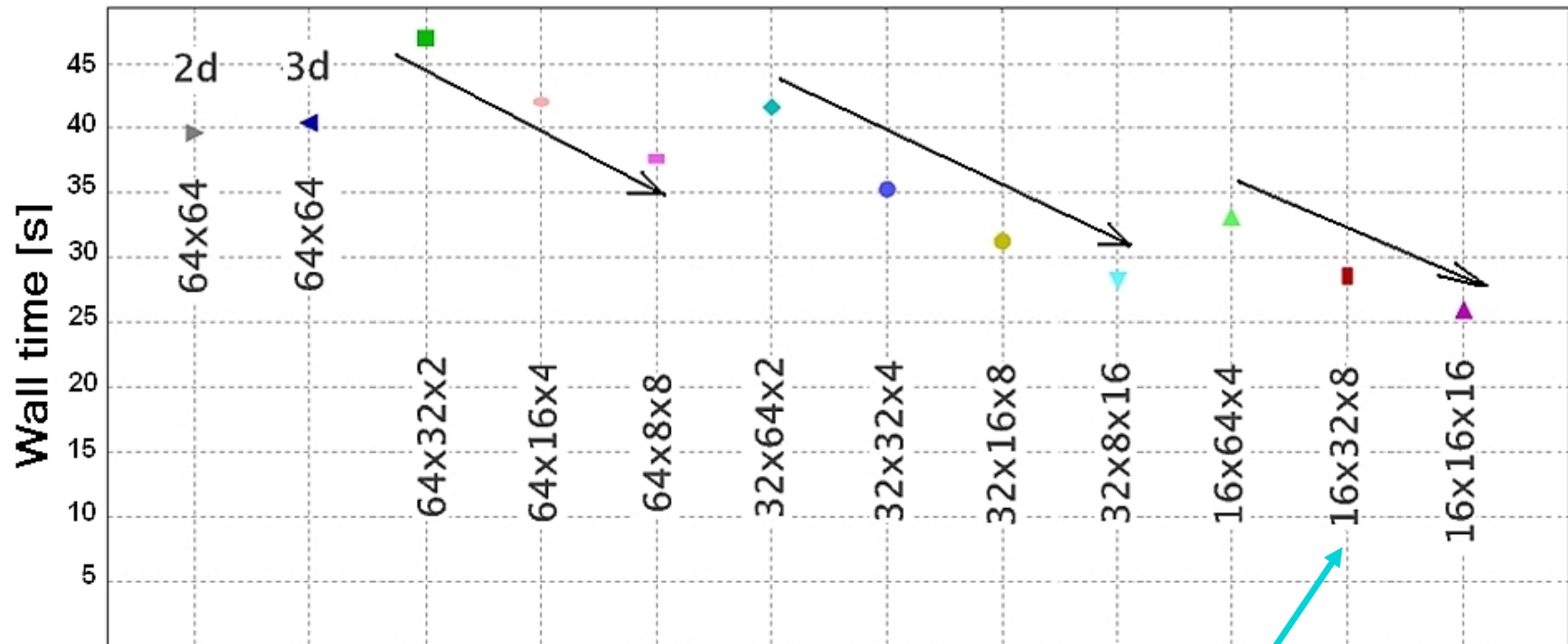
# Test experiments in the range of scales from micro to planetary

- Triply periodic decaying turbulence in the box (Taylor – Green vortex) – perfect candidate for three-dimensional parallelization
- Idealized climate simulations in a thin atmosphere shell (after Held Suarez, 1994) – traditionally decomposed in two horizontal dimensions

# Strong scaling - triply periodic decaying turbulence on Cray XT4



512<sup>3</sup> gridpoints decaying turbulence -  
dependence of performance on the processor  
configuration on Bluegene/L



Longest innermost loop

# Performance model for halo communication bandwidth usage

Examine  $R = r_{3d}/r_{2d}$ ,  $r_{3d} = [(np_{3d} + 2h) \times (mp_{3d} + 2h) \times (lp_{3d} + 2h) - V_{3d}]/V_{3d}$   
 where:  $r_{2d} = [(np_{2d} + 2h) \times (mp_{2d} + 2h) \times lp_{2d} - V_{2d}]/V_{2d}$ .

$$R\left(\frac{P}{bQ}; P, \tilde{M}\right) = \frac{\left(1 + \frac{\sqrt{P/b}}{\tilde{M}} \sqrt{\frac{bQ}{P}}\right)^2 \left(1 + \frac{a}{\tilde{M}} \frac{P}{bQ}\right) - 1}{\left(1 + \frac{\sqrt{P/b}}{\tilde{M}}\right)^2 - 1},$$

No. of  
cores in vertical

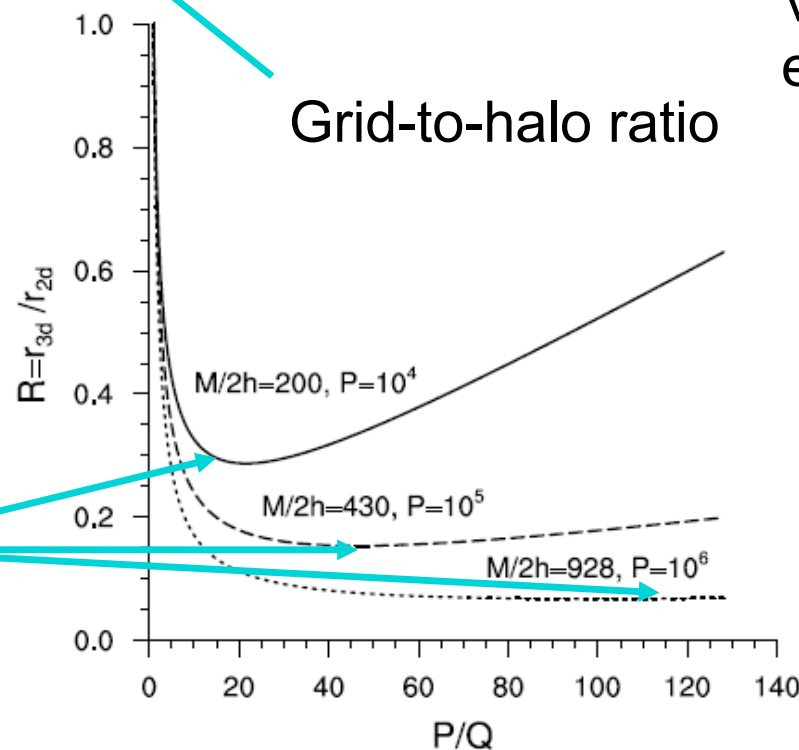
Total no. of  
cores

Optimal no. of cores in  
the vertical

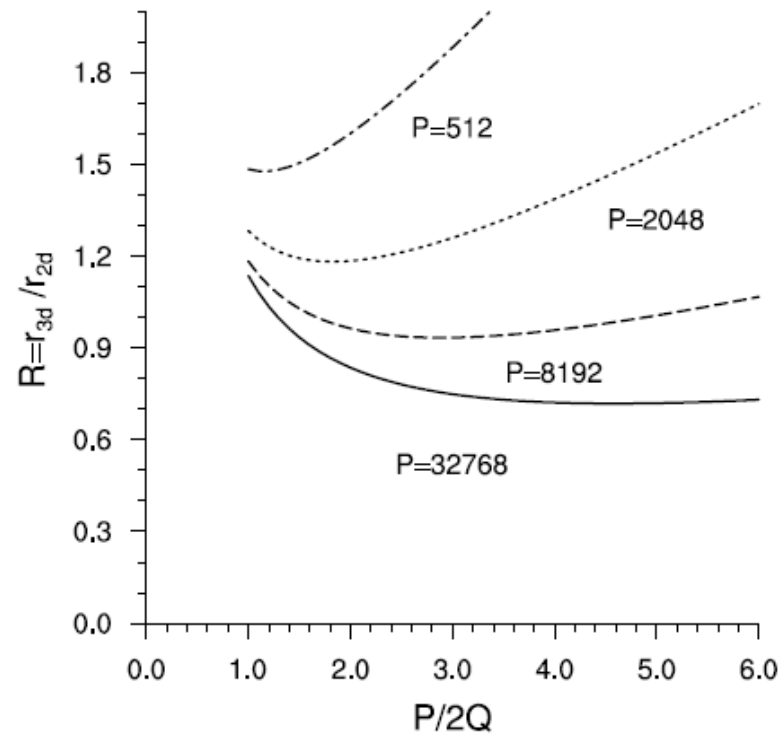
$$P/bQ = \sqrt[3]{P/ba^2}.$$

Grid-to-halo ratio

Vertical/horizontal  
extent



## Performance model for $1024 \times 512 \times 41$ idealized climate simulation



Not always a performance gain from the 3D decomposition !

... but we can always TRY to use more cores to decrease time-to-solution !

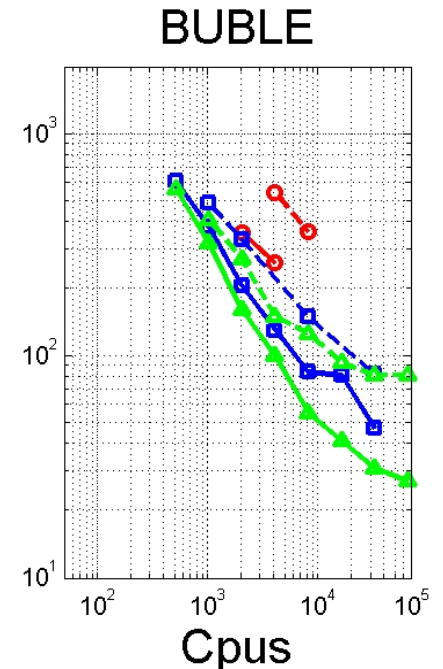
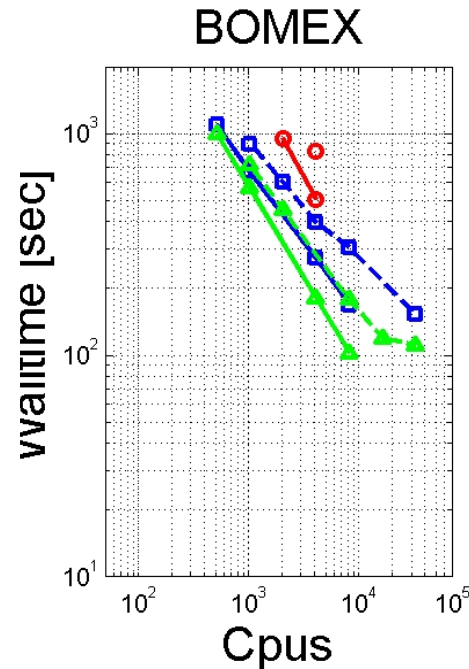
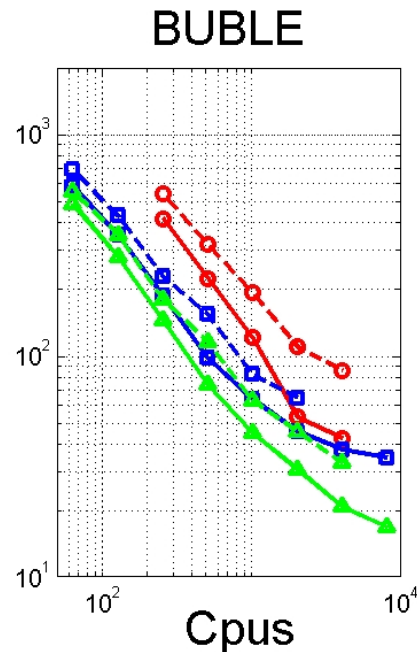
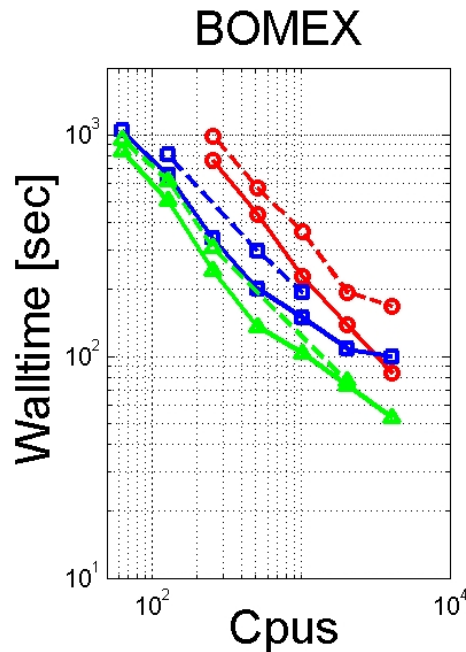
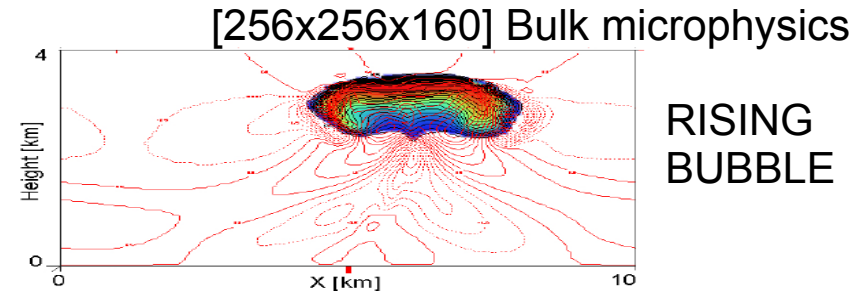
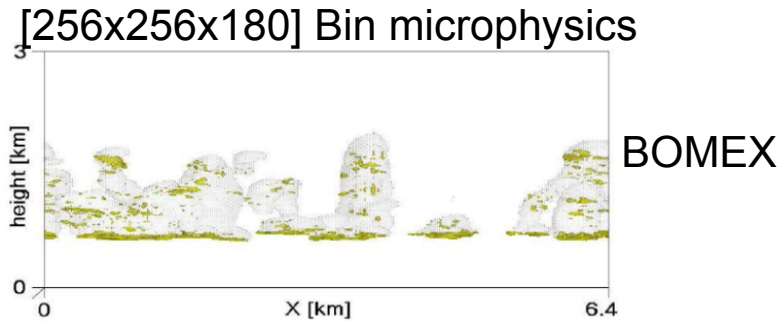
Table 1: Strong scaling of idealized climate simulation on a  $256 \times 128 \times 64$  grid, using 512 processors in the horizontal with increasing number of processors in the vertical.

Total processor number	512	1024	2048	4096
Processor configuration	$32 \times 16 \times 1$	$32 \times 16 \times 2$	$32 \times 16 \times 4$	$32 \times 16 \times 8$
Wallclock time [sec]	52	30	20	15

Everything depends on the problem size and architecture, if communication takes 80 % of the wall time (e.g. if pressure solver works really hard and there is no physics), there is no way to achieve significant speedup



# 2D/3D decomposition scalability (full model physics, Thomas preconditioner)



Strong scalability results with full model physics. The red, blue, and green lines shows results from IBM BG//L, CRAY XT4 and Cray XE6 respectively, the dashed lines represent 2D decomposition, the continuous lines 3D decomposition. Left and right panels show default and double resolution problems, respectively.

## Remarks on vertical algorithms

- Strong domain anisotropy (thin shell) results in very bad conditioning hurting the performance of iterative solvers
- Effective preconditioning is a key to the iterative solver convergence ...
- ... but it demands direct inversion of the tridiagonal matrix in the vertical direction (same for radiation)
- Thomas algorithm is a embarrassingly serial recurrence → special treatment necessary
- Possible solution is the recurrence doubling approach  
 $a(n+1) = Ba(n) + C$  is rewritten as:  
 $a(n+1) = F(B, C)a(1) + \text{parallel part}$
- + pipelining or single GATHER/SCATTER in the vertical (depending on the machine and number of cores)

## Additional benefits of 3D MPI parallelization

- Most part of the EULAG code is now symmetrical in  $x, y, z$
- A number of long lasting bugs revealed and fixed
- For large class of experiments, time-to-solution significantly decreased for fixed number of cores
- Size of the innermost loop is more flexible – beneficial for vectorization
- Many optimizations introduced in process of coding and testing of the new code

## More remarks ...

With the new, 3D parallelization we can attempt to simulate much larger problems, BUT there is a memory wall ahead.

→ Need for improving memory locality and cache use efficiency

Also, we can decompose problem to use many more cores, BUT there is a communication wall ahead

→ Need for minimizing halo updates and, especially, reduce number of global MPI operations to minimum

# Conclusions

- Three dimensional MPI parallel formulation, for symmetric (e.g. cubical turbulence) problems, can decrease time to solution for given number of cores used by factor of  $\sim 0.5$ .
- For thin-shell applications (weather and climate), it allows for decreasing time-to-solution by admitting much larger number of computing cores.