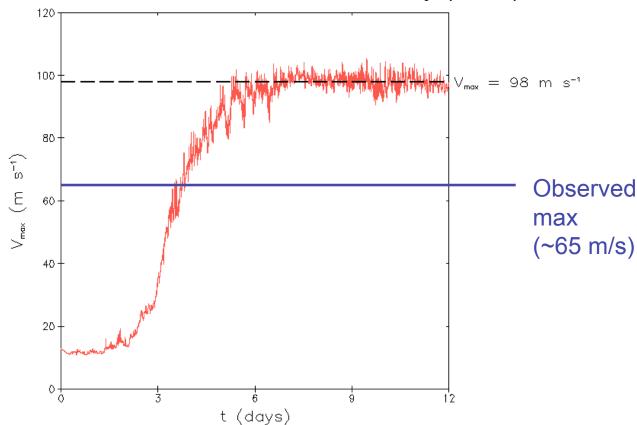
The effects of small-scale turbulence on maximum hurricane intensity

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- Axisymmetric numerical model (2d: r-z)
 - Nonhydrostatic, primitive equations, time-dependent
 - See Bryan and Rotunno (2009b, MWR) for details
 - T_s = 26 °C, same setup as Rotunno-Emanuel (1987) and Persing-Montgomery (2003)

Time series of max. azimuthal velocity (m s⁻¹):



Model components investigated:

[see Bryan and Rotunno (2009b, MWR) for details]

- Resolution
- Numerics
- Initial vortex
- Governing equations
 - unique mass/energy conservation in this model
- Microphysics
 - liquid / ice processes
 - single-moment / double-moment
 - fall velocity of condensate
- Surface exchange coefficients (C_E / C_D)
- Turbulence

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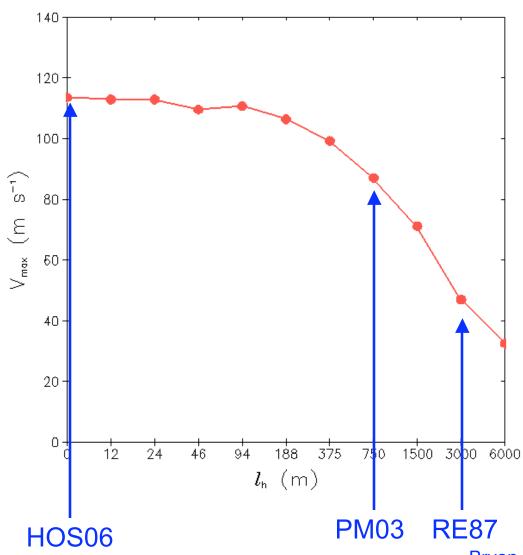
$$\nu_h = l_h^2 S_h,$$

$$\nu_v = l_v^2 \left(S_v^2 - N_m^2 \right)^{1/2}.$$

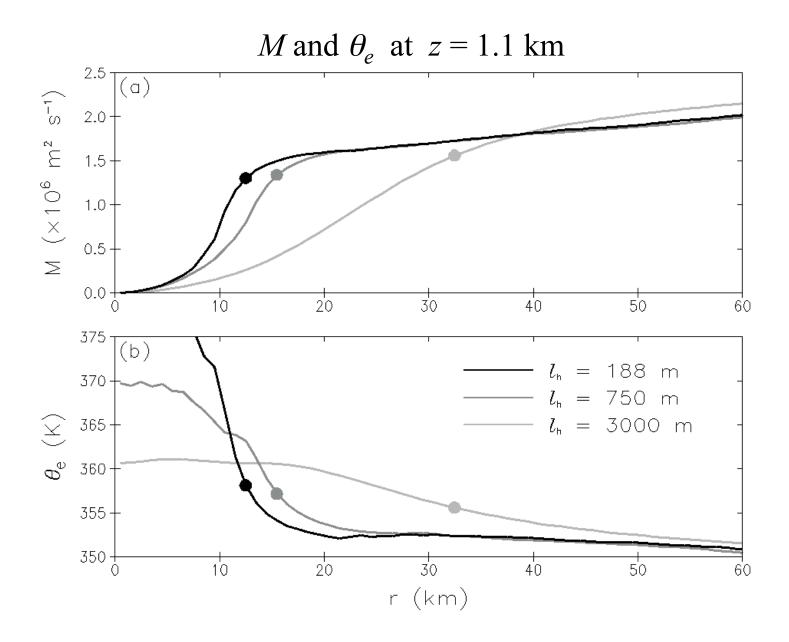
Turbulence eddy viscosities:

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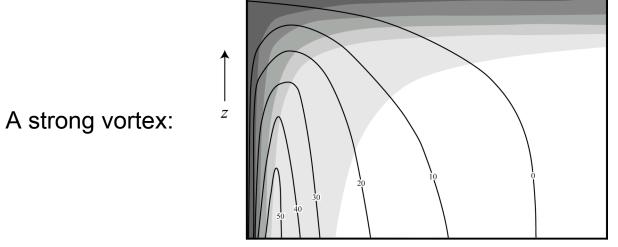


Bryan and Rotunno (2009b, MWR)



Thermal-wind balance

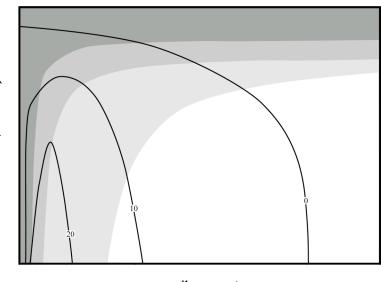
 vertical wind shear is proportional to the horizontal temperature (entropy) gradient



shading = entropy

contours = $v (m s^{-1})$

A weak vortex:



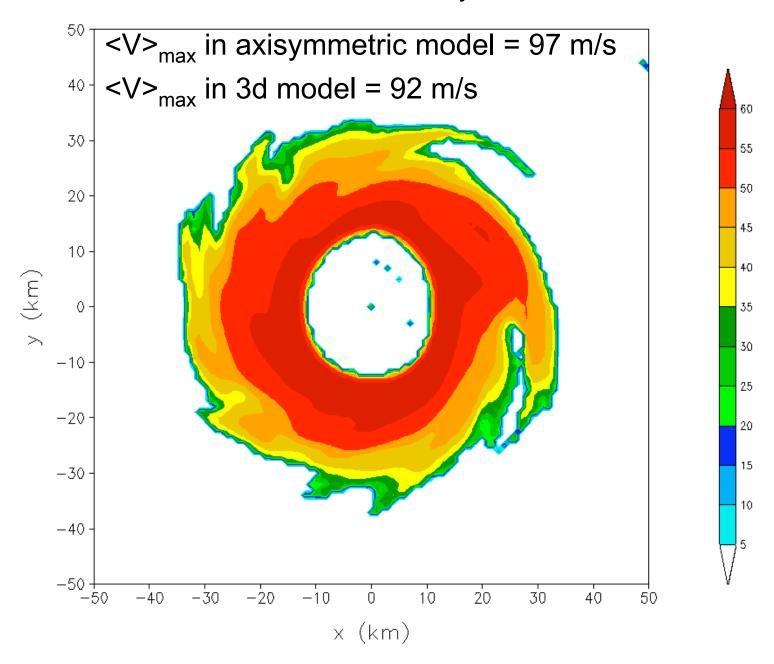
Outstanding question:

What happens in 3d numerical simulations?

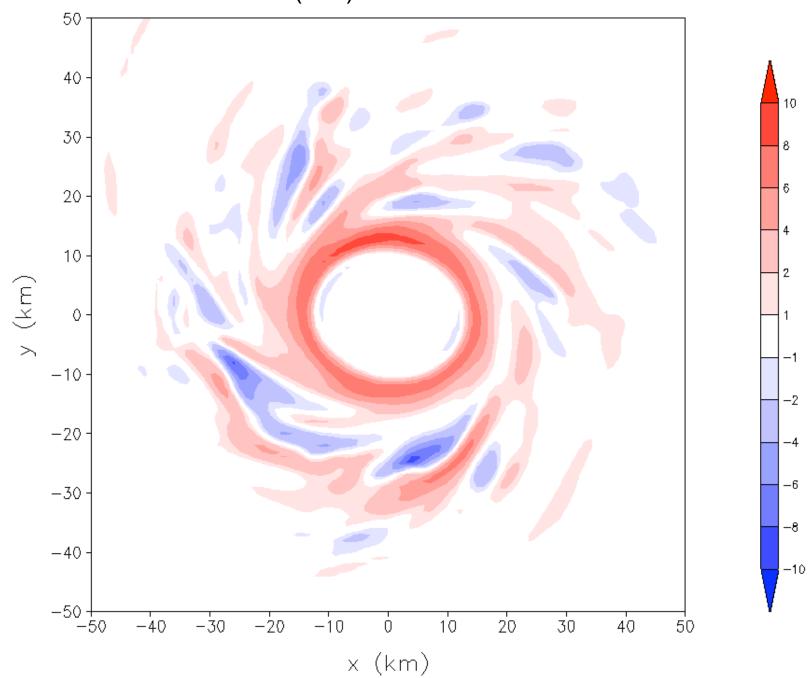
Setup:

- Same initial conditions, physics, etc
- 3d geometry (Cartesian grid)
- $-\Delta x = \Delta y = 1$ km, $\Delta z = 250$ m (same as axisymmetric simulations)

Surface reflectivity

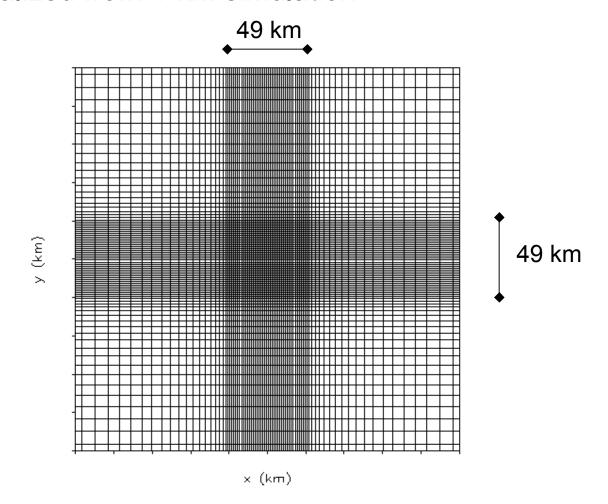




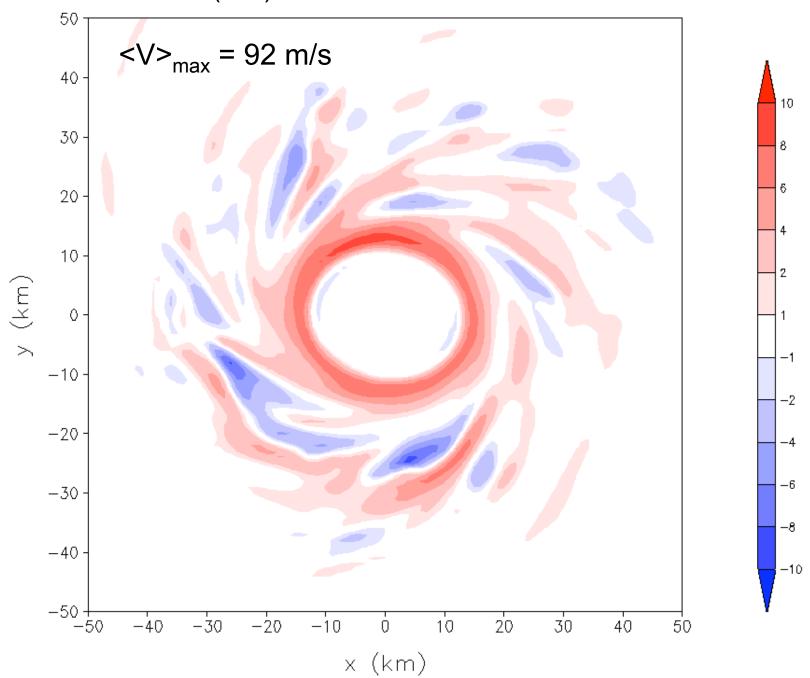


A very high-resolution simulation

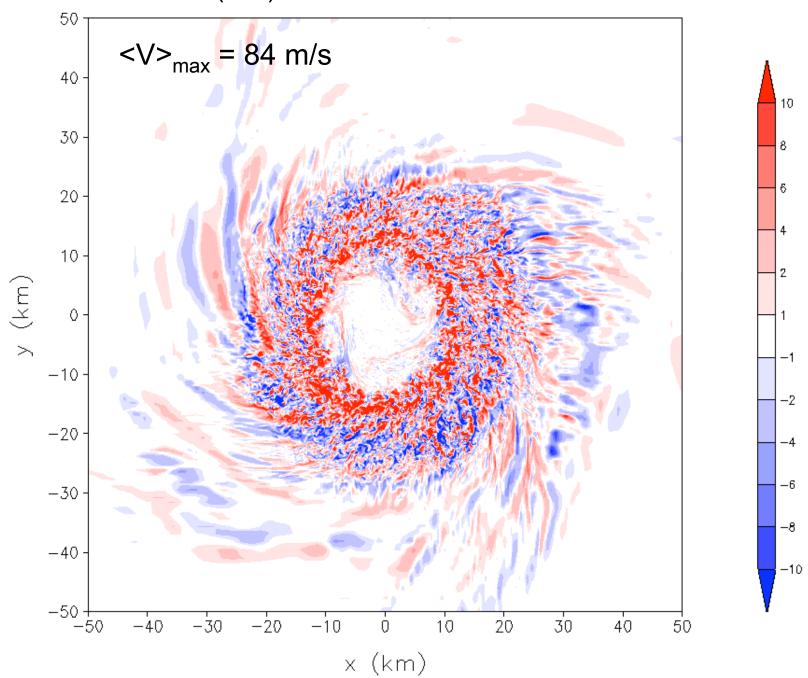
- Motivated by Rotunno et al. (2009, BAMS, in press)
- In center: $\Delta x = \Delta y = \Delta z = 62.5$ m
- (stretched structured grid)
- Initialized from 1-km simulation



w (m/s) at z = 1 km: Δ = 1000 m

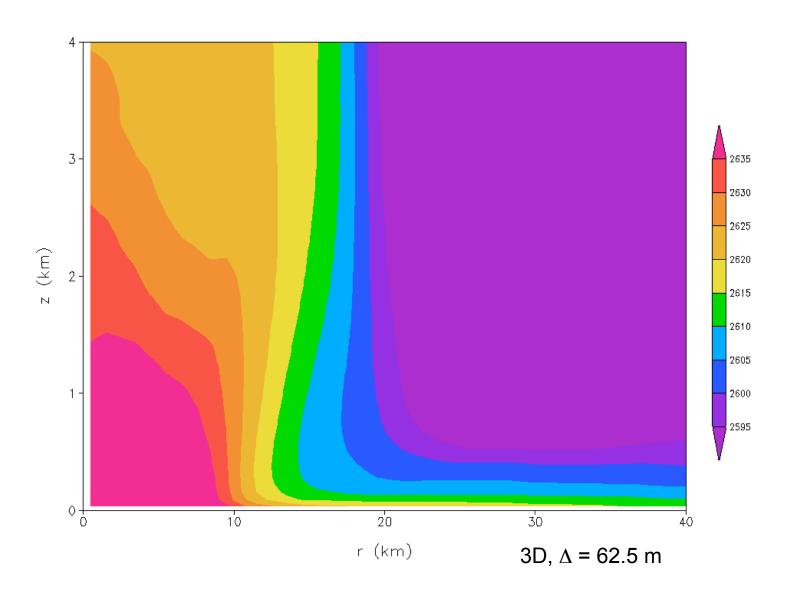


w (m/s) at z = 1 km: Δ = 62.5 m



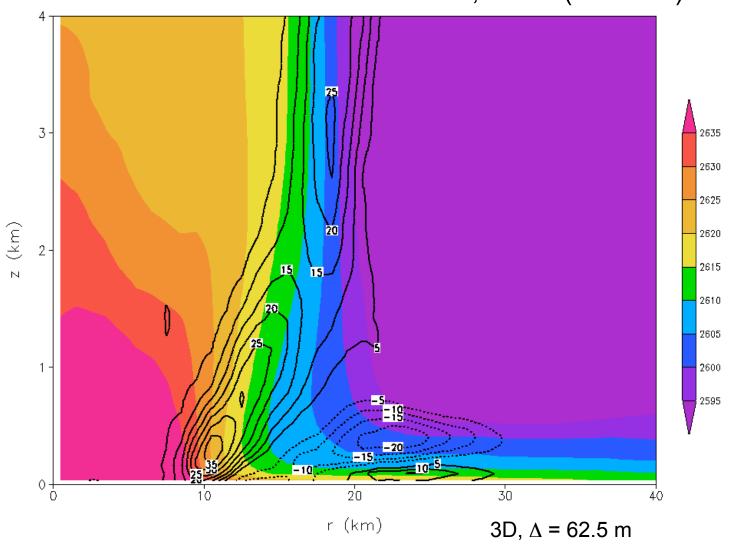
Let $\alpha(r,\phi,z) = <\alpha>(r,z) + \alpha'(r,\phi,z)$

<*s*> (shaded)



Let $\alpha(r,\phi,z) = \langle \alpha \rangle(r,z) + \alpha'(r,\phi,z)$

 $\langle s \rangle$ (shaded) and turbulent flux of s in radial direction, $\langle u's' \rangle$ (contours)



total moist entropy, <s>:

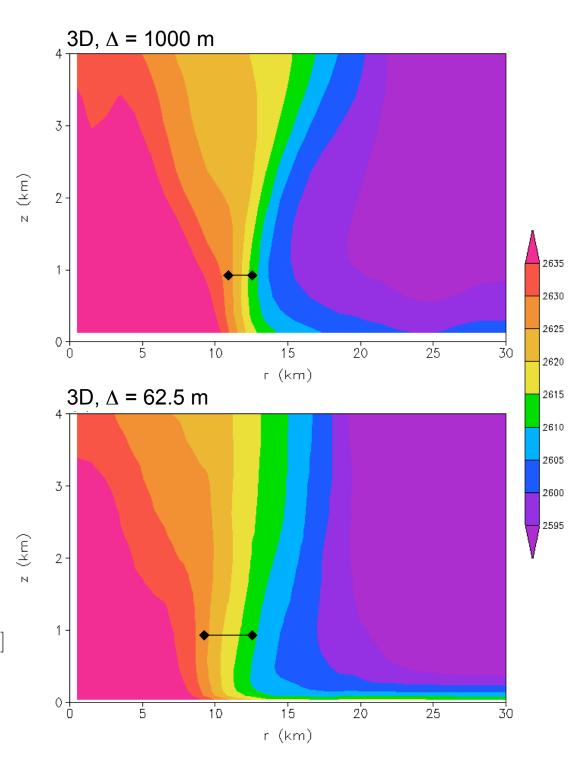
$$\frac{\partial \langle s \rangle}{\partial r} = -8.8 \times 10^{-3} \text{ m s}^{-2} \text{ K}^{-1}$$

$$\frac{\partial \langle s \rangle}{\partial r} = -4.3 \times 10^{-3} \text{ m s}^{-2} \text{ K}^{-1}$$

Hurricane Isabel (2003):

[from Montgomery et al. (2006, BAMS)]

$$\frac{\partial \langle s \rangle}{\partial r} = -1.7 \times 10^{-3} \text{ m s}^{-2} \text{ K}^{-1}$$



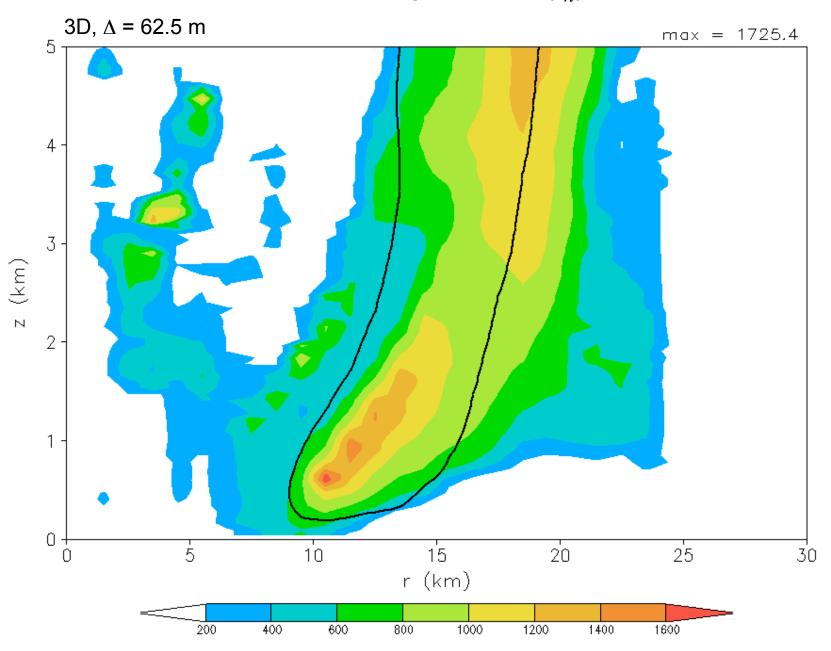
turbulence length scale:

$$\langle u's' \rangle = -K \frac{\partial \langle s \rangle}{\partial r}$$

where:

$$K = l_h^2 \left[2 \left(\frac{\partial \langle u \rangle}{\partial r} \right)^2 + 2 \left(\frac{\langle u \rangle}{r} \right)^2 + \left(\frac{\partial \langle v \rangle}{\partial r} - \frac{\langle v \rangle}{r} \right)^2 \right]^{1/2}$$

turbulence length scale (l_h) :



Summary

- Turbulence in the eyewall of hurricanes <u>reduces</u> hurricane intensity
- Very high resolution (∆ < 100 m) in three dimensions is required to simulate turbulent processes (see also Rotunno et al. 2009, BAMS, in press)

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... otherwise, turbulent processes must be parameterized (even with \Delta \approx 1 km)
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... $l_h \approx 1000 \text{ m}$