

# **Test Cases for Atmospheric Model Dynamical Cores**

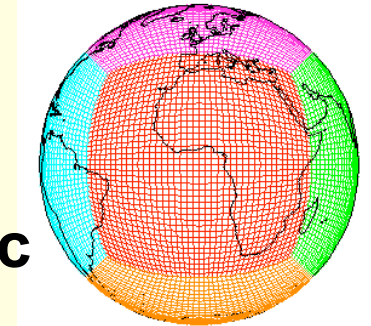
Christiane Jablonowski  
(email: [cjablono@umich.edu](mailto:cjablono@umich.edu))  
University of Michigan

NCAR Global Atmospheric Core Workshop  
Sep/24/2008

# Motivation

- Test cases for 3D dynamical cores on the sphere
  - are hard to find in the literature
  - are often not fully documented
  - have (often) not been systematically applied by a large number of modeling groups
  - lack standardized & easy-to-use analysis techniques
- Idea: Establish a collection of test cases that finds broad acceptance in the community
- Test suite that clearly describes the initial setups and suggests evaluation methods like the
  - Test suite for the SW equations (Williamson et al. 1992)
  - Proposed test suite for 2D non-hydrostatic dynamical cores (Bill Skamarock, NCAR, see Bill's web page:  
[http://www.mmm.ucar.edu/projects/srnwp\\_tests/#proposal](http://www.mmm.ucar.edu/projects/srnwp_tests/#proposal))

# Goals of the Test Suite



Test cases should

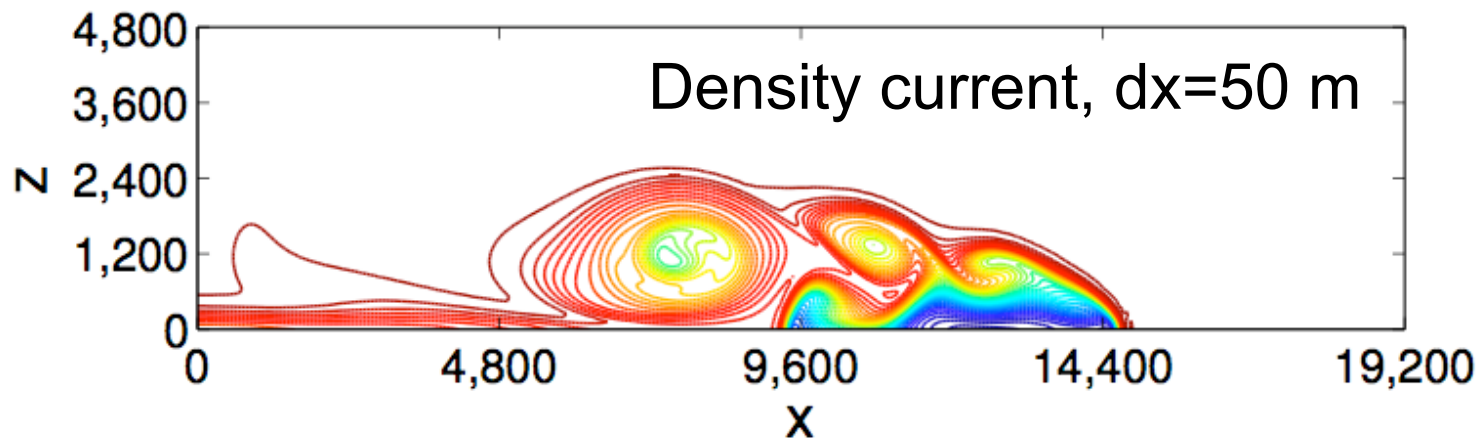
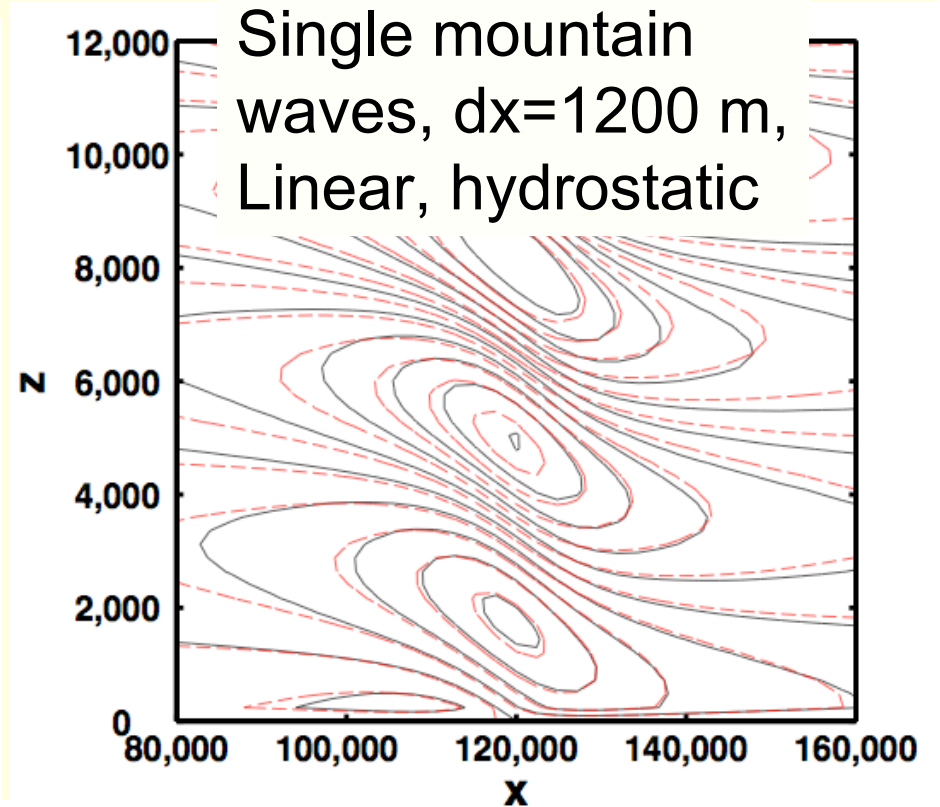
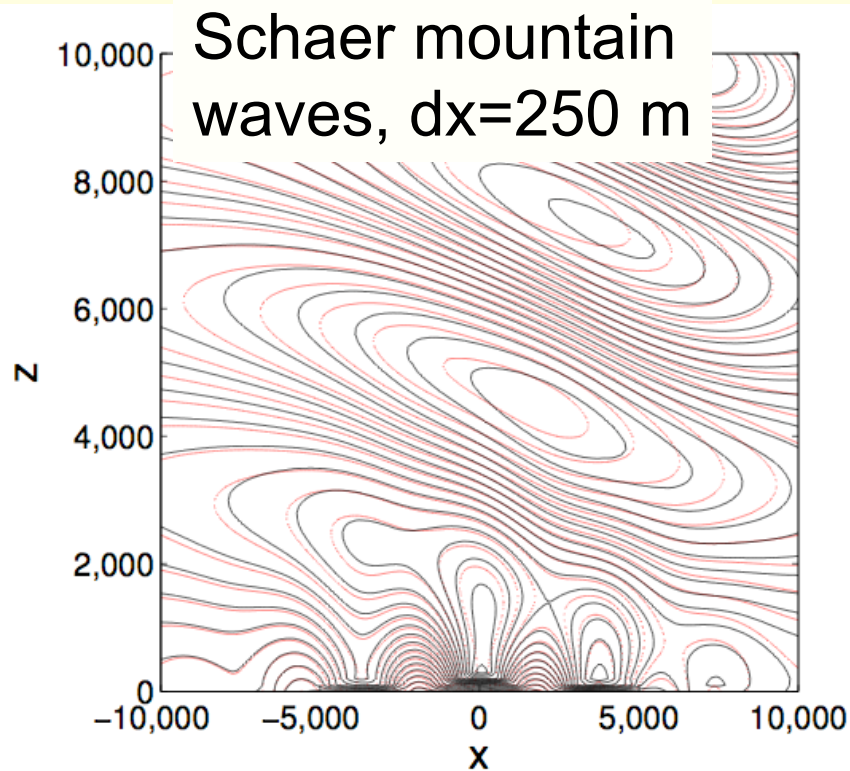
- be designed for **hydrostatic** and **non-hydrostatic** dynamical cores on the sphere, for both **shallow** and **deep atmosphere** models
- be easy to apply: analytic initial data (if possible) suitable for **all grids**, formulated for **different vertical coordinates**
- be easy to evaluate: standard diagnostics
- be relevant to atmospheric phenomena
- reveal important characteristics of the numerical scheme
- have an analytic solution or converged reference solutions

# Review of non-hydrostatic test cases

Most often: formulated for **2D (x-z) Cartesian** geometry without the Earth's rotation:

- **Thermally induced circulation:**
  - Density current (Straka et al. (1993))
  - Warm bubble (Robert, JAS (1993), Bryan and Fritsch (2002), ...): triggered by convective instability
  - Cold bubble
- **Mountain-induced gravity waves**
  - Hydrostatic / nonhydrostatic determined by ratio  $(N d)/u_0$
  - Linear / nonlinear determined by ratio  $(N h)/u_0$
  - Either single mountain (Dudhia, MWR (1993))  
or more complex topography (Schaer et al, MWR (2002))
- **Inertia-gravity waves in periodic channel** (Skamarock and Klemp, MWR, (1994)), includes Coriolis forces

# Review of non-hydrostatic test cases



from Giraldo  
and Restelli,  
JCP in press

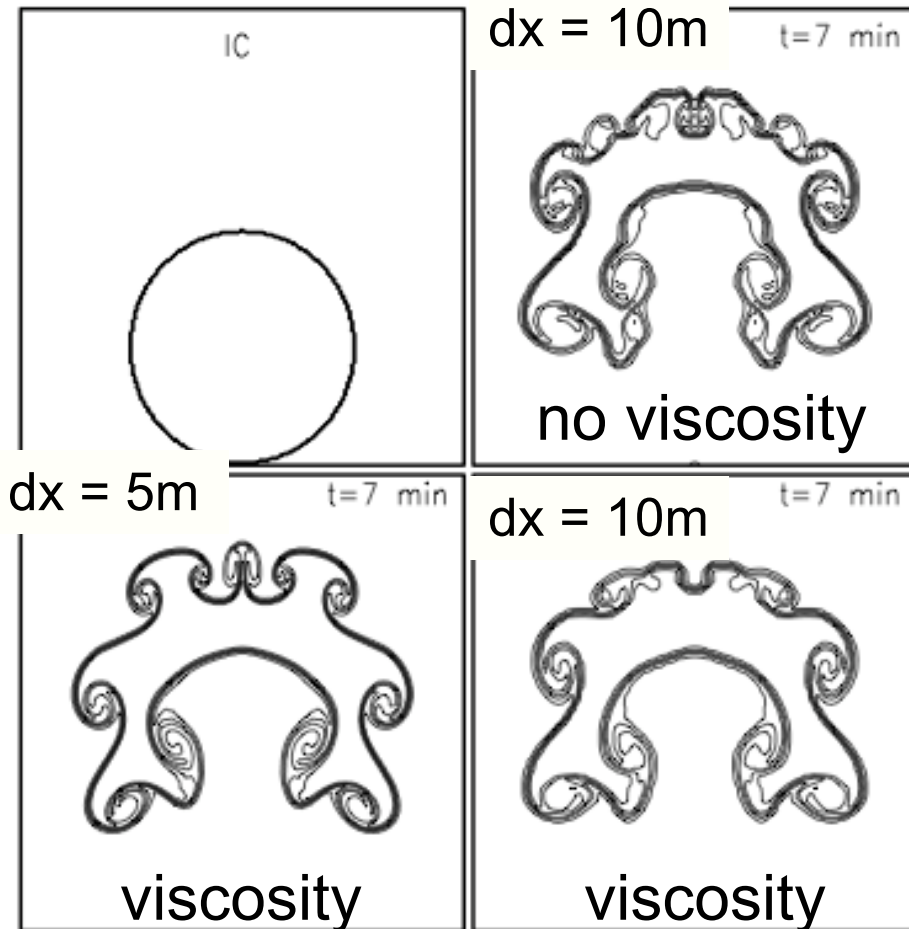
# Review of non-hydrostatic test cases

## Observations:

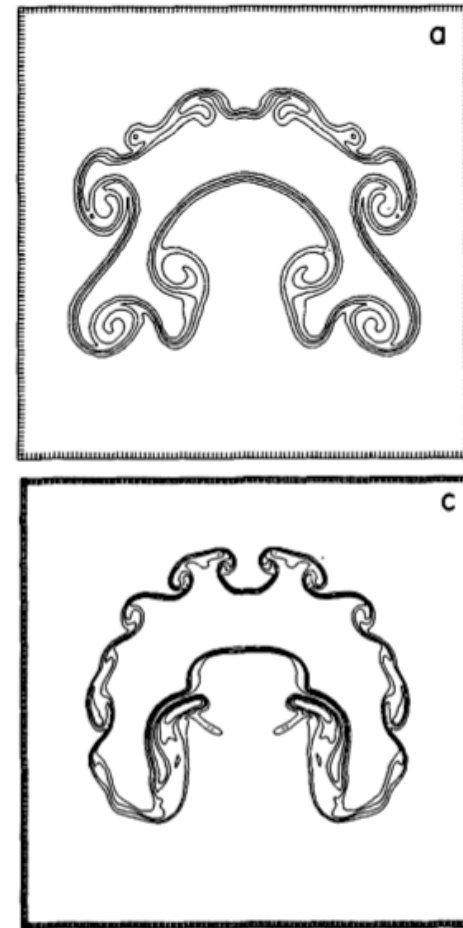
- Tests need very **high resolutions** in the horizontal and vertical directions (sometimes on the order of 10-100 m)
- Tests run for very **short** time periods, e.g. 10 minutes
- Tests run in **small** domains (a few km)
- Some tests have linear analytic solutions (e.g. some mountain wave test cases)
- Modelers often **vary** the initial conditions and sizes of the domains: very difficult to compare model results unless they are compared against analytic solutions
- High-resolution reference solutions depend strongly on the **diffusion characteristics** (either implicit or explicit)
- **Eyeball-norm** comparisons: Assessments lack additional diagnostics

# Example: non-hydrostatic test cases

**Warm bubble experiment:** Fine scales differ, rely on viscosity



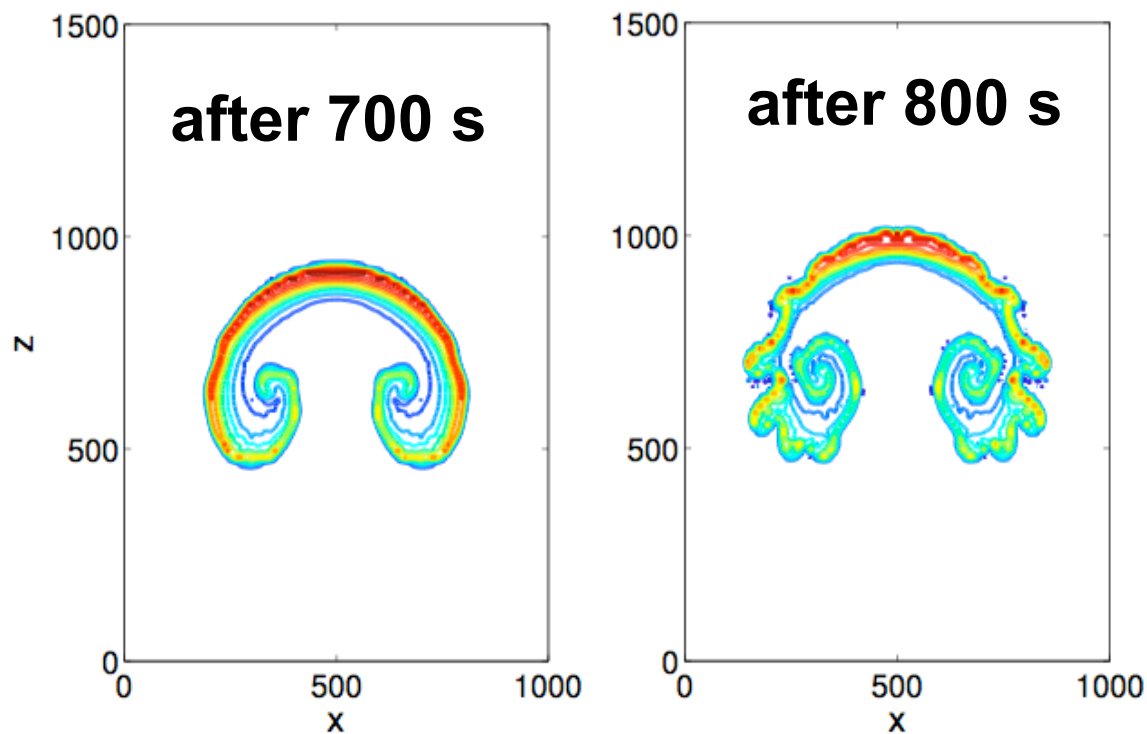
**Lin, QJ (in review)**



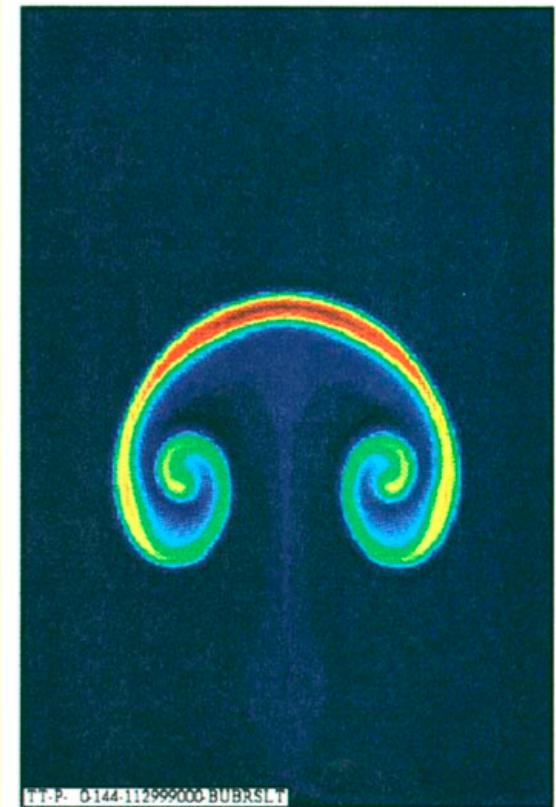
**Robert (1993), after 7 min.**

# Example: non-hydrostatic test cases

**Warm bubble experiment (Gaussian):** Slightly different setups or/and time steps are difficult to compare



**Giraldo and Restelli**  
JCP, in press



**Robert (1993),**  
after 720 s

# Review of idealized test cases on the sphere

So far in the literature:

- **Deterministic**

- Polvani et al., MWR (2004)
- Collection by Tomita and Satoh, Fluid Dyn. Res. (2004)
- Jablonowski and Williamson, QJ (2006)
- Test suite discussed today:

[http://www-personal.umich.edu/~cjablono/dycore\\_test\\_suite.html](http://www-personal.umich.edu/~cjablono/dycore_test_suite.html)

74-page 'Test Suite' document, to be submitted as journal paper and NCAR Tech Report

- **Climate-runs with idealized forcings**

- Held-Suarez (1994)
- Boer-Denis (1998)
- Moist Held-Suarez (Galewsky et al. JAS (2005))

- **Aqua-planet simulations** (ocean-covered Earth with prescribed SST, full physics), Neale and Hoskins (2001)

# Review of idealized test cases on the sphere

Some more comments on the test case collection in Tomita and Satoh, Fluid Dyn. Res. (2004)

- Used for **nonhydrostatic deep atmosphere** dycore
- But test cases are used **at hydrostatic scales**
- Test are formulated for **shallow** atmospheres

## **Two classes:**

- Irrotational:
  - Sound waves
  - Gravity waves
  - Mountain waves
- Rotational:
  - Kelvin and Equatorial Rossby waves triggered by tropical heating
  - Rossby waves in midlatitudes (mountain induced)

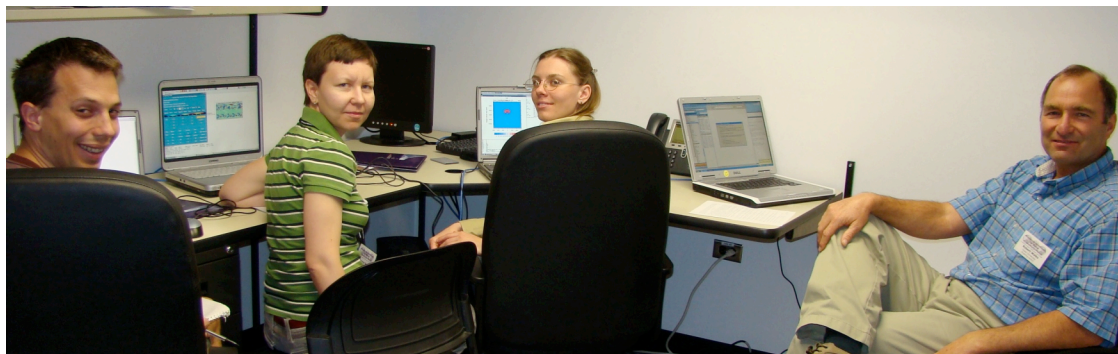
# Test cases on the sphere: NCAR 2008 ASP Colloquium

Peter Lauritzen, Christiane Jablonowski, Ram Nair, Mark Taylor

A community effort towards **standard evaluations** of dynamical cores with over 10 modeling groups, 36 students and 17 lecturers

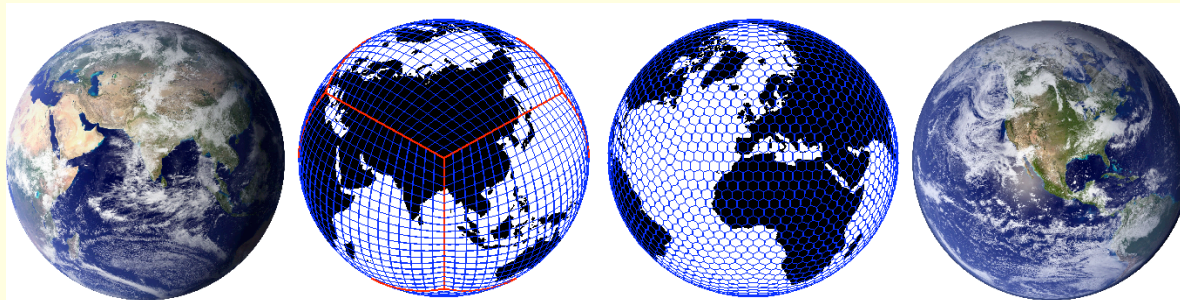


# NCAR 2008 ASP Colloquium

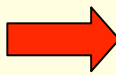


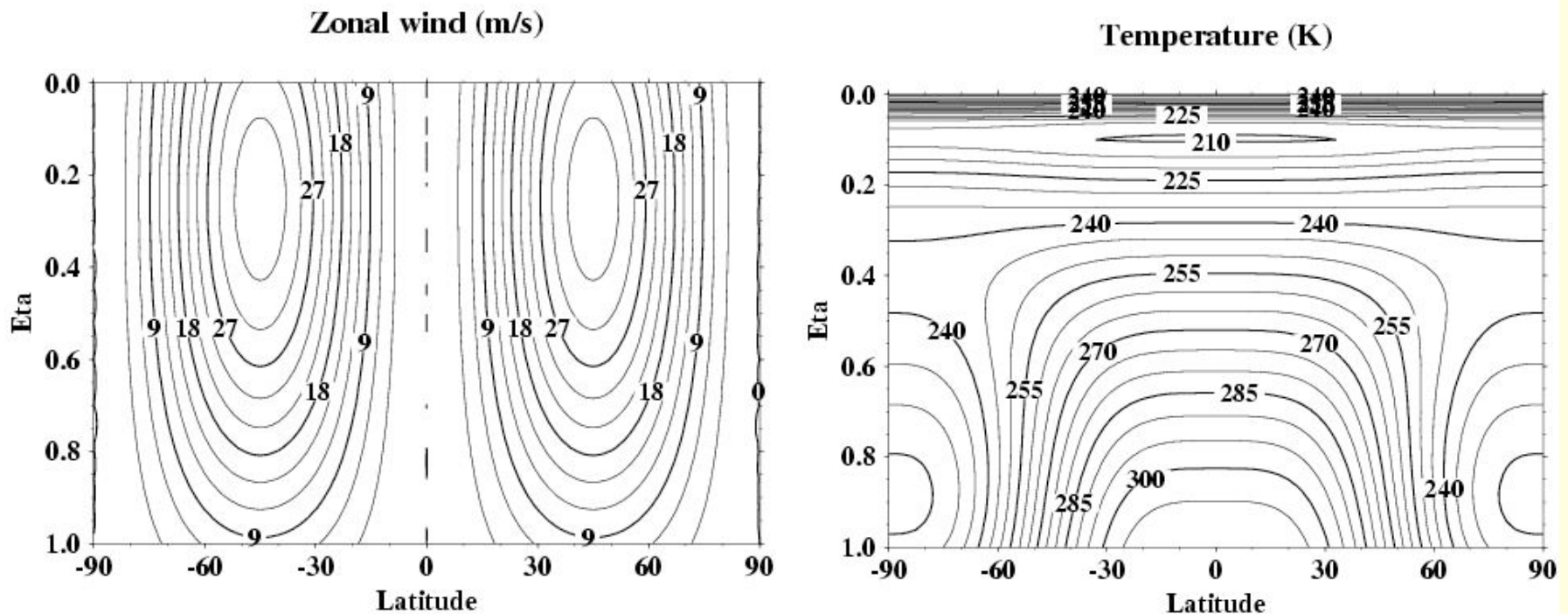
# Proposed Dynamical Core Test Suite used during the 2008 NCAR ASP Colloquium

- All tests are formulated on the sphere
  - Some have multiple test variants, e.g. rotation angle  $\alpha$
1. Steady-state test case
  2. Evolution of a baroclinic wave
  3. 3D advection experiments
  4. 3D Rossby-Haurwitz wave with wavenumber 4
  5. Mountain-induced Rossby wave train
  6. Pure gravity waves and inertial gravity waves



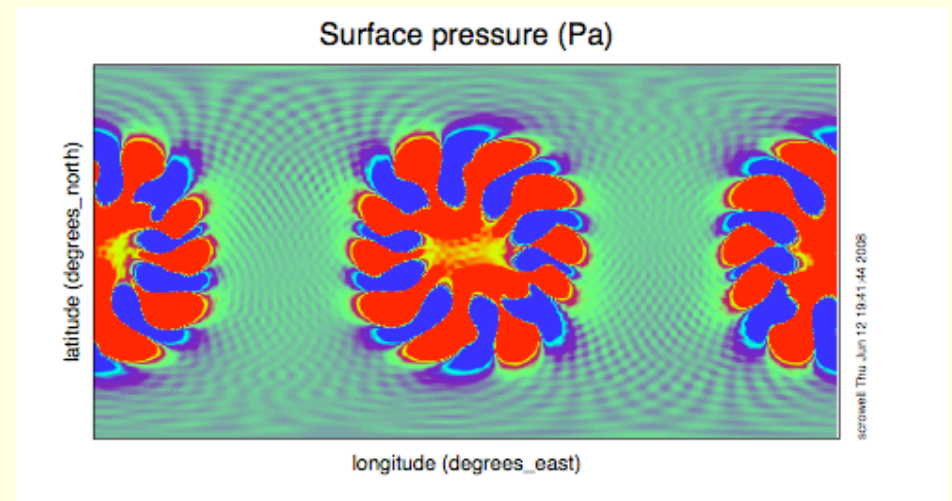
# Test 1: Steady-State Initial Conditions

- Analytical solution to the Primitive Equations with pressure-based vertical coordinates (like  $\sigma$  or  $\eta$ )
- Prescribe  $v = 0$  m/s,  $p_s = 1000$  hPa
- Prescribe  $u$   derive  $\Phi_s$  and  $T$



# Test 1) Steady-State

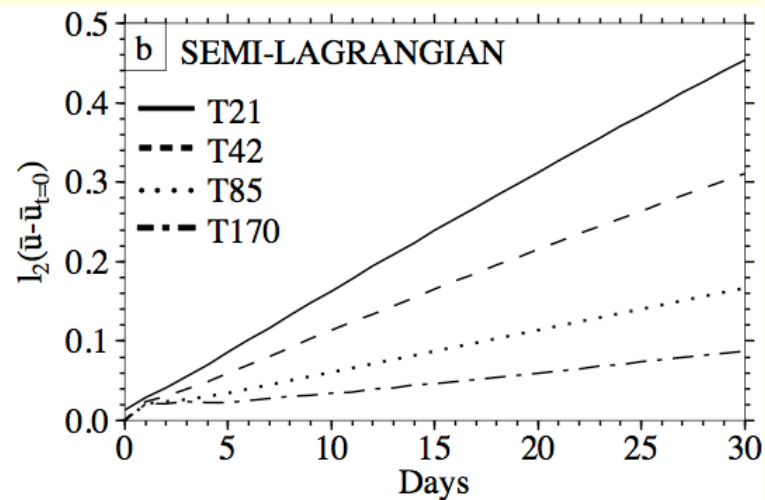
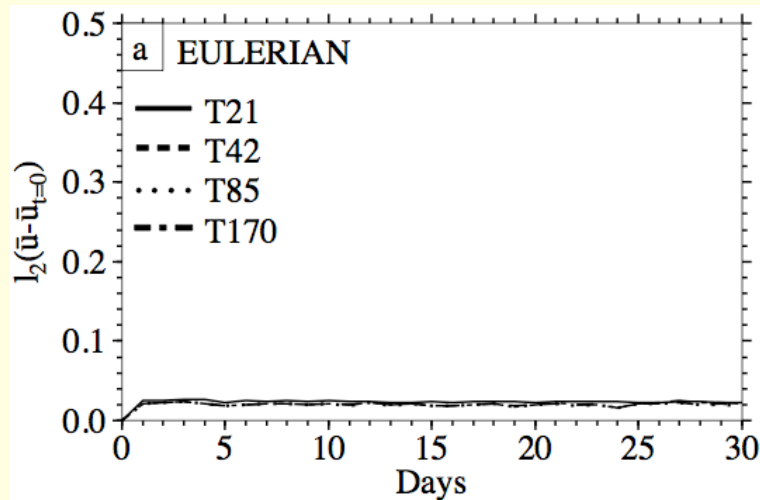
- Initialize the dynamical core with the analytic initial conditions (balanced & steady state)
- Let the model run over 30 days (if possible without explicit diffusion)
- Does the model maintain the steady state?
- The answer is '**sometimes**':
- Yes if regular lat-lon grid is used and the flow is a pure W-E flow (no rotation)
- No for cubed-spheres, triangular grids (grid imprinting), or  $\alpha > 0$
- Steady-state in irregular grids improves with increasing resolution



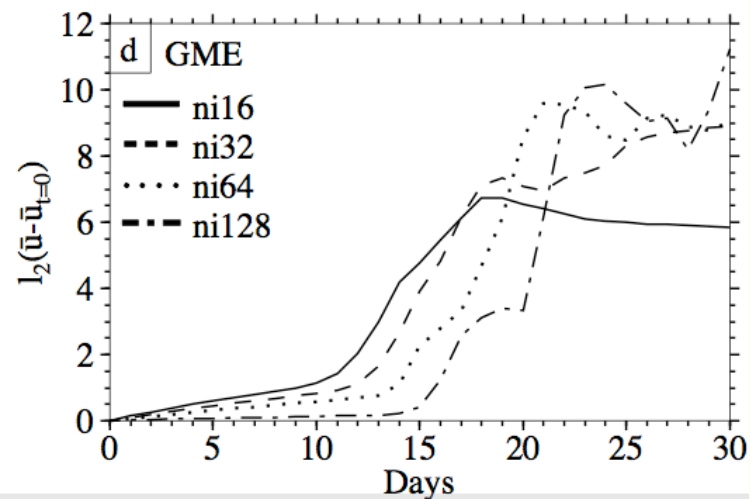
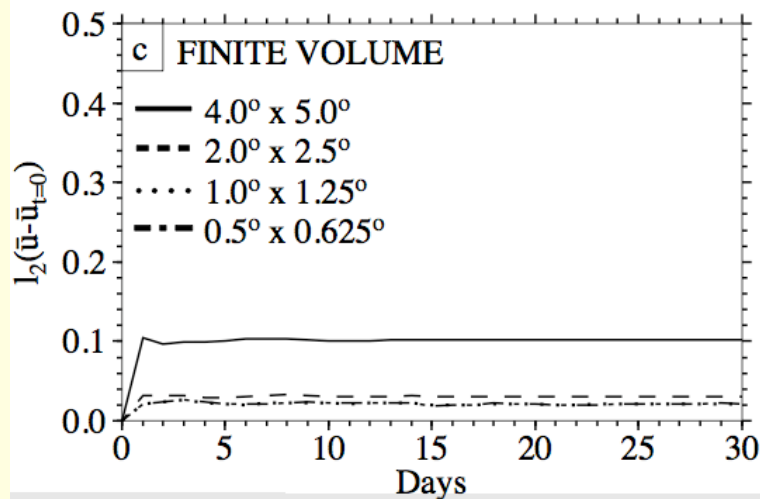
CAM-EUL, day 23 with  $\alpha=90^\circ$

# Test 1: Error analysis

- Initial state is analytic solution
- Maintenance of the zonal-mean initial u wind (I2 error)



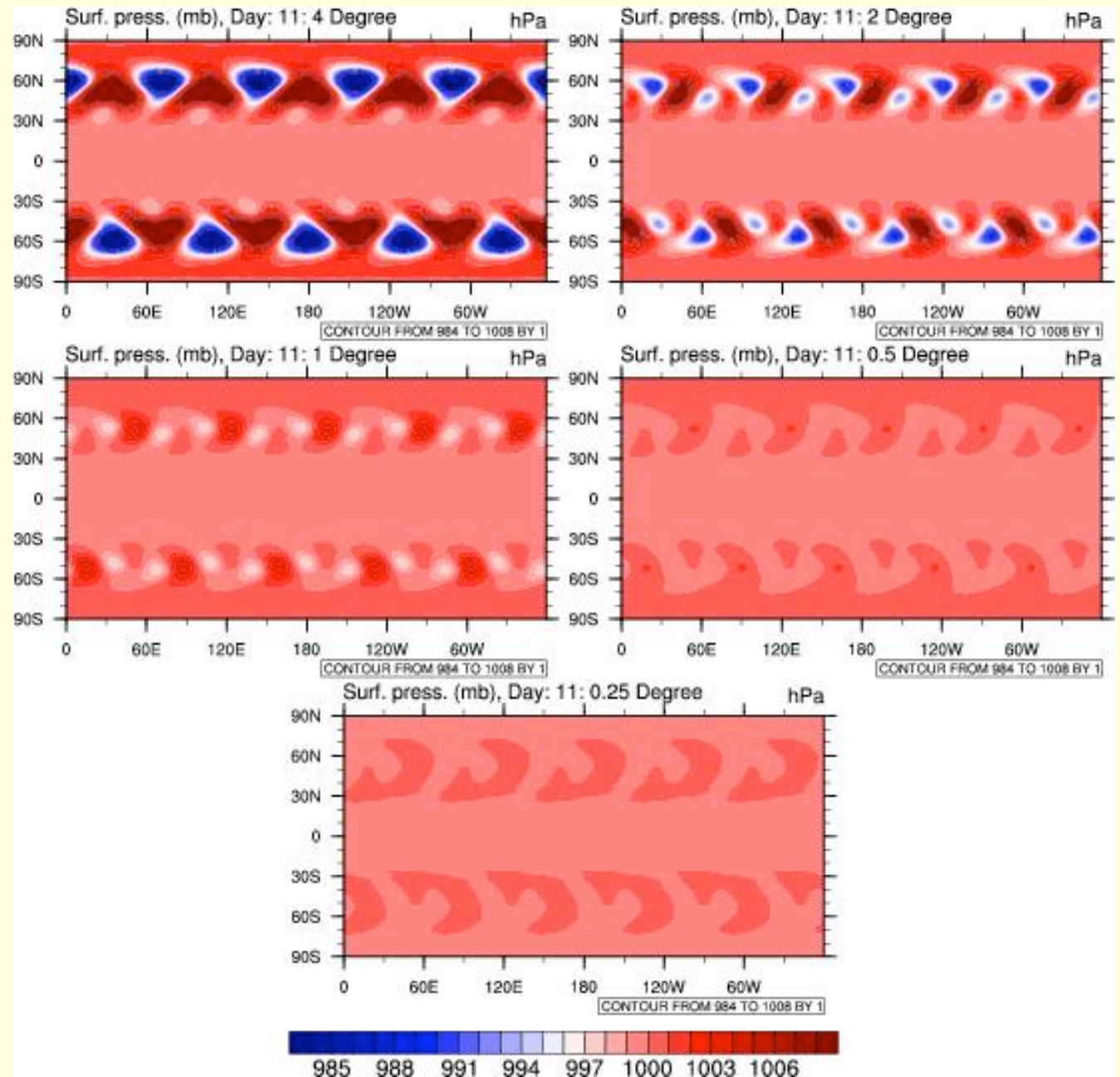
← Decentering parameter effect



← Wave number 5 effect

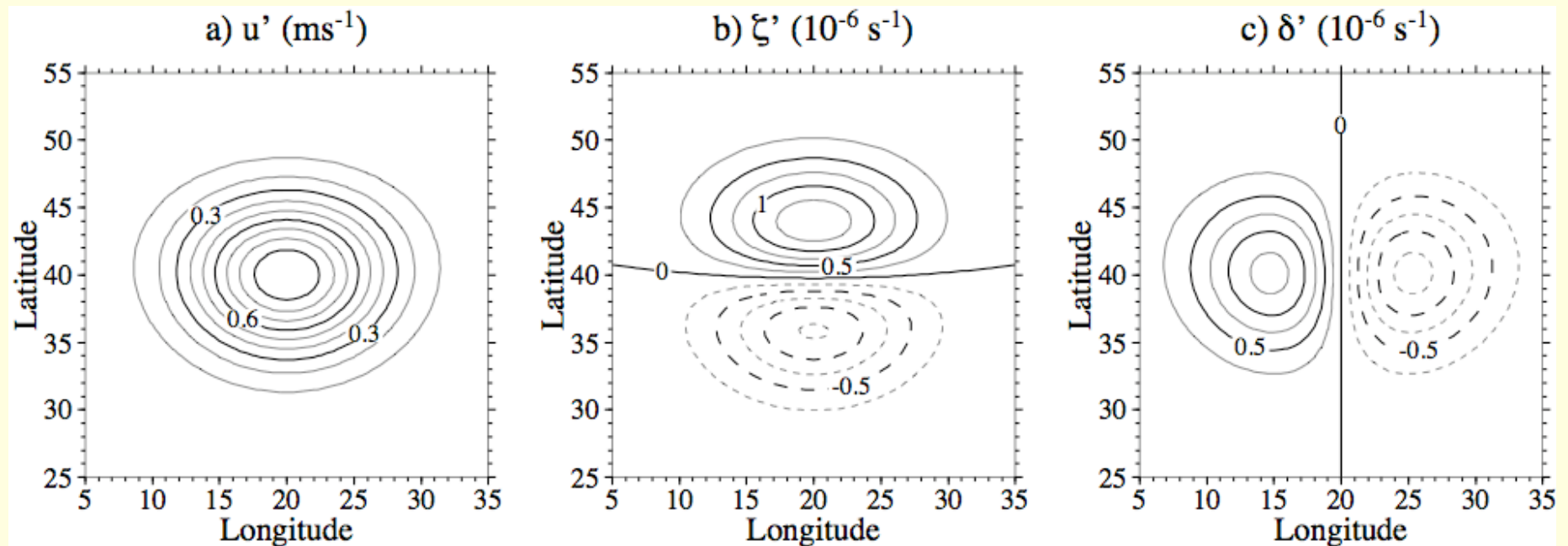
# Test 1: Grid imprinting

- GME:  $p_s$  field, day 11
- Decreases with increasing resolution
- Emphasized by idealized test setup
- Important for real runs?

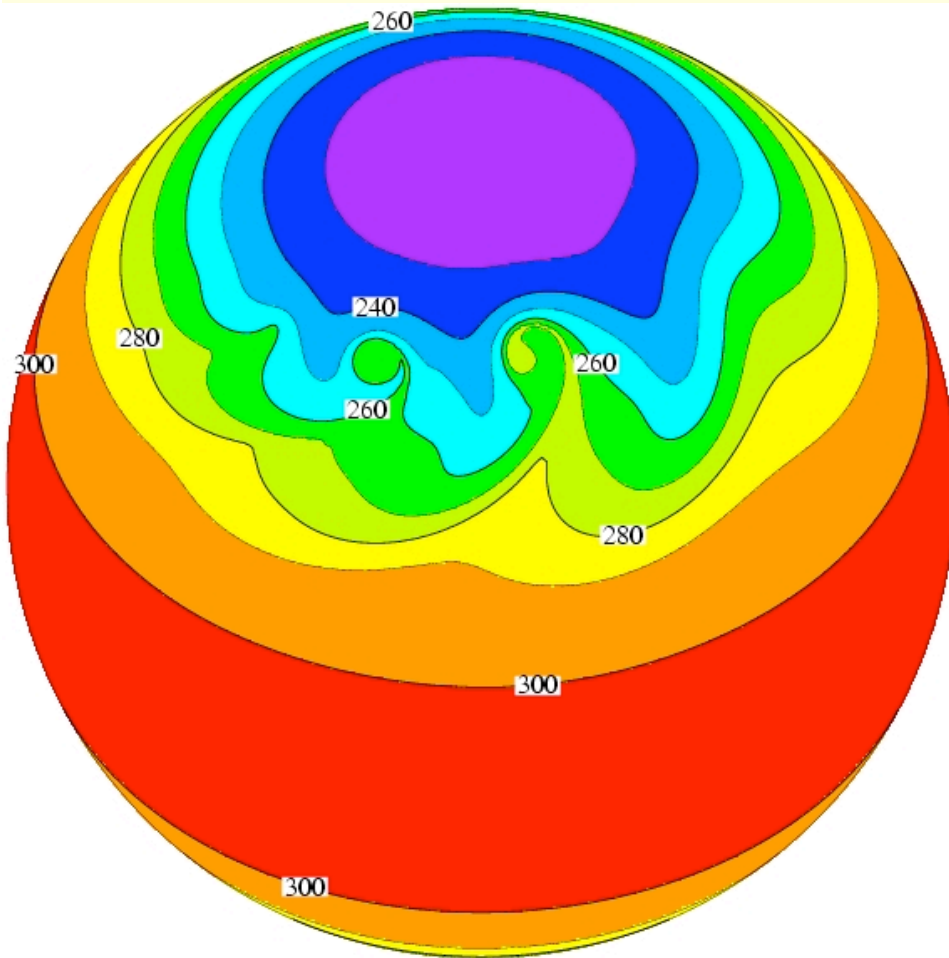


## Test 2) Select Gaussian Hill Perturbation

- Start with initial conditions from test 1
- Overlay a Gaussian perturbation (at each level):  
triggers the evolution of a baroclinic wave over 10 days
- Suggested: perturbation of the zonal wind field 'u' or the vorticity and divergence (for models in  $\zeta$ - $\delta$  form)



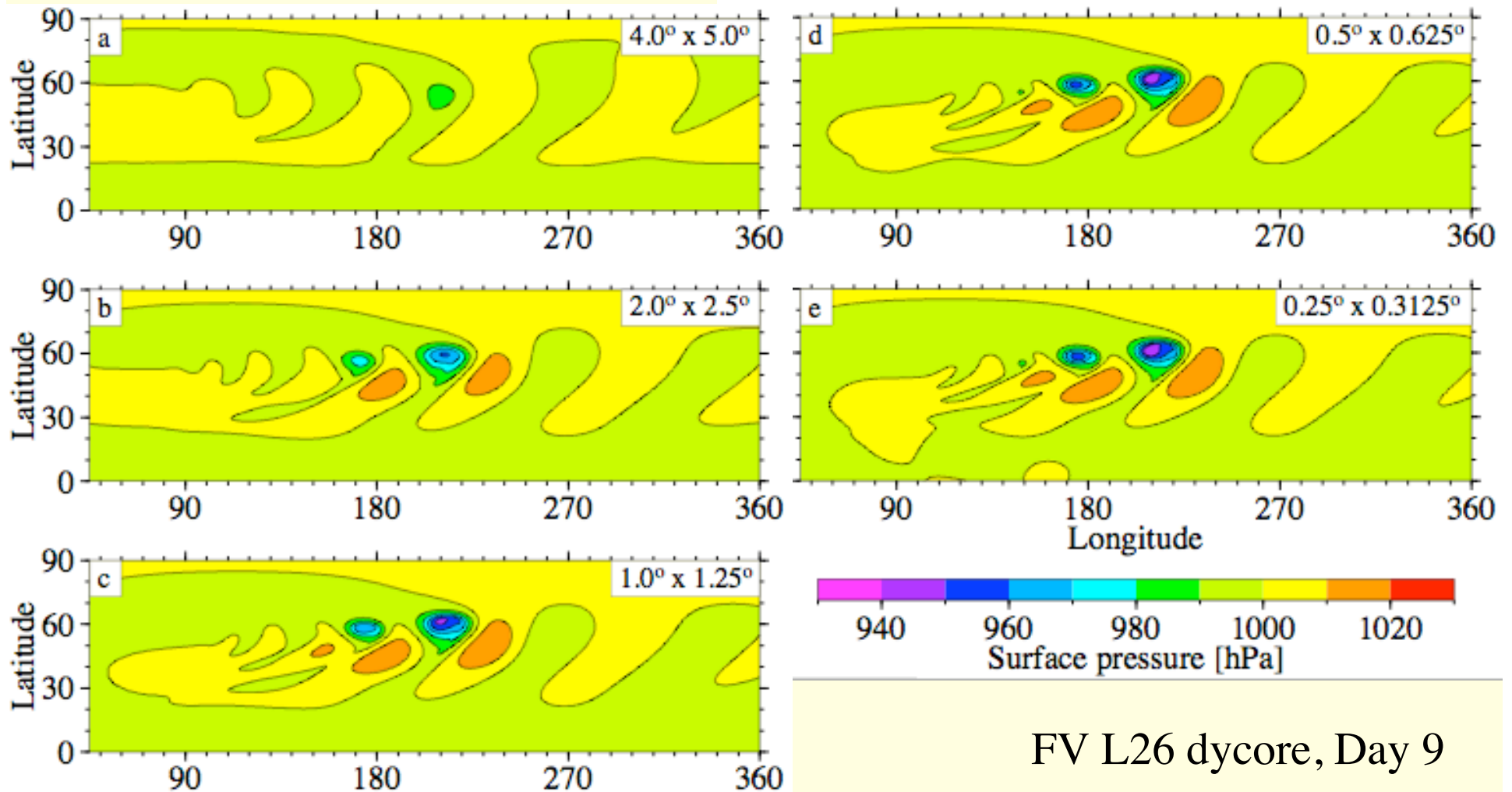
## Test 2) Baroclinic Waves



- 850 hPa temperature field (in K) of an idealized baroclinic wave at model day 9
- Initially smooth temperature field develops strong gradients associated with warm and cold fronts
- Explosive cyclogenesis after day 7
- Baroclinic wave breaks after day 9

# Analysis: Convergence with Resolution

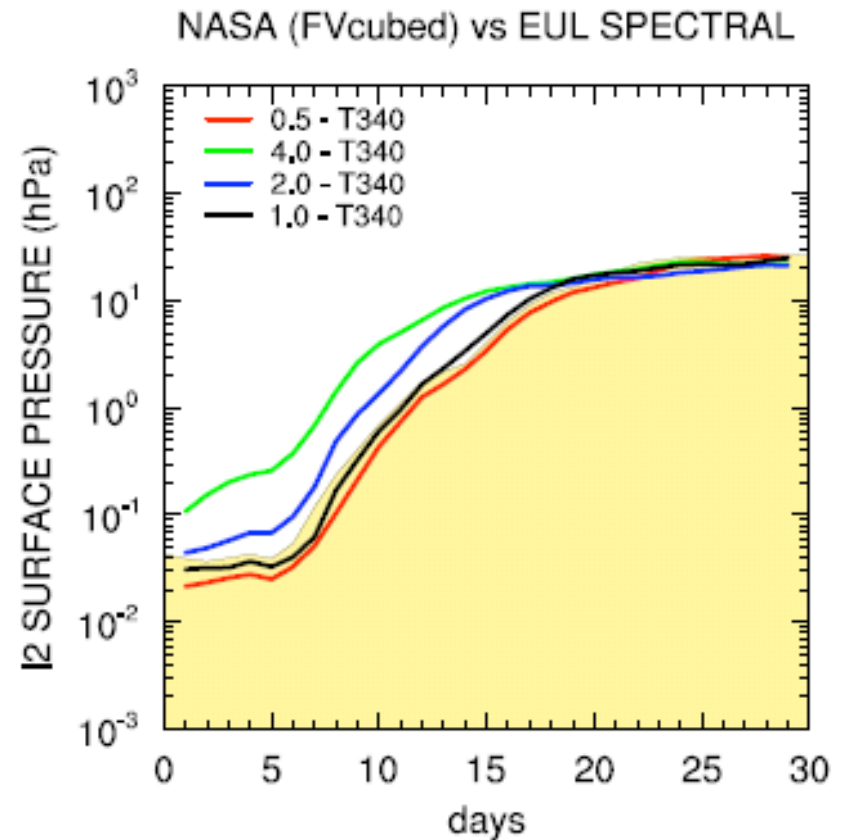
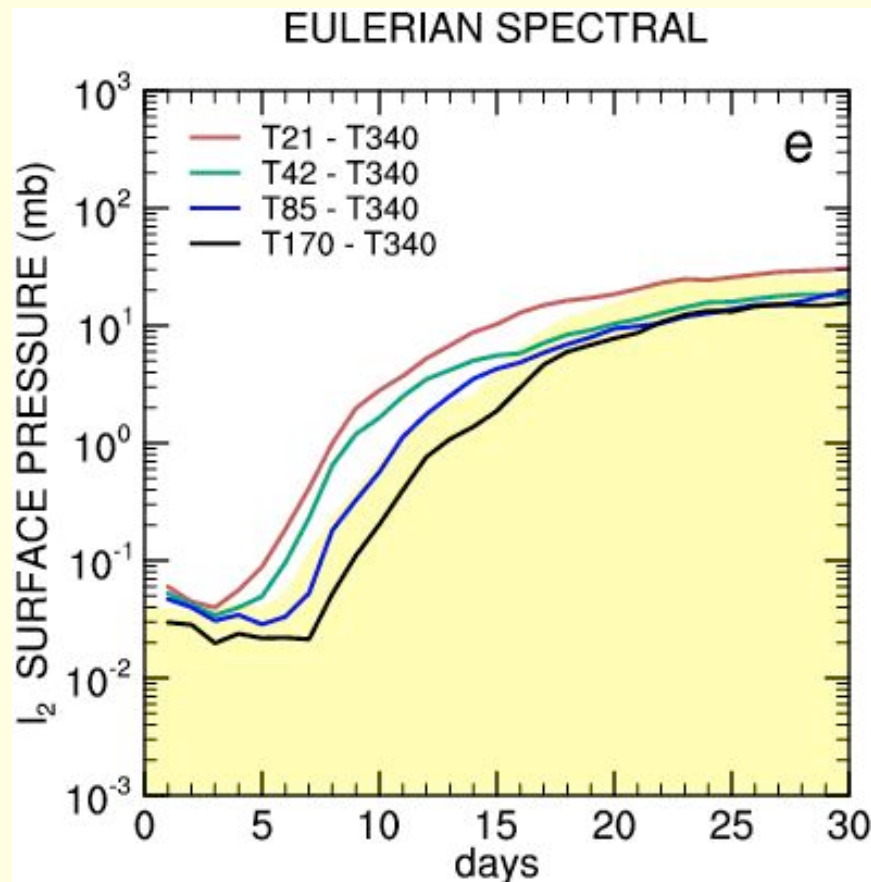
- Surface pressure starts converging at  $1^\circ \times 1.25^\circ$



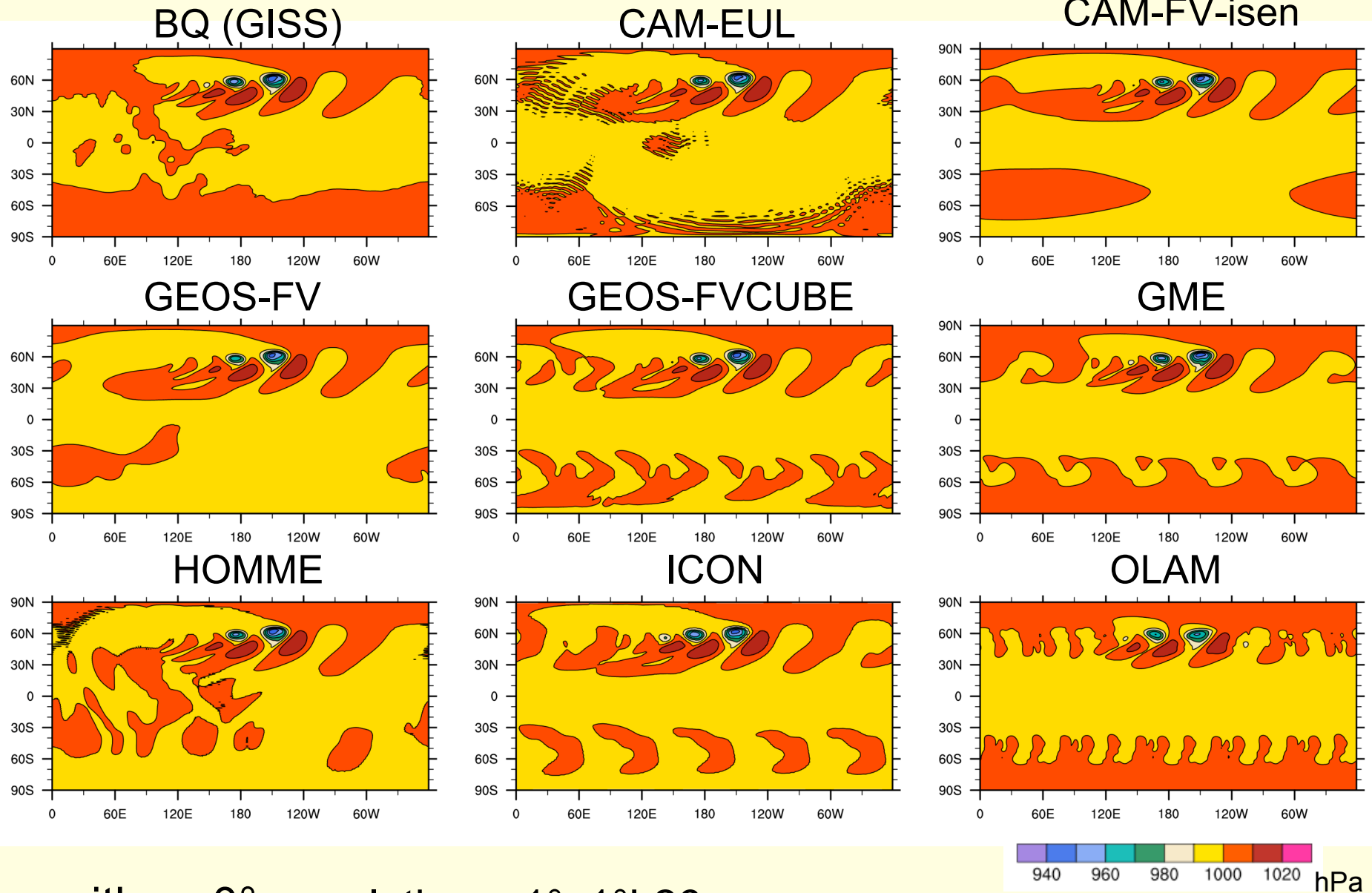
FV L26 dycore, Day 9

# Model Convergence

- Single-model uncertainty stays well below the uncertainty across models
- Models converge within the uncertainty for the resolutions T85 (EUL & SLD), around  $1^\circ$  (FV), GME (55km / ni=128)

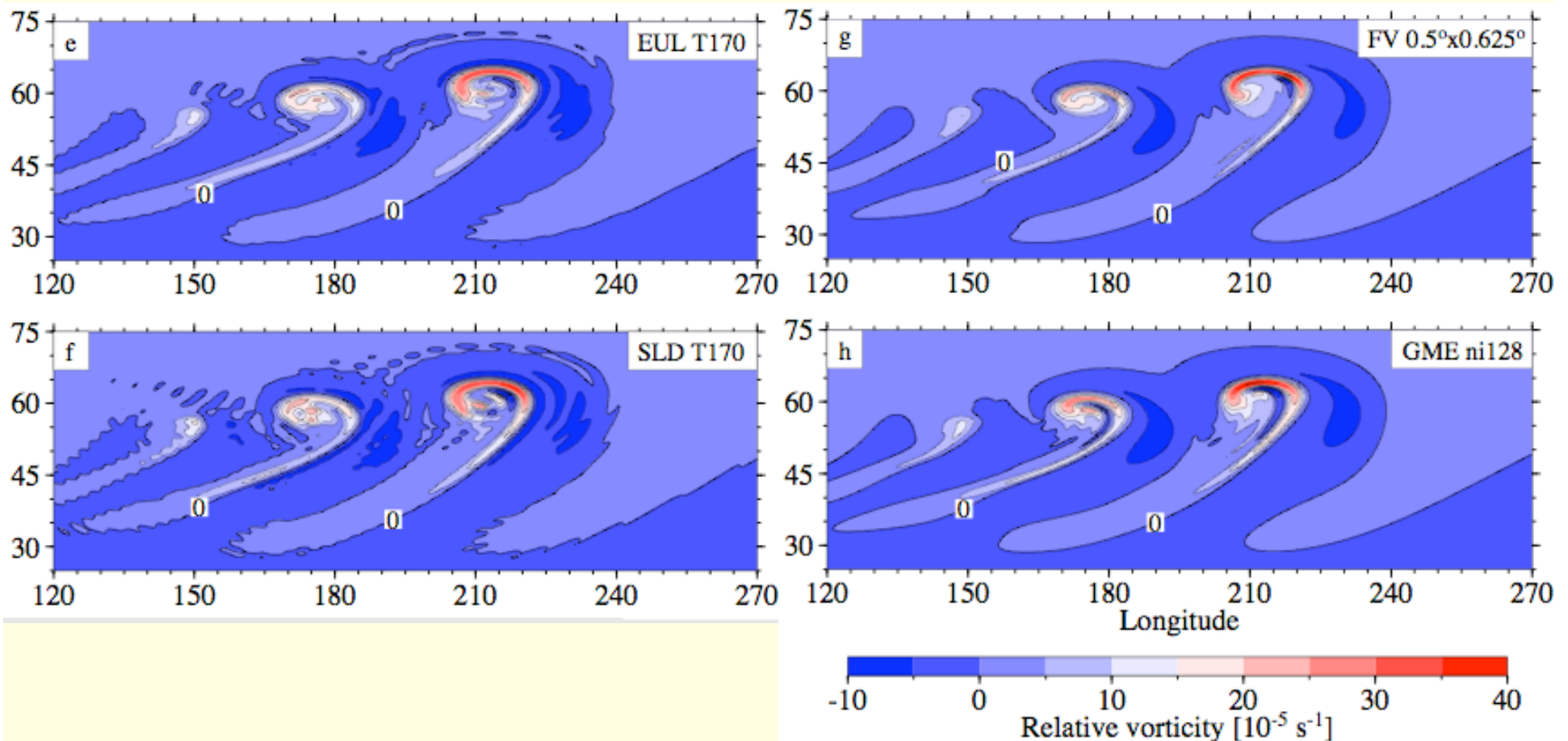


# Model Intercomparison: $p_s$ at Day 9



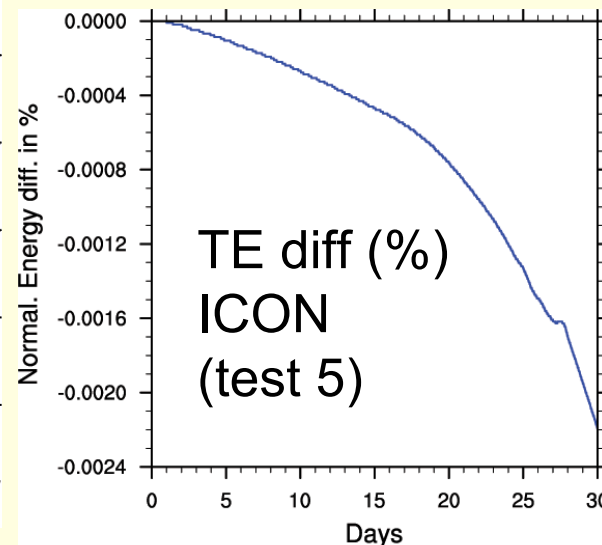
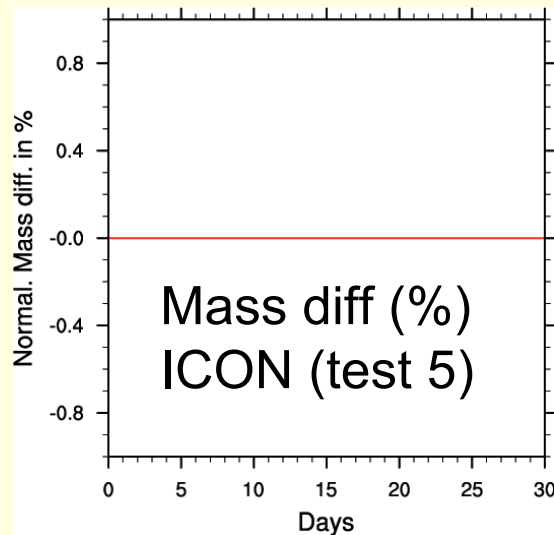
# 850 hPa Vorticity at Day 9

- Differences in the vorticity fields grow faster than  $p_s$  diff.
- Small-scale differences easily influenced by diffusion
- Spectral noise in EUL and SLD (L26)

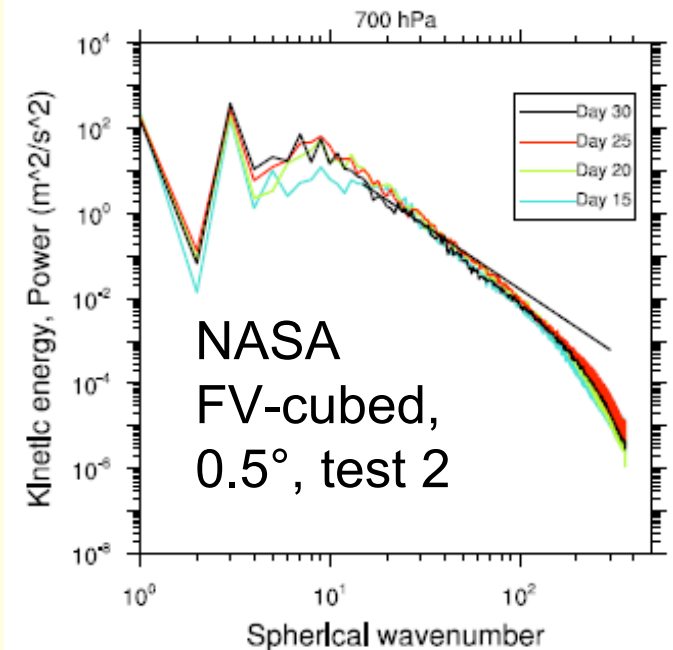
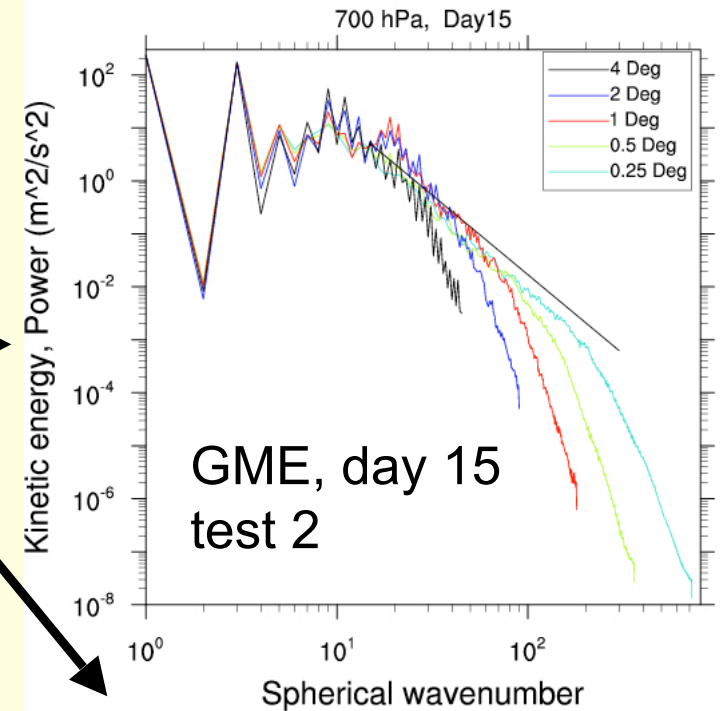


# Standard diagnostics

- **Kinetic energy spectra**
  - Variation with resolution
  - Variation with time
- Assessments of conserved quantities (compute on native grid)
  - **mass**
  - **total energy (TE)**

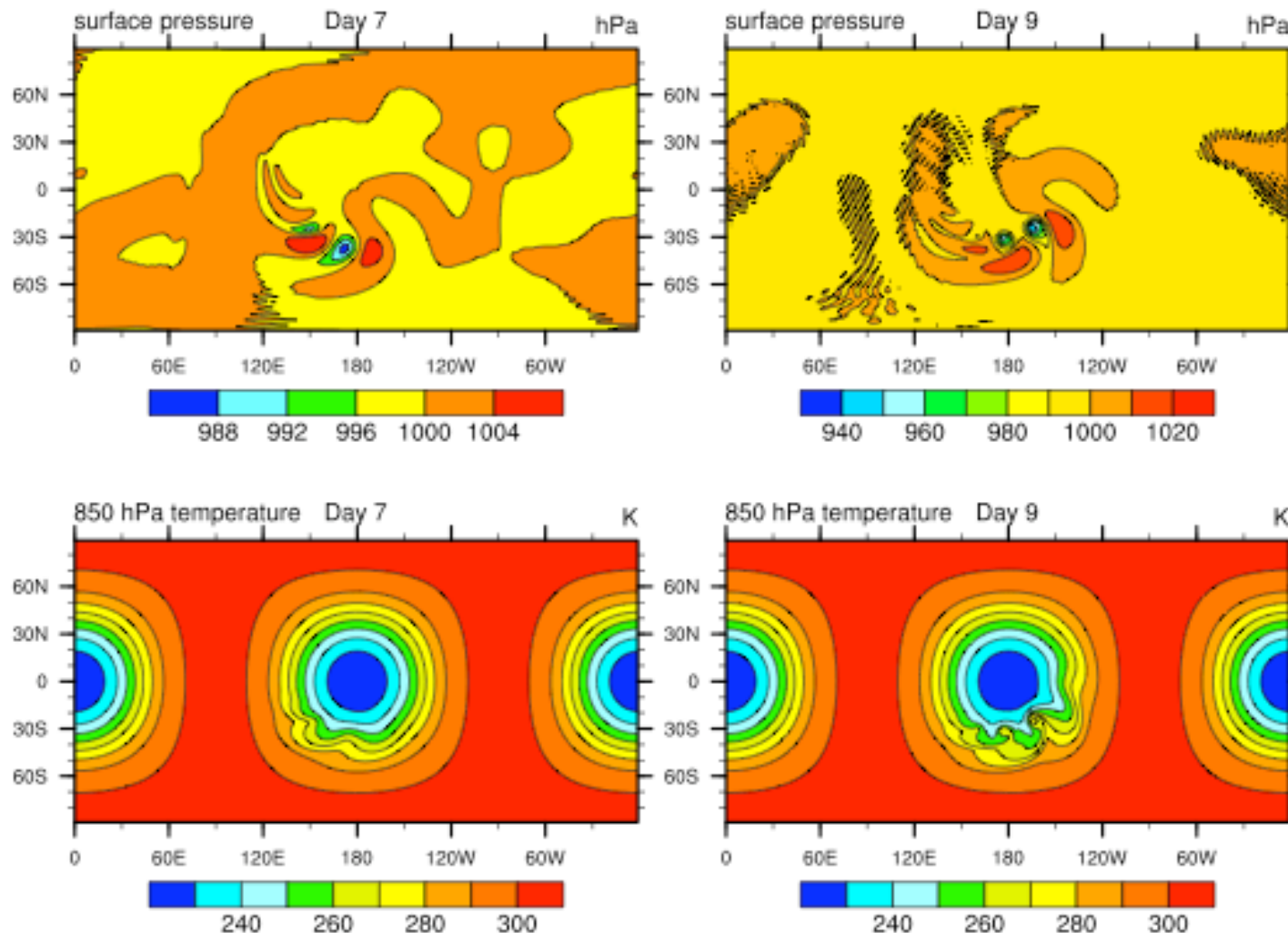


Multi-Scale Kinetic Energy Spectrum (700 mb)



## Test 2 with a rotation angle $\alpha=90^\circ$

- Increase the challenge for models with regular grids



## Test 2 with tracer $q_1(\alpha=0^\circ)$

- Explore the diffusive properties
- Mass conservation
- Over- and undershoots
- Consistency (does a constant stay a constant?)

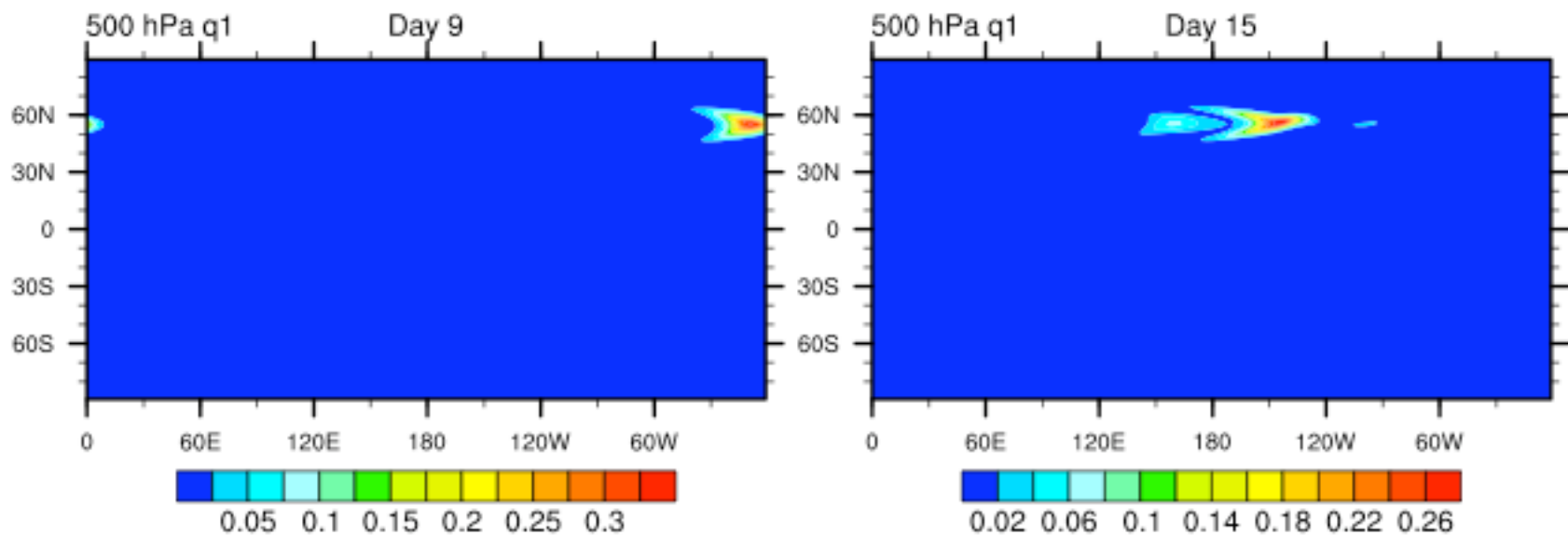
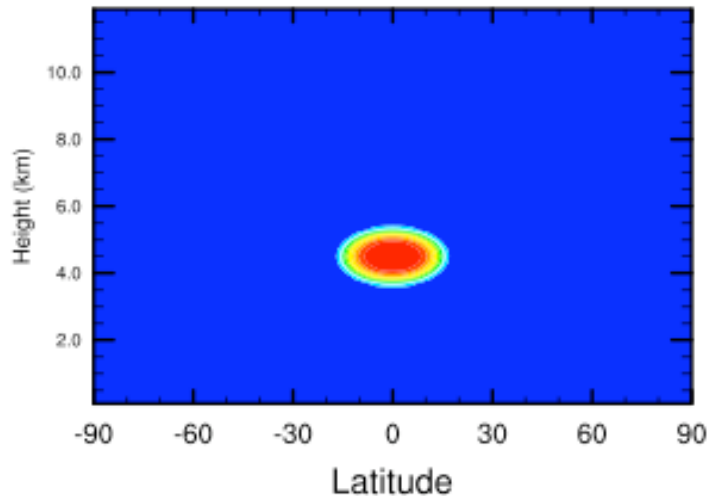


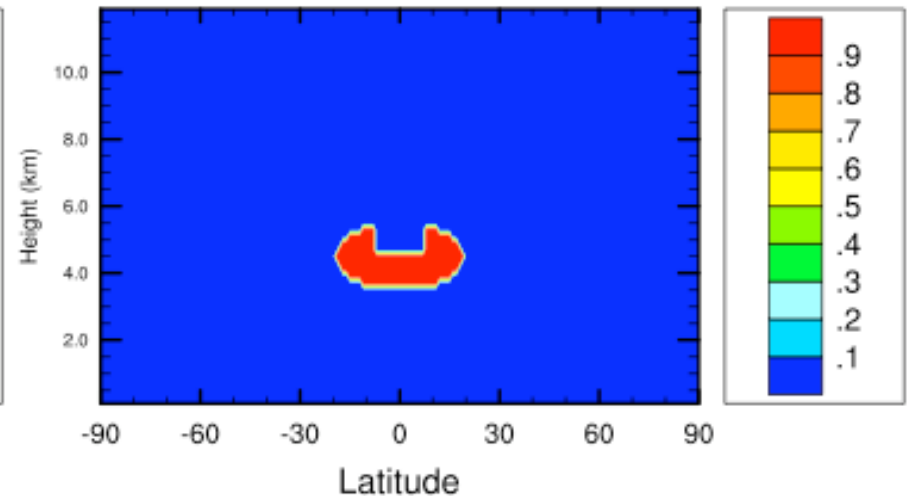
Figure 6: [2-0-1] simulated with EULT106L26: Tracer distribution  $q_1$  at day 9 and day 15 at the pressure levels 700, 600 and 500 hPa. The flow orientation angle is  $\alpha = 0$ .

## Test 3) 3D Advection Tests

Prescribe two 3D tracer distributions:  
Latitude-height cross sections



**Smooth**



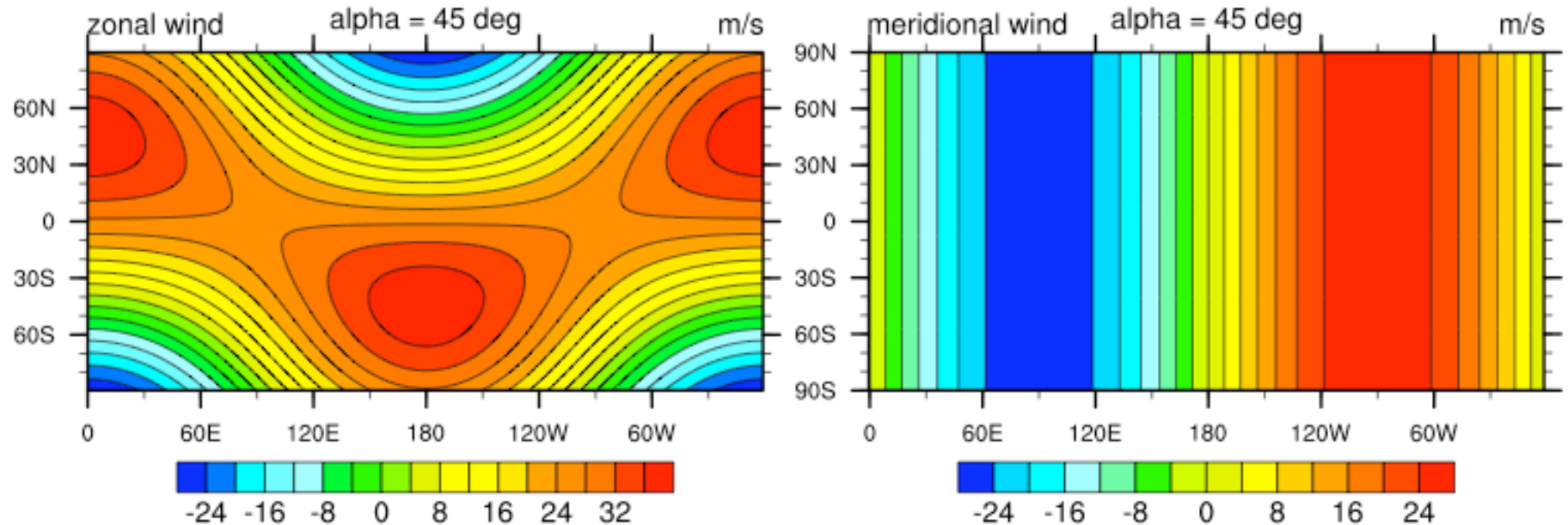
**Non-smooth:  
Slotted ellipse**

## Test 3) Advecting wind speeds

Example: Prescribed horizontal winds with  $\alpha = 45^\circ$

**U**

**V**

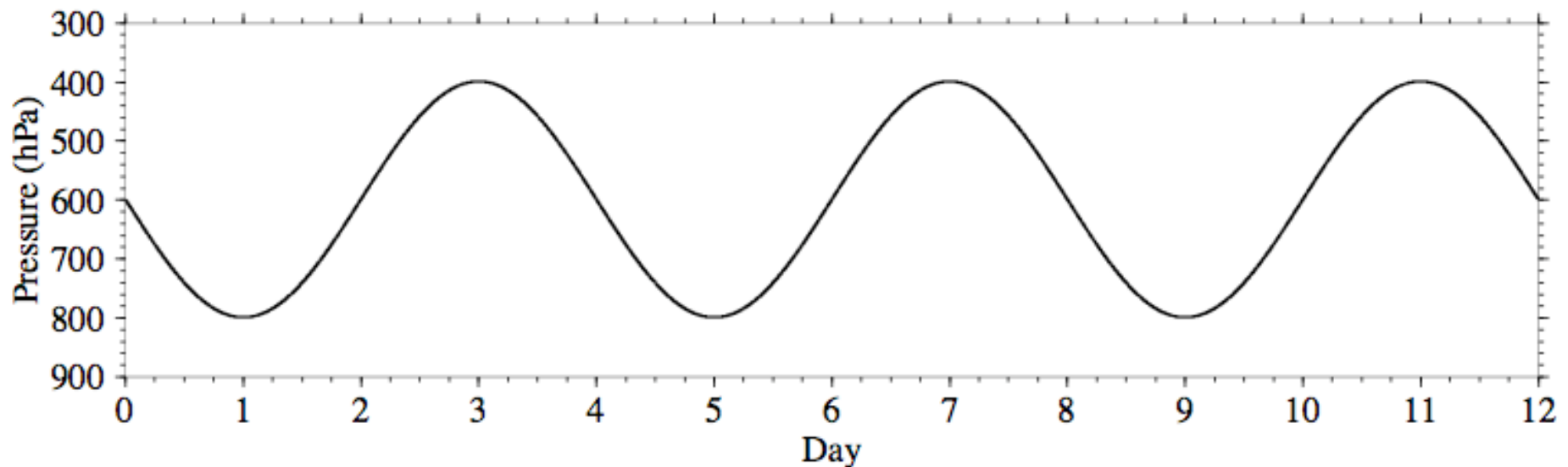


Velocities transport the tracers once around the sphere within 12 days

## Test 3) Vertical advection

Tracers undergo 3 wave cycles in the vertical

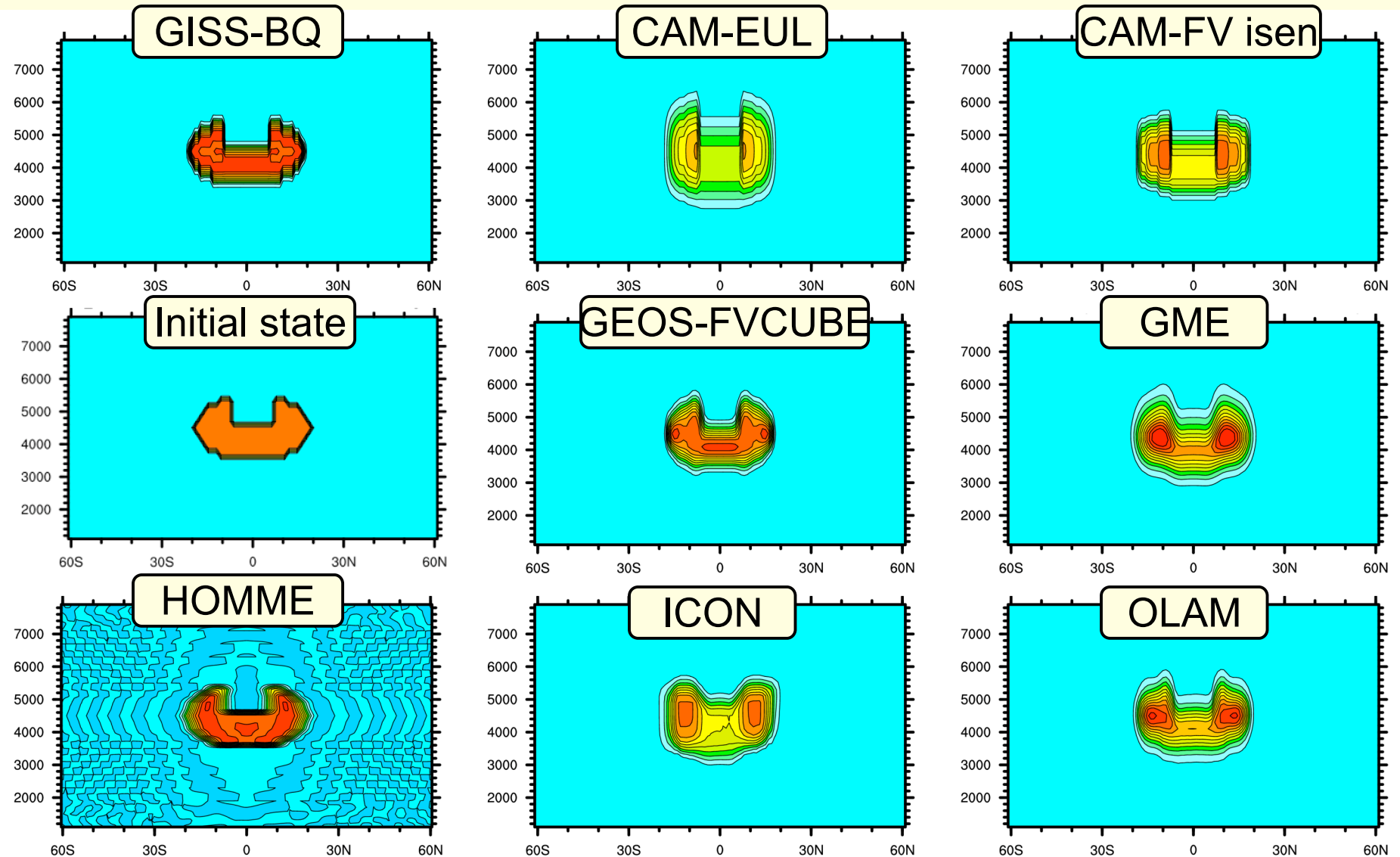
a) Trajectory of the tracer (center position)



Tracers return to initial position after 12 days  
(initial state is analytic solution):

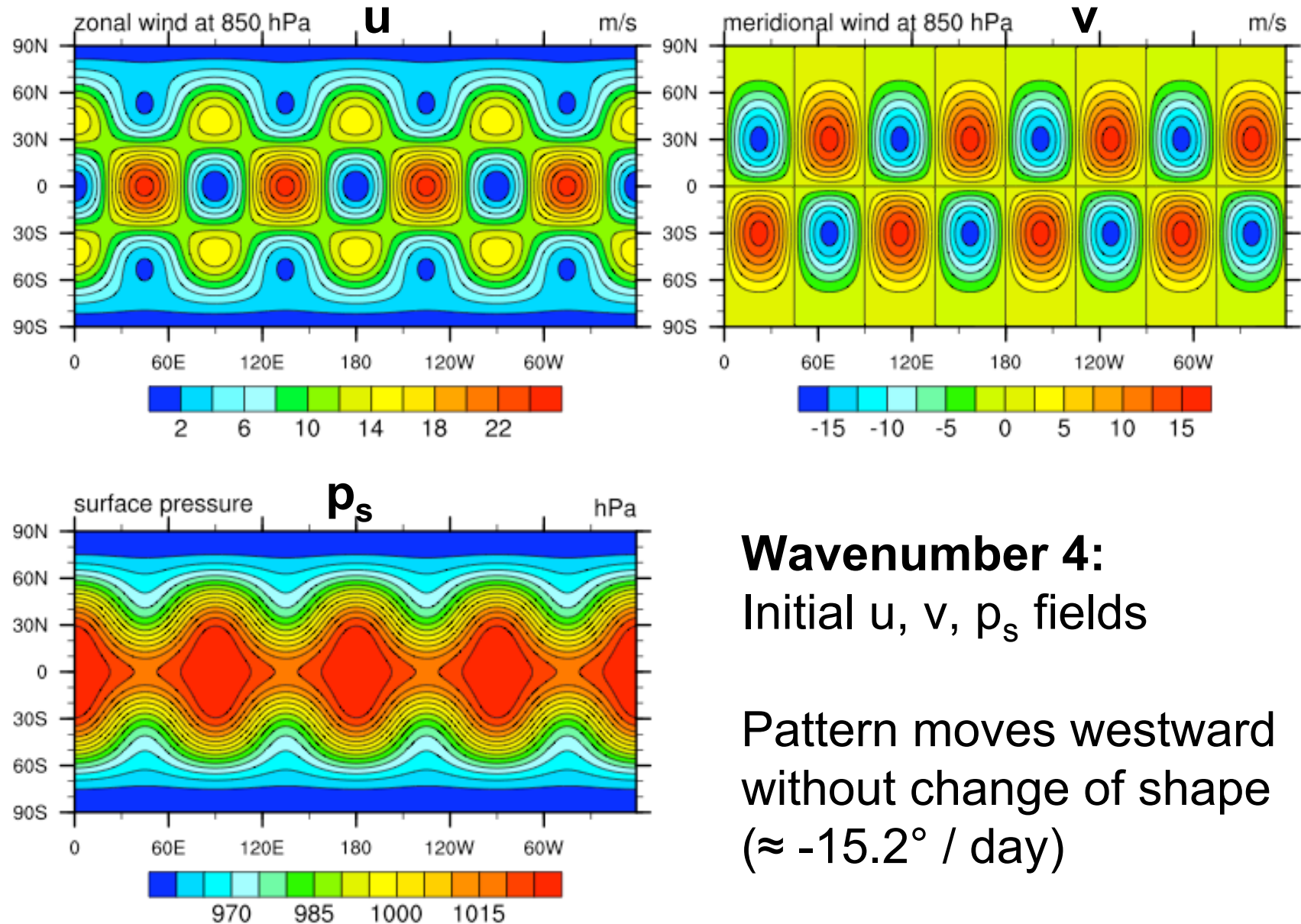
**Allows assessment of the diffusion**

# Test 3) Slotted Ellipse after 12 Days



with  $\alpha=0^\circ$ , ( $\approx 1^\circ \times 1^\circ \text{L60}$ ,  $dz=250 \text{ m}$ )

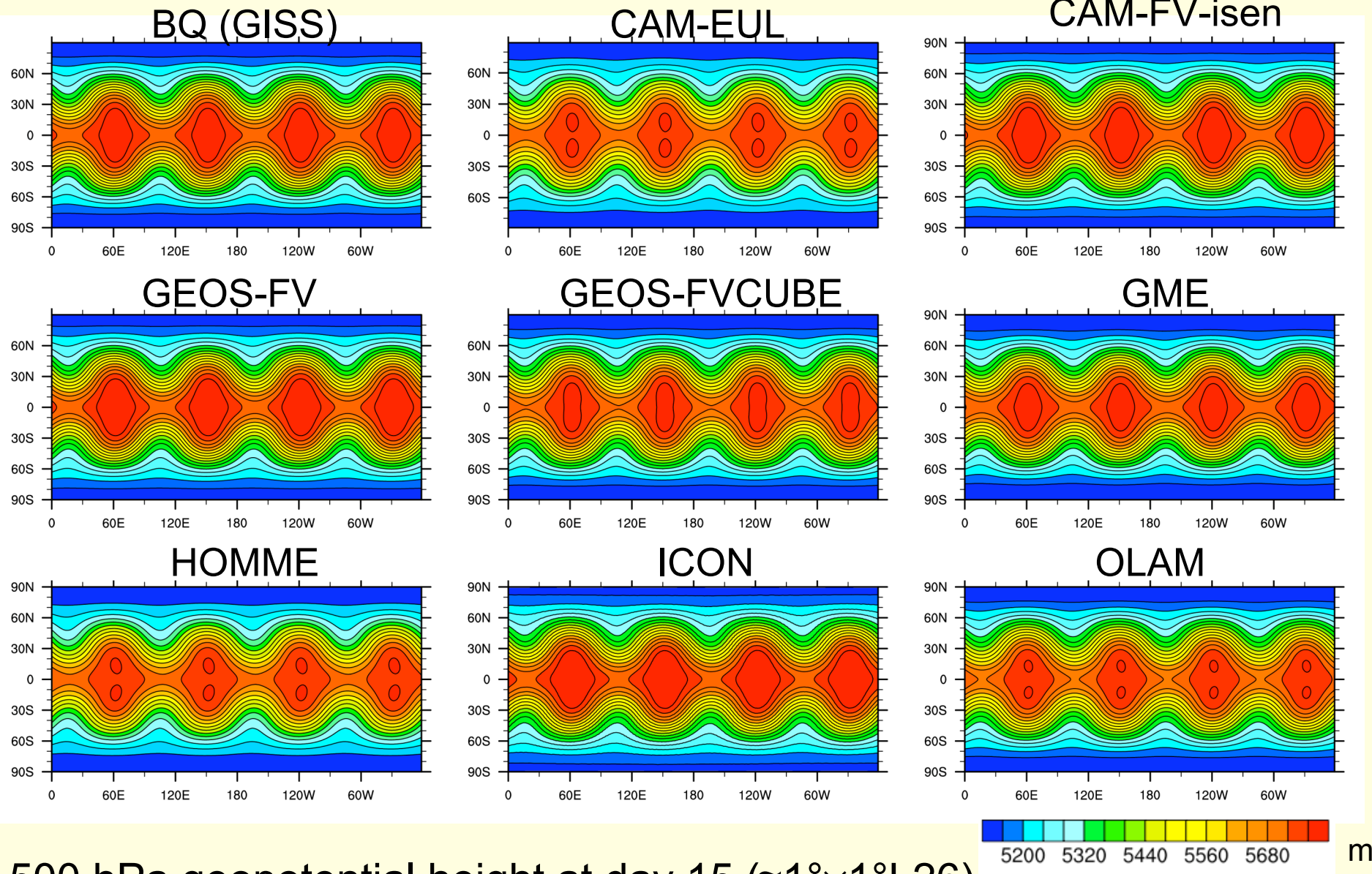
# Test 4) 3D Rossby-Haurwitz Wave



**Wavenumber 4:**  
Initial  $u$ ,  $v$ ,  $p_s$  fields

Pattern moves westward  
without change of shape  
( $\approx -15.2^\circ / \text{day}$ )

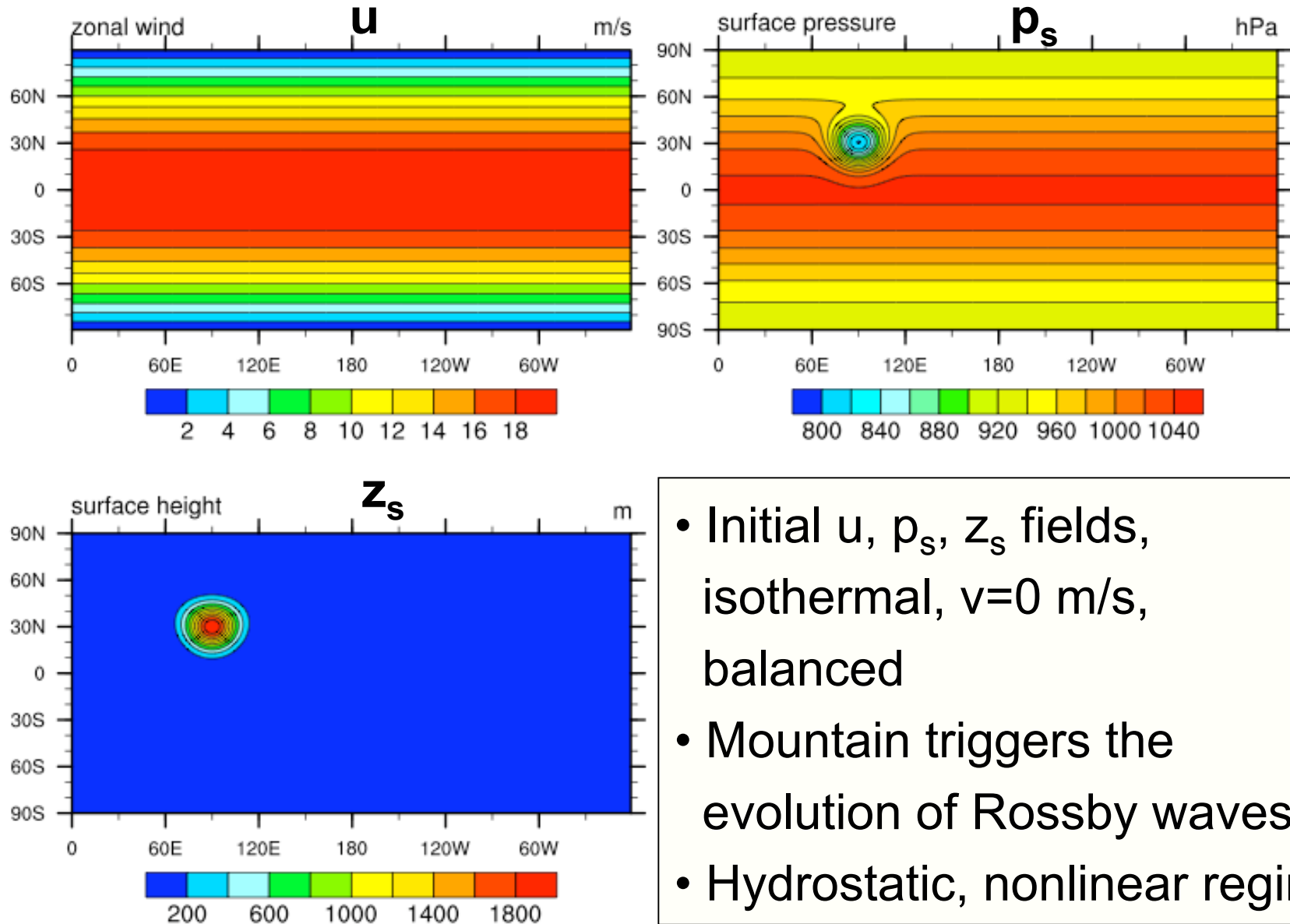
# Test 4: Assess diffusion and symmetry



500 hPa geopotential height at day 15 ( $\approx 1^\circ \times 1^\circ$  L26)

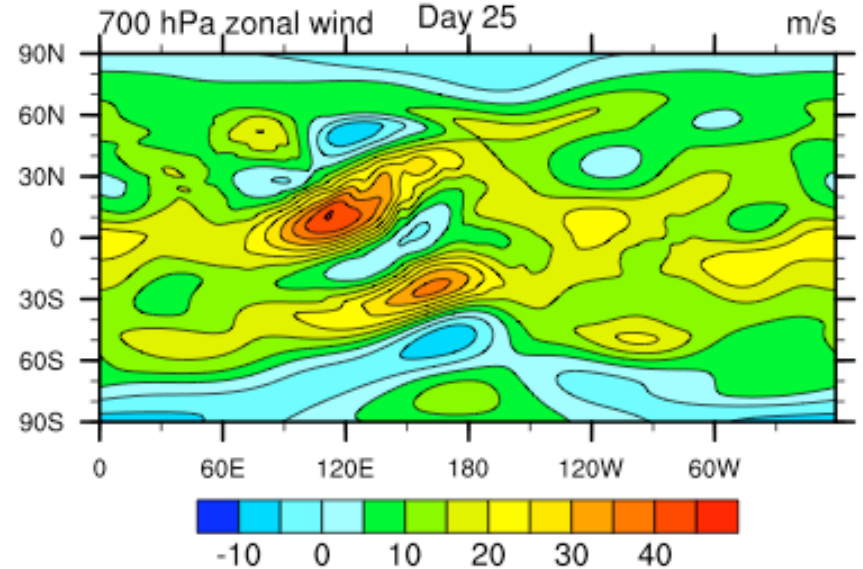
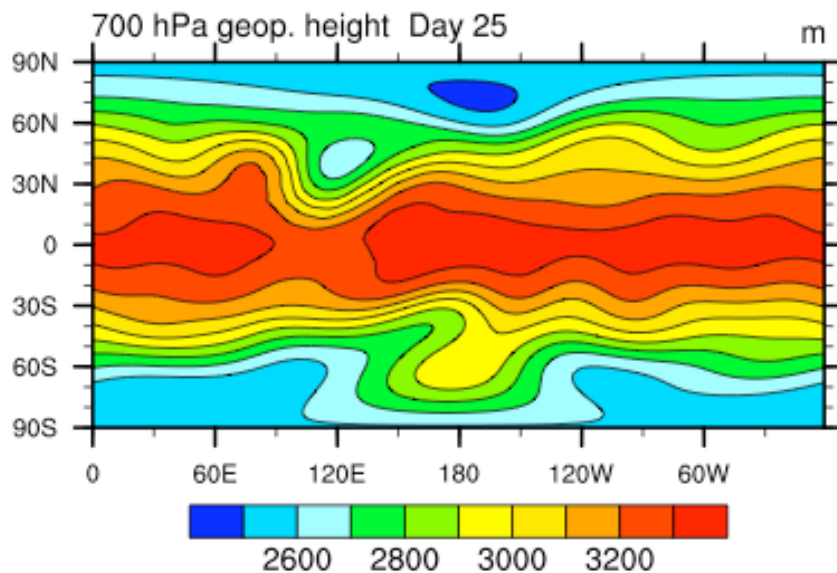
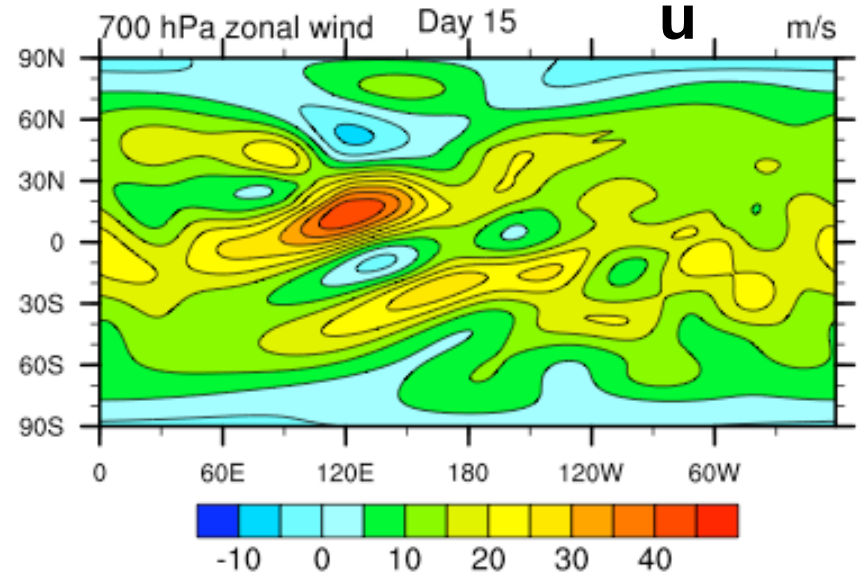
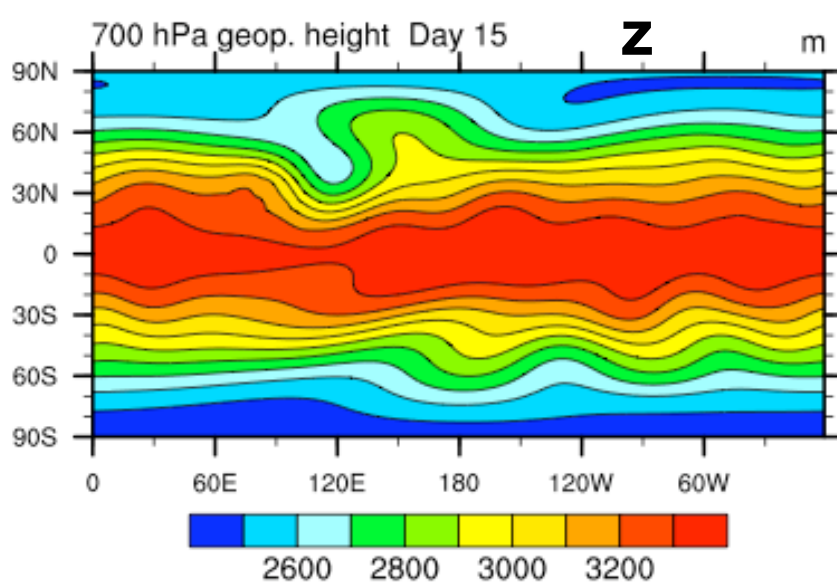
m

# Test 5) Mountain-induced Rossby waves

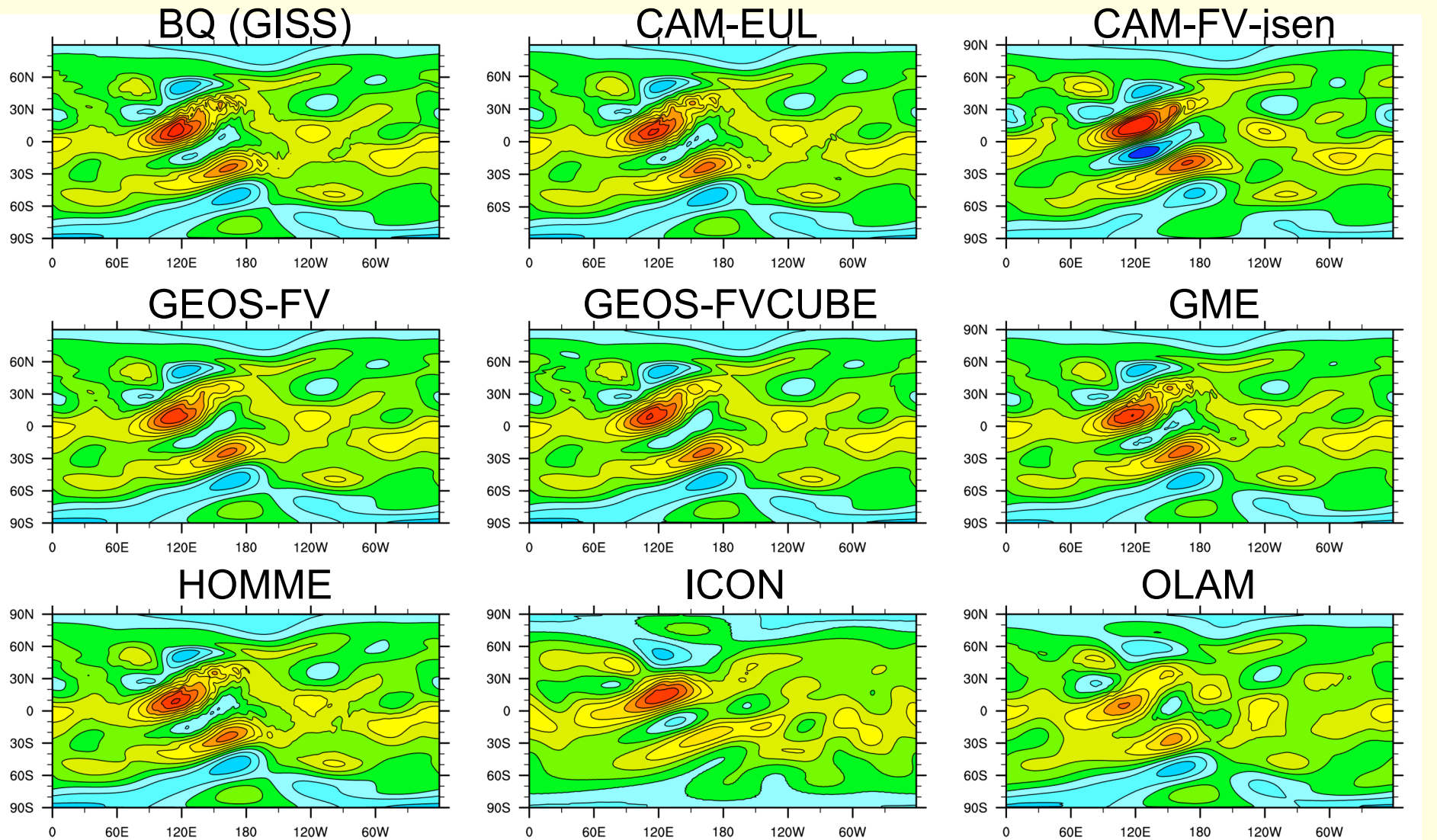


# Days 15 & 25: Mountain-induced waves

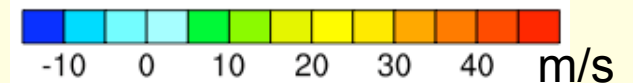
CAM-FV 180x360L26



# Day 25: Mountain-induced waves - noise?

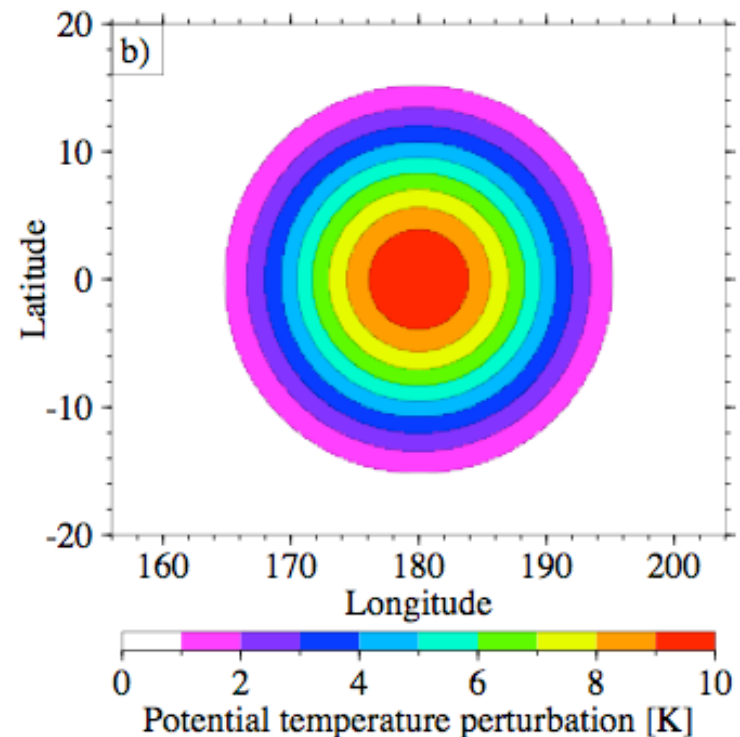
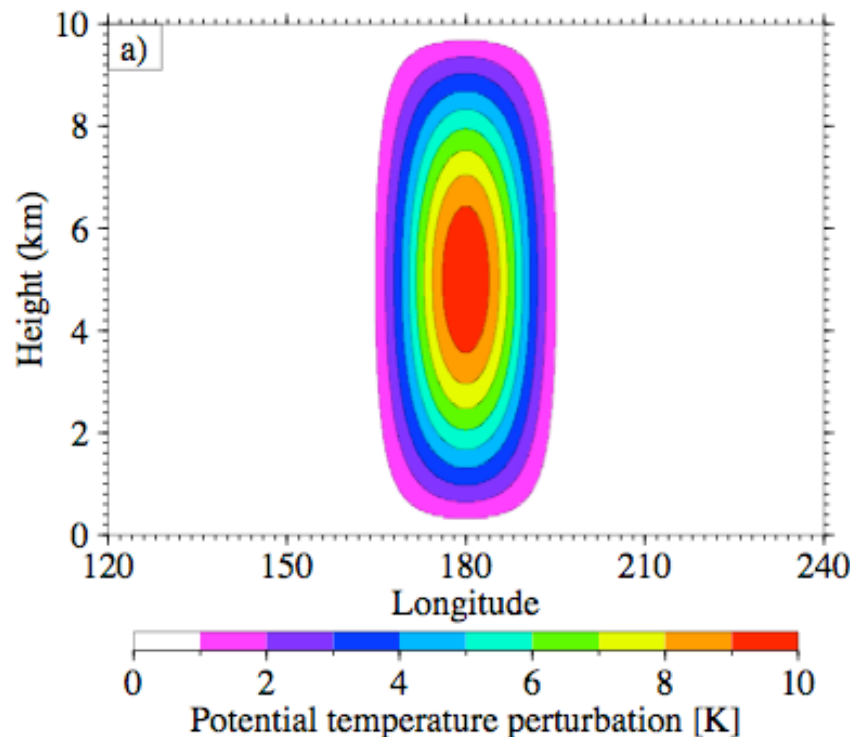


700 hPa zonal wind at day 25 ( $\approx 1^\circ \times 1^\circ$  L26)

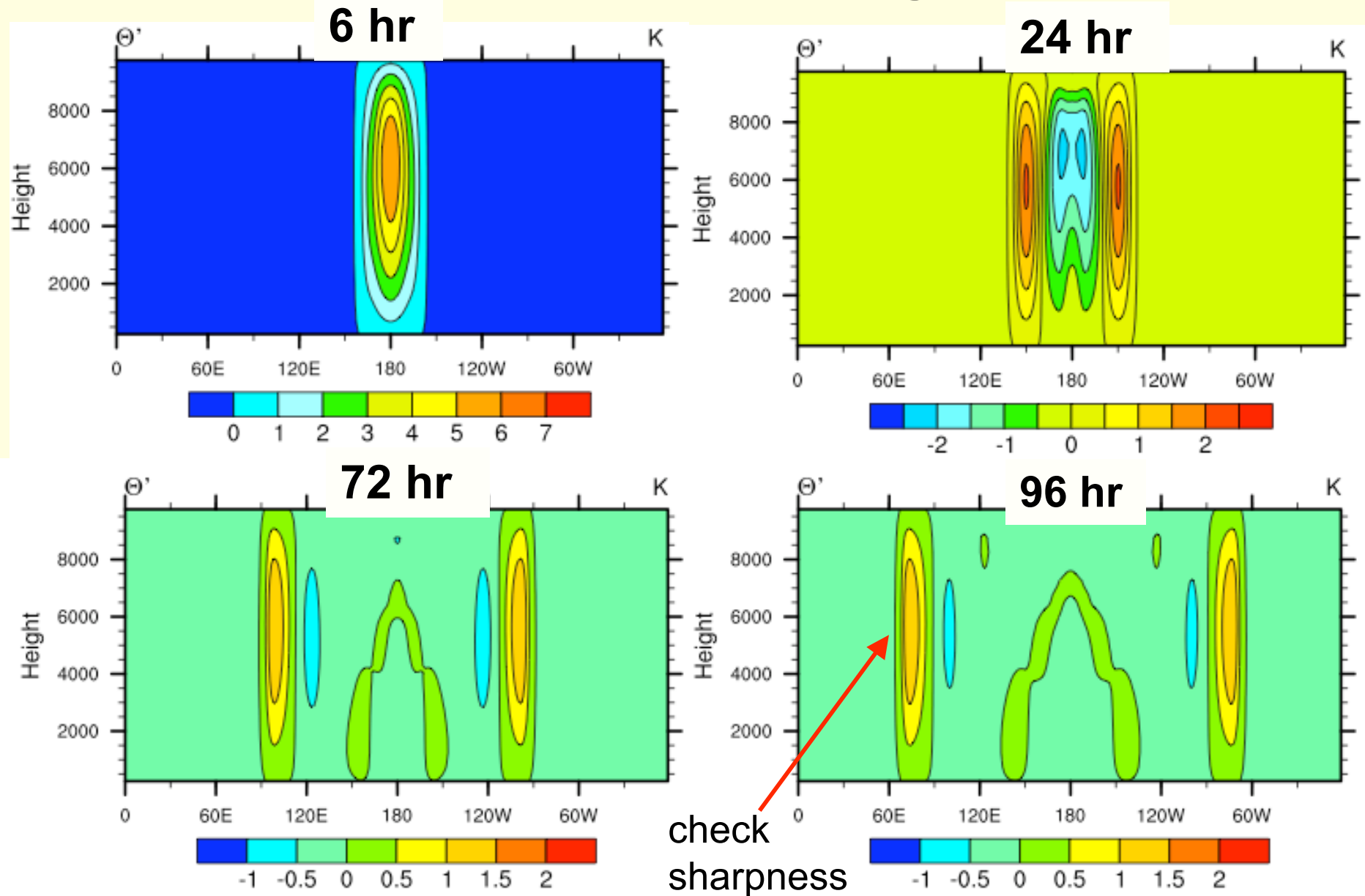


# Test 6) Gravity Waves, Inertial Gravity Waves

- No rotation in test [6-0-0], rotation in [6-3-0]
- Balanced initial state with potential temperature perturbation
- Perturbation triggers hydrostatic gravity waves

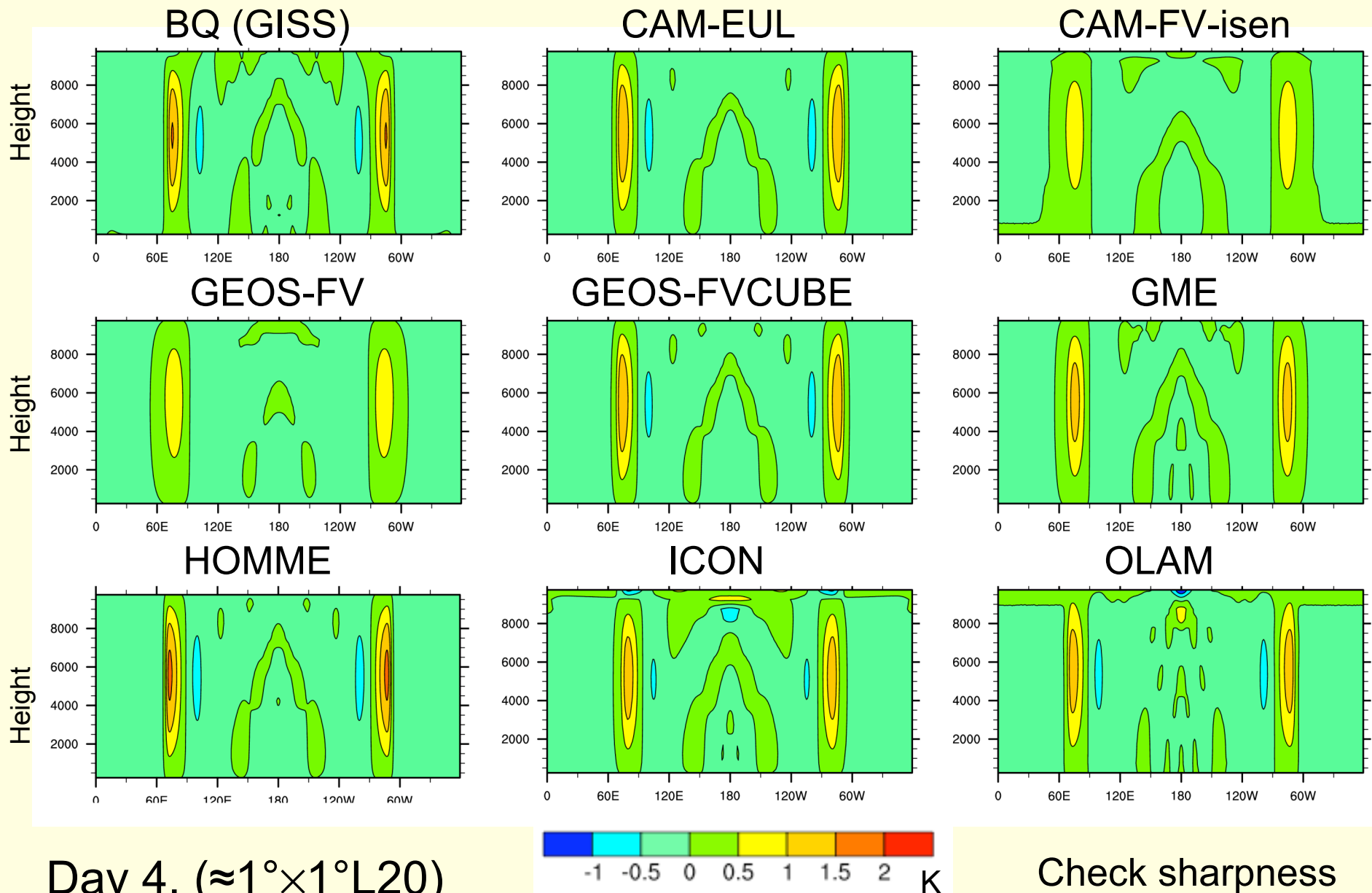


# [6-0-0]: $\Theta'$ cross section along the equator



CAM-EUL T106 L20 with standard diffusion

# [6-0-0]: $\Theta'$ cross section along the equator



# Dynamical Core Intercomparison

- Modeling mentors and students produced a 1.2 TB data base that is open to the community
- Data files are stored as netcdf files and are available on the Earth System Grid, our gateway is <http://dycore.ucar.edu>
- We work closely with the Earth Curator Project (NCAR group in CISL):  
<http://www.earthsystemcurator.org>  
to provide Metadata that describe the model configurations
- We provide NCL scripts for standard evaluations

# Observations

- Test suite used during the ASP colloquium got very positive feedback from the modeling community
- We suggested specific diagnostics and the evaluation of specific time snapshots
- Tests have different complexities:
  - Pure advection
  - Irrotational
  - Steady state
  - Idealized topography
  - From large to small scales, nonlinear barclinic waves
- Next version of the test suite needs
  - More nonlinear, small-scale tests
  - Non-hydrostatic tests on the sphere
  - More diagnostics
  - Extensions/provisions for deep-atmosphere dynamical cores
  - Simplified physics?

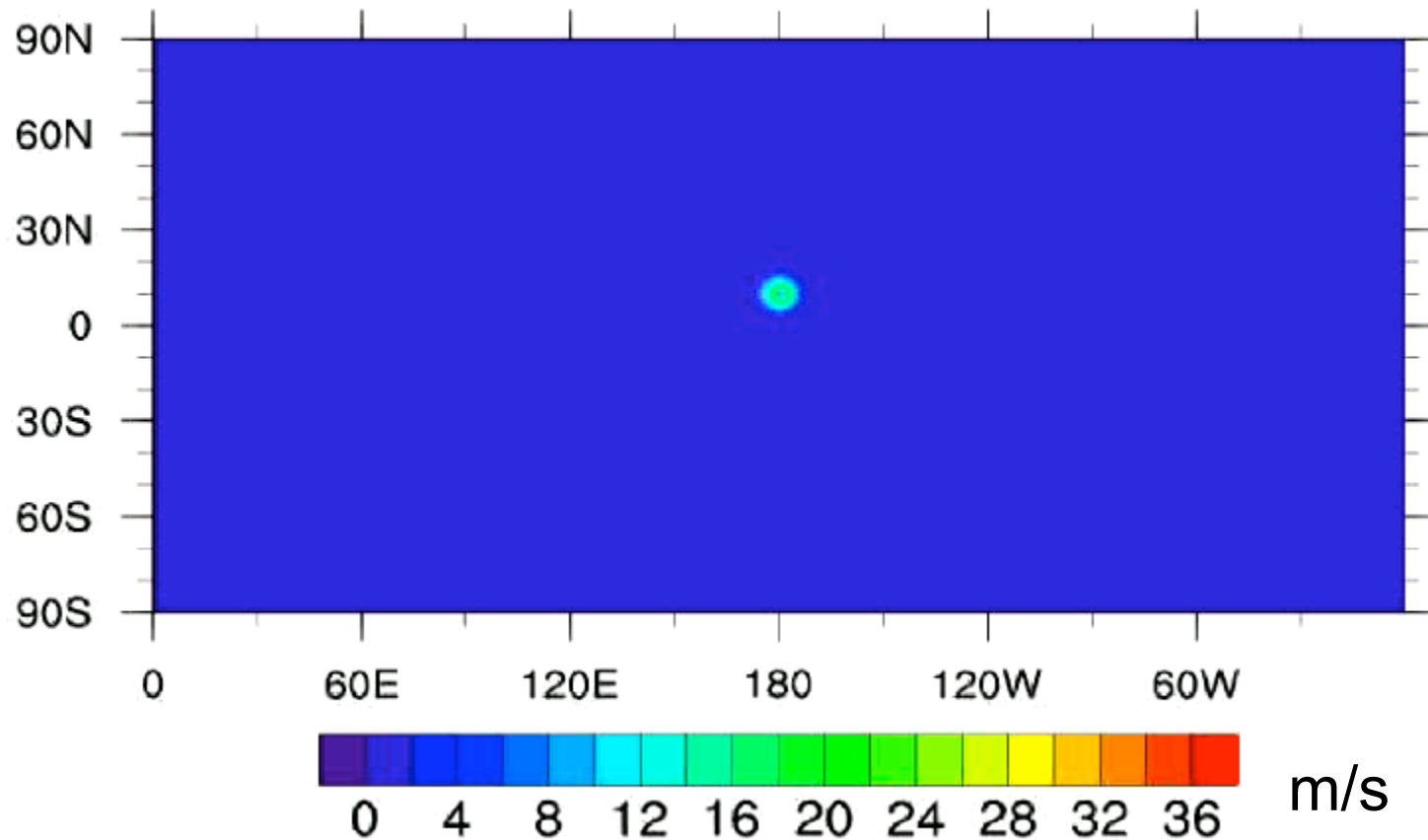
# Future test case candidates

- 3D Mountain Waves (irrotational) on the sphere: hydrostatic & non-hydrostatic, linear & non-linear
- Acoustic Waves (non-hydrostatic)
- Dycore tests with more complex (or real) orography
- Unsteady tests with analytic solutions (Staniforth and White, QJ (in review), time-dependent Coriolis force
- Steady-state, deep atmospheres (Staniforth and White, QJ (2007))
- 3D Advection with divergent and convergent flows
- Idealized cyclones:
  - Prescribed tropical vortex with balanced initial conditions, ocean-covered surface with specified (e.g. constant) SST, (see 1st movie)
  - Qualitative similar test possible with the shallow water equations (Lin, Putman) (see 2nd movie)
  - On a smaller scale: idealized tornados

# Idealized (Tropical) Cyclones

CAM3.1 - FV dycore, 15-day aqua-planet run with  $0.5^\circ \times 0.5^\circ$  L26

Wind speed near the surface, hour=0



Kevin Reed and Christiane Jablonowski