



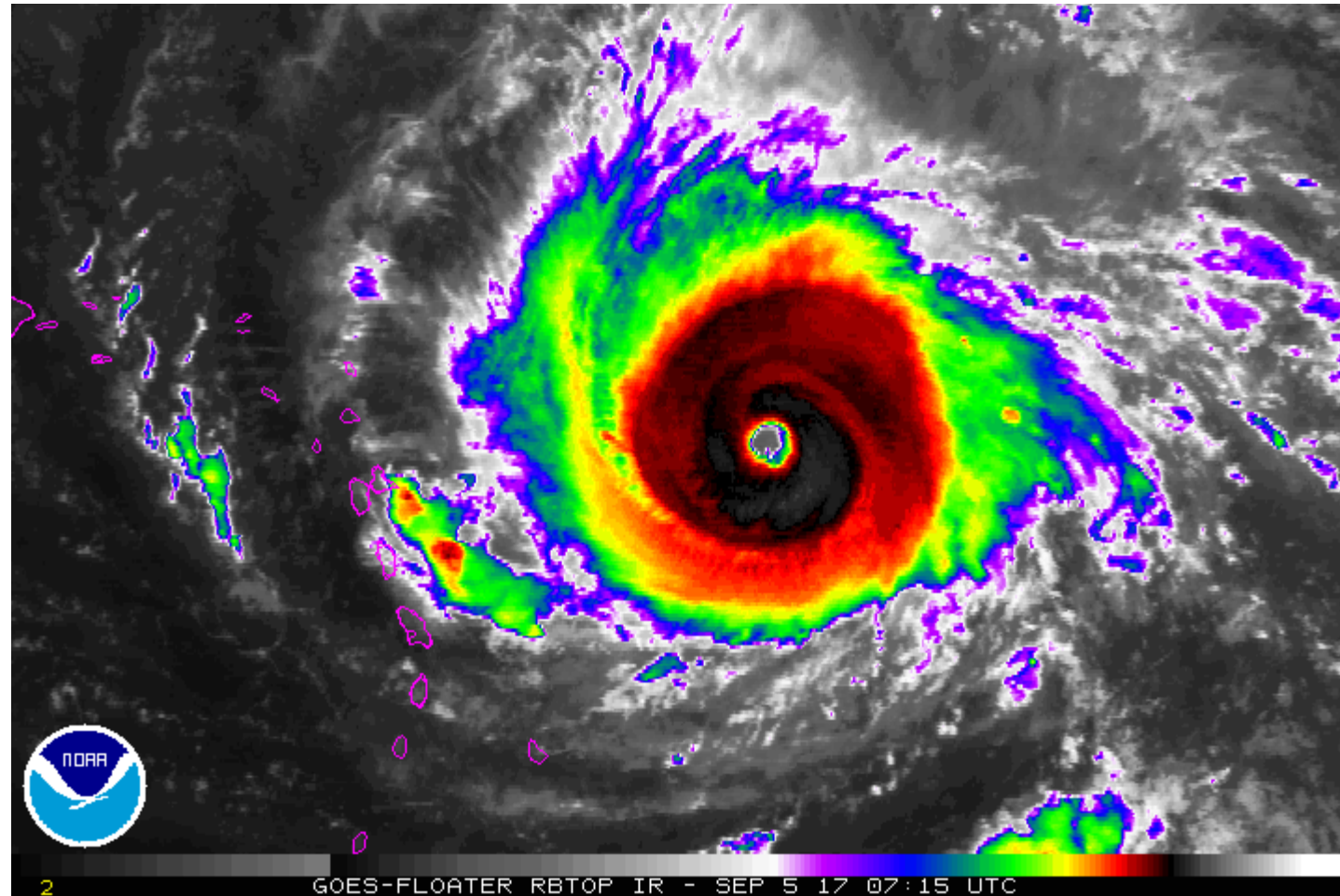
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Mass Flux in Hurricane Irma

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Hurricane Irma



Hurricane Irma

- Hurricane Irma was an extremely powerful and catastrophic Cape Verde hurricane, the strongest observed in the Atlantic in terms of maximum sustained winds since Wilma, and the strongest storm on record to exist in the open Atlantic region. [Wikipedia](#)
- **Total fatalities**: 134
- **Highest wind speed**: 177 mph
- **Date**: August 30, 2017 – September 13, 2017
- **Affected areas**: [Florida](#), [Cuba](#), [Saint Martin \(Island\)](#), [Puerto Rico](#), [MORE](#)
- **Category**: Category 5 Hurricane (SSHWS), Category 4 Hurricane (SSHWS), Category 1 Hurricane (SSHWS)
- **Did you know**: Irma is the fifth-costliest Atlantic hurricane (\$64.8 billion in damage). [wikipedia.org](#)

https://en.wikipedia.org/wiki/Hurricane_Irma

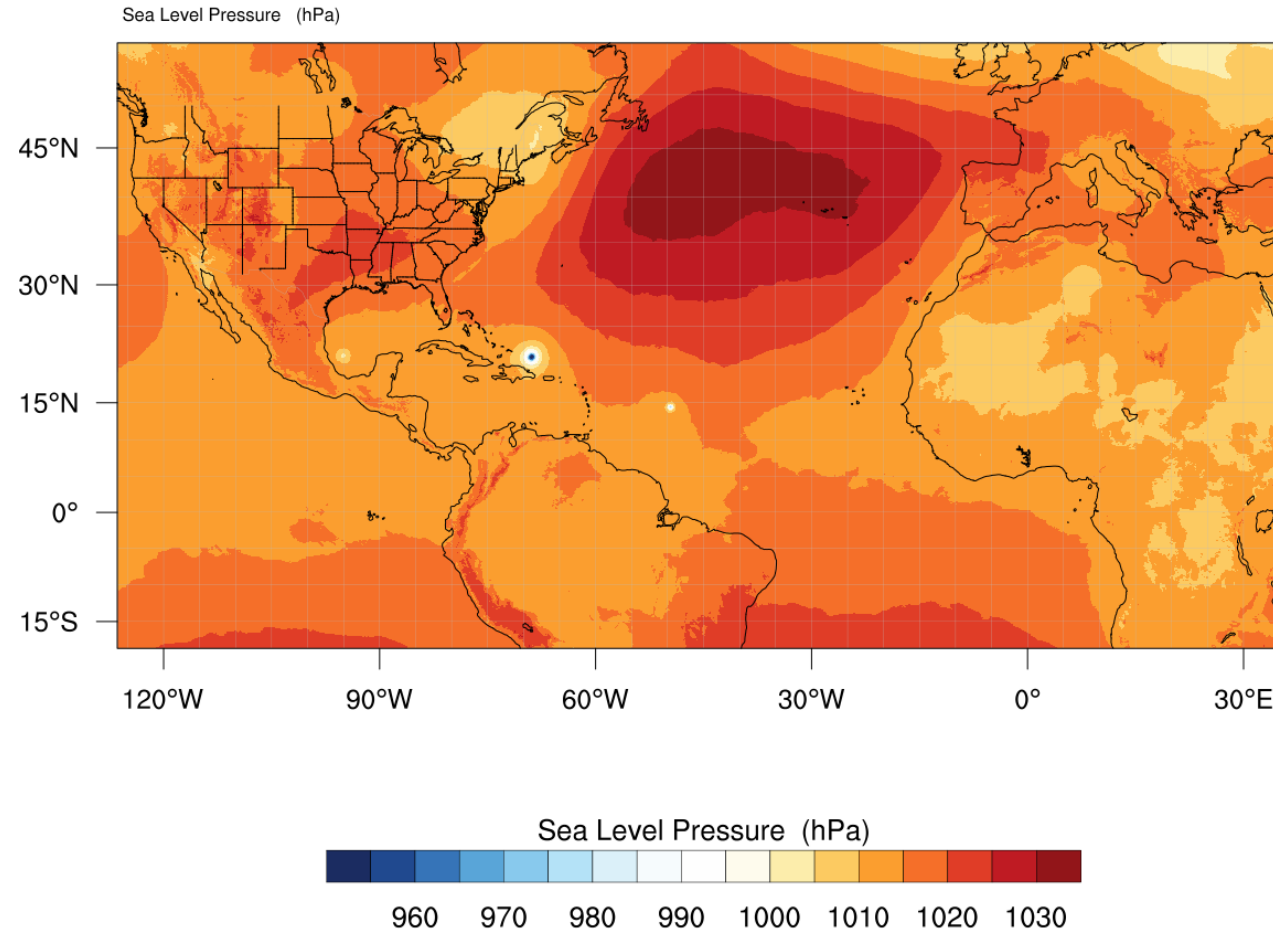
Case Setup

- 2017.9.06 Hurricane Irma*
- Grid: x-3100, y-1600, z-45*
- Resolution: 5.4 km*
- Forecast: 6 days*
- Output Frequency: 1 hour*
- Time step: 20 seconds*

Sea Level Pressure at Full Domain

Full-domain SLP at 2017-09-07_12:00:00

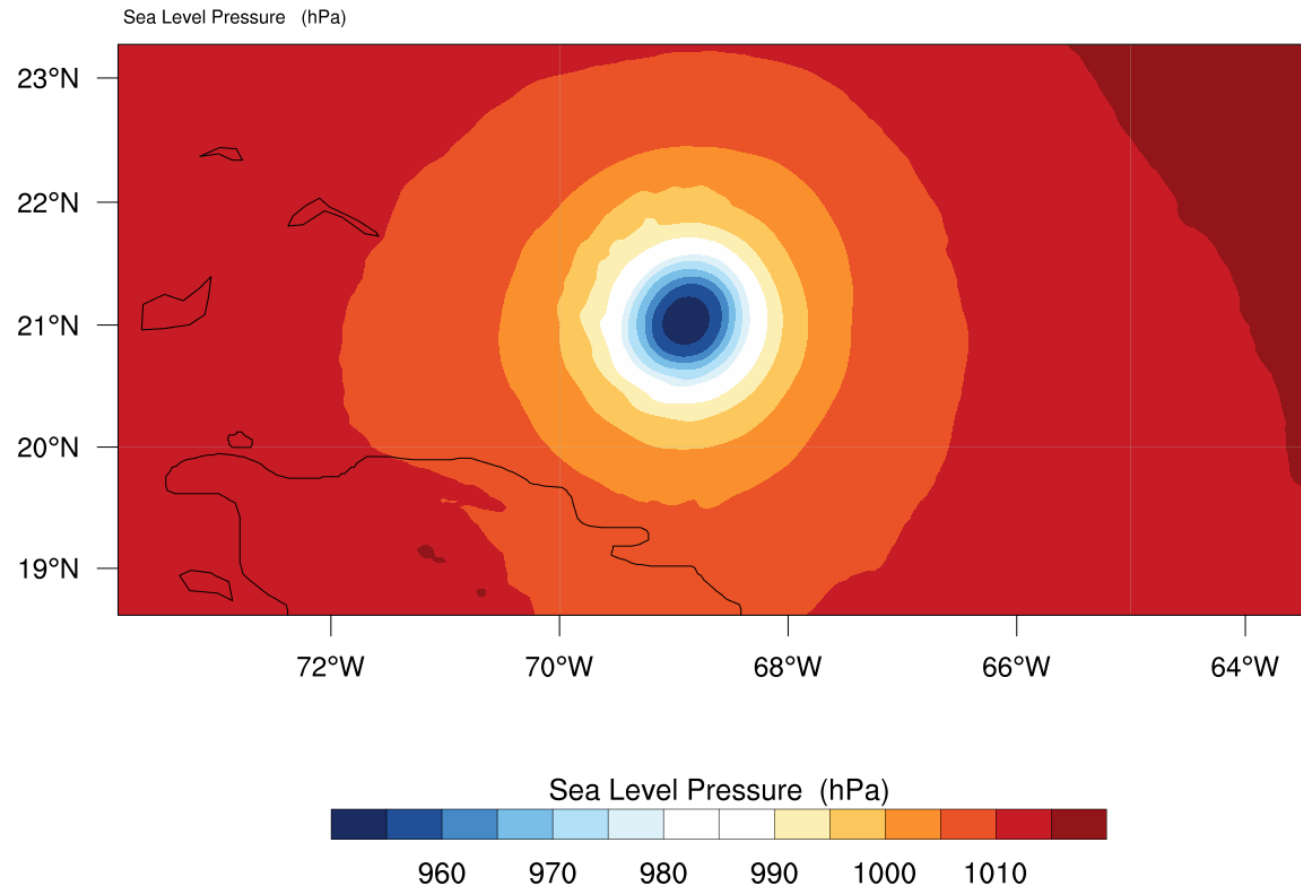
Init: 2017-09-06_06:00:00



Sea Level Pressure at Sub-domain

Sub-domain SLP at 2017-09-07_12:00:00

Init: 2017-09-06_06:00:00



Calculate Mass Flux

–Continuity equation:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \vec{V}) = 0 \quad (1)$$

–Can be rewrite as:

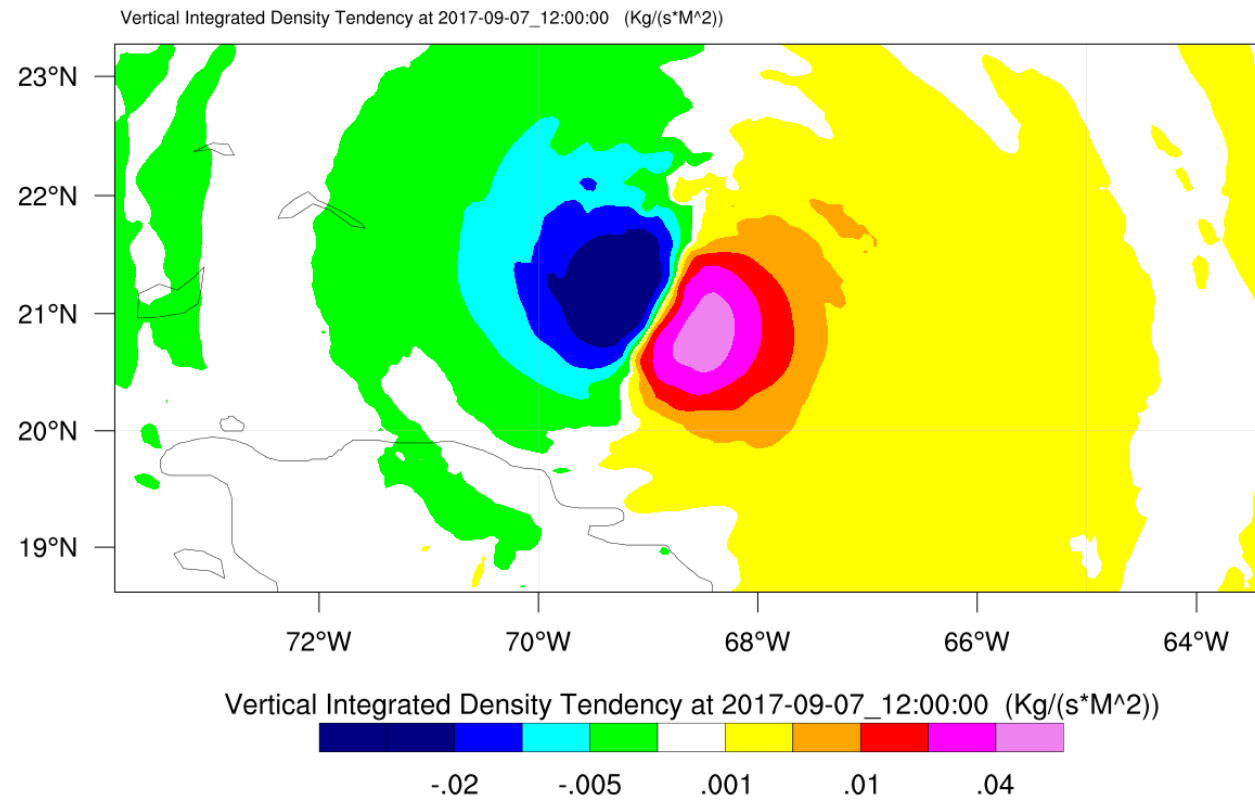
$$\frac{\partial \rho}{\partial t} = -\nabla \cdot (\rho \vec{V}) \quad (2)$$

–Integrate the above equation along vertical direction to get air column mass change at left hand side, and mass flux at right hand side.

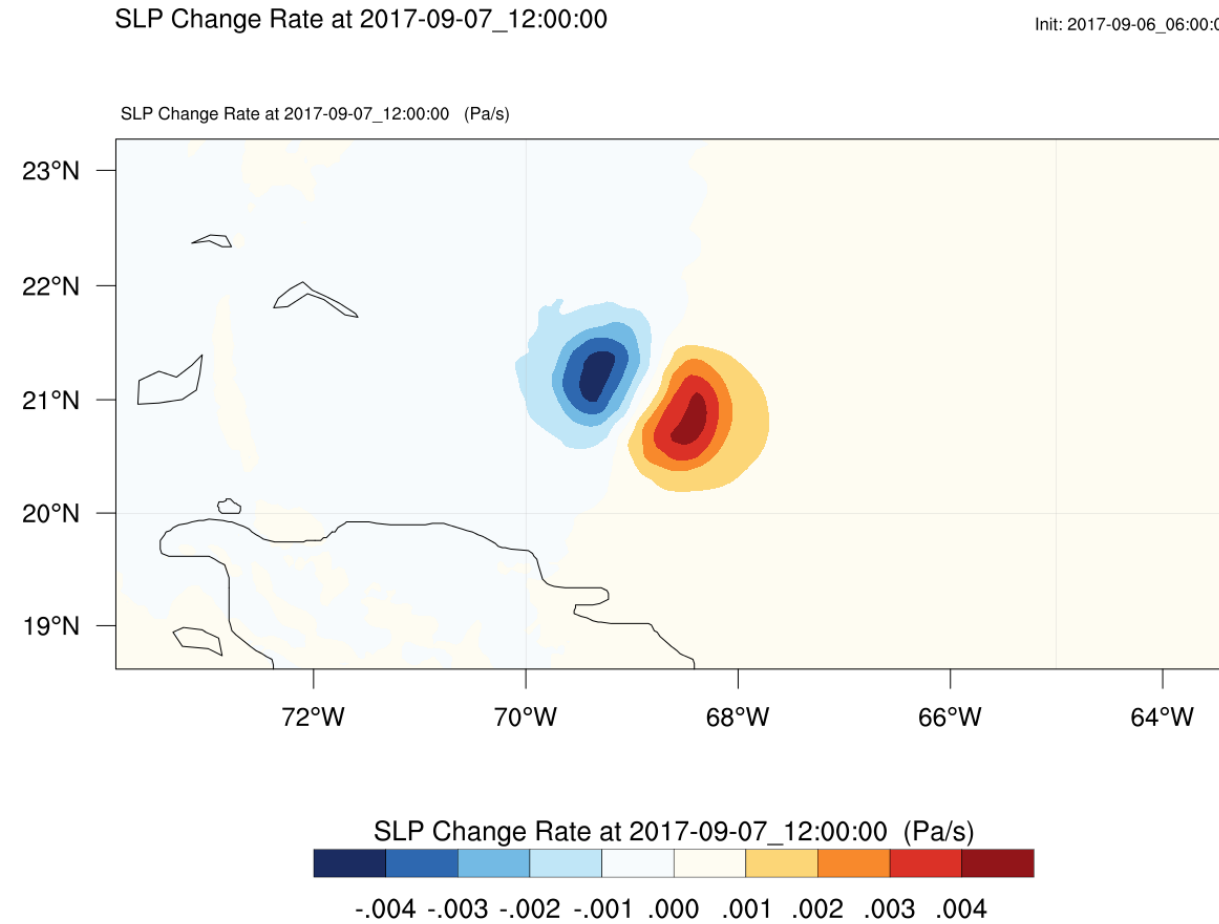
Mass Change Rate

Vertical Integrated Density Tendency at 2017-09-07_12:00:00

Init: 2017-09-06_06:00:00



Sea Level Pressure Change Rate



OUTPUT FROM WRF V3.9.1.1 MODEL
WE = 3100 ; SN = 1600 ; Levels = 46 ; Dis = 5.4km ; Phys Opt = 4 ; PBL Opt = 1 ; Cu Opt = 6

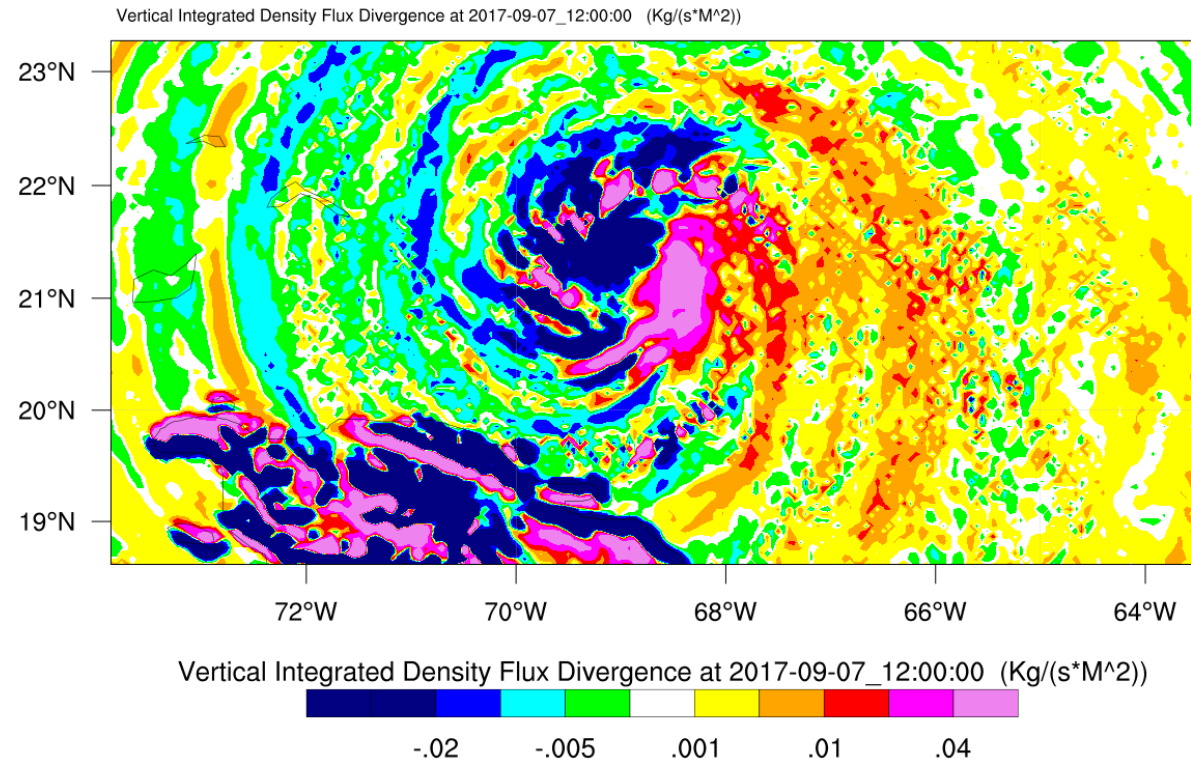
Compare Hourly SLP Change and Integrated Mass Change

- As surface pressure is caused by the air in the vertical column, so the vertical integrated air mass should have exactly the same pattern as surface pressure (or Sea Level Pressure, if over sea).
- From continuity Equation, we expect that the vertical integrated mass flux, as the right hand side of Eq. 2 should have the similar pattern as hourly vertical mass change, right?

Vertical Integrated Mass Flux Divergence

Vertical Integrated Density Flux Divergence at 2017-09-07_12:00:00

Init: 2017-09-06_06:00:00

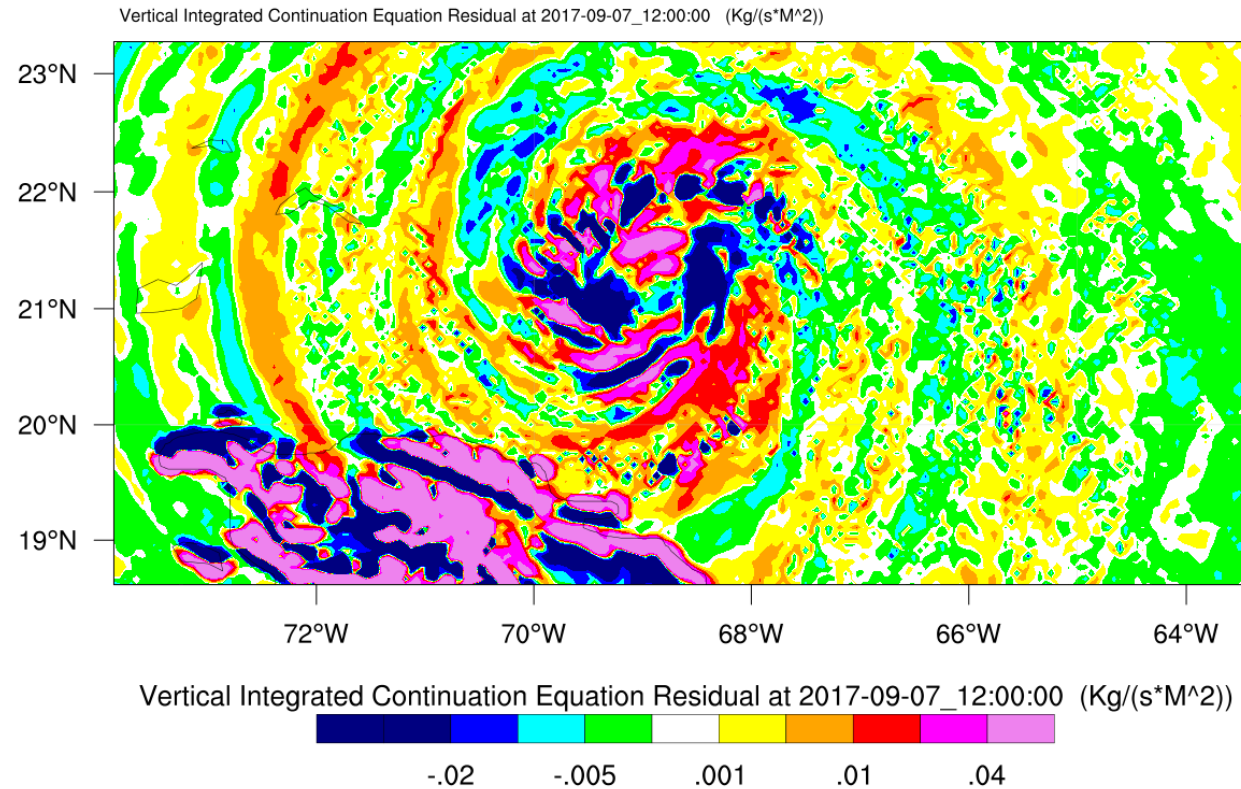


OUTPUT FROM WRF V3.9.1.1 MODEL
WE = 3100 ; SN = 1600 ; Levels = 46 ; Dis = 5.4km ; Phys Opt = 4 ; PBL Opt = 1 ; Cu Opt = 6

Vertical integrated (Density tendency – density flux divergence)

Vertical Integrated Continuation Equation Residual at 2017-09-07_12:00:00

Init: 2017-09-06_06:00:00



OUTPUT FROM WRF V3.9.1.1 MODEL
WE = 3100 ; SN = 1600 ; Levels = 46 ; Dis = 5.4km ; Phys Opt = 4 ; PBL Opt = 1 ; Cu Opt = 6

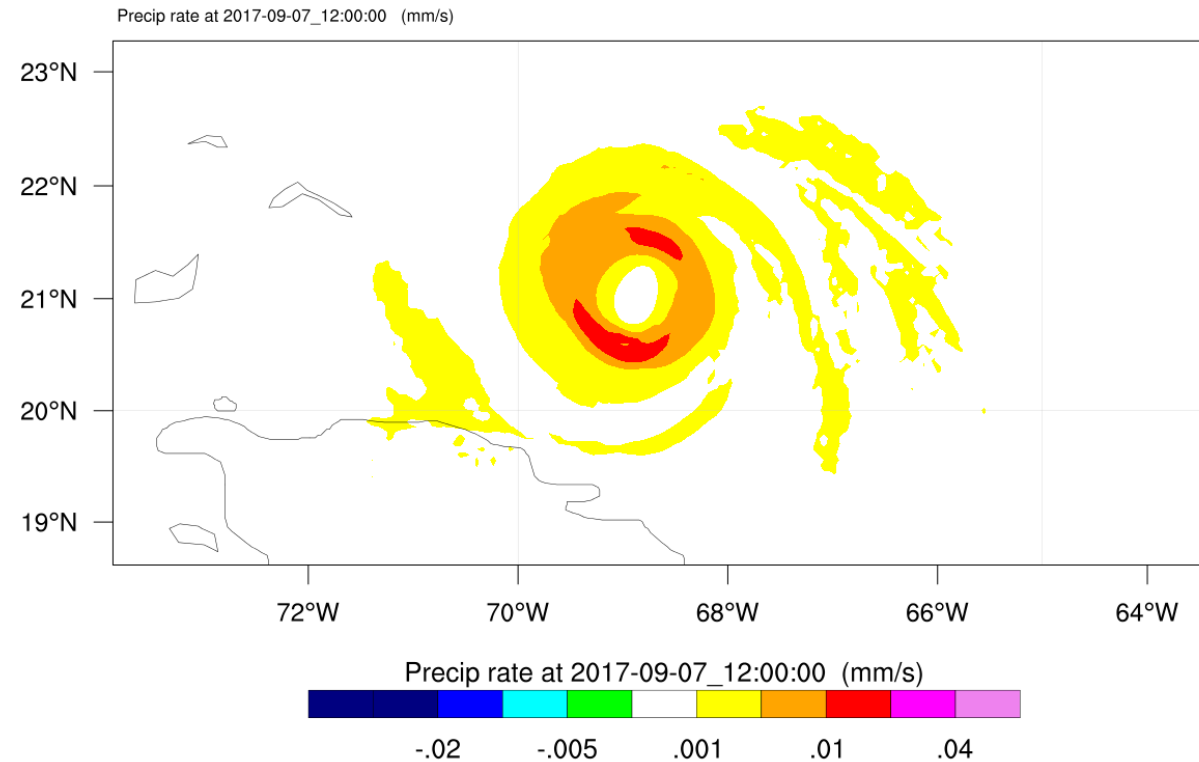
Compare Mass Change and Mass Flux

- In the hurricane region, the vertical integrated mass (hourly) change has totally different pattern to the vertical integrated Mass Flux.
- What the vertical integrated mass flux similar to?

Total Precipitation Rate

Precip rate at 2017-09-07_12:00:00

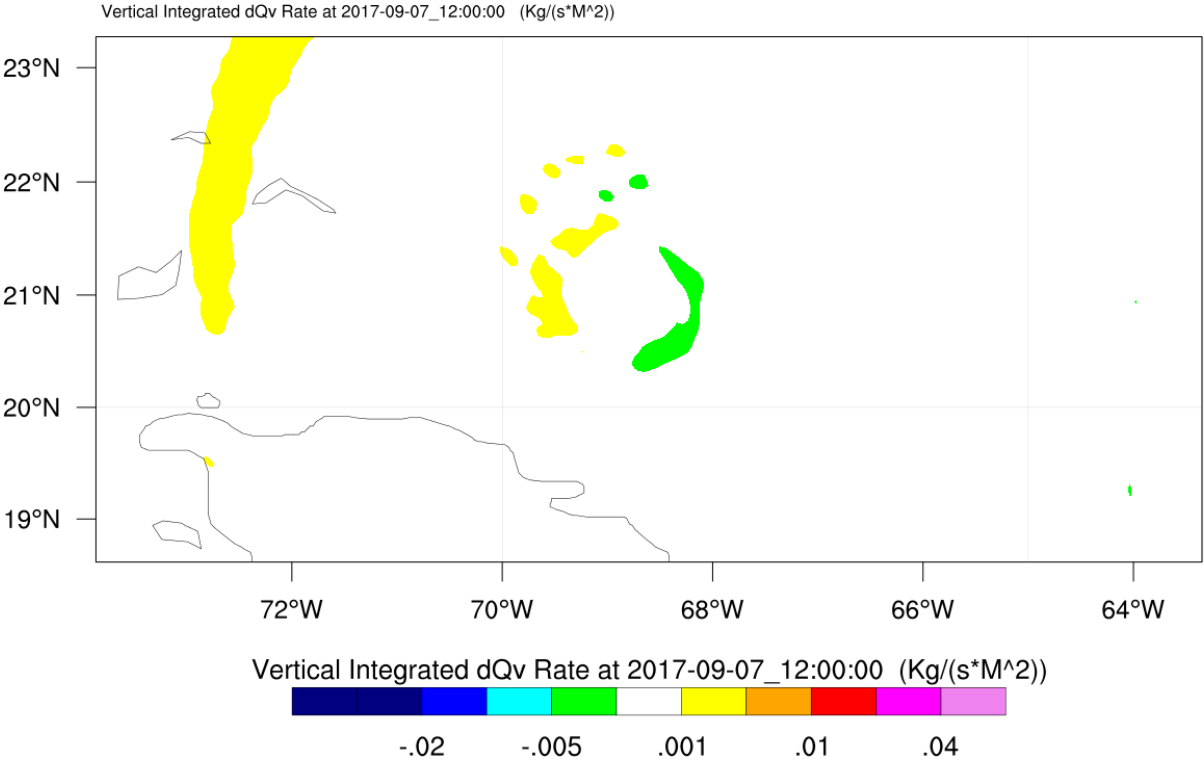
Init: 2017-09-06_06:00:00



OUTPUT FROM WRF V3.9.1.1 MODEL
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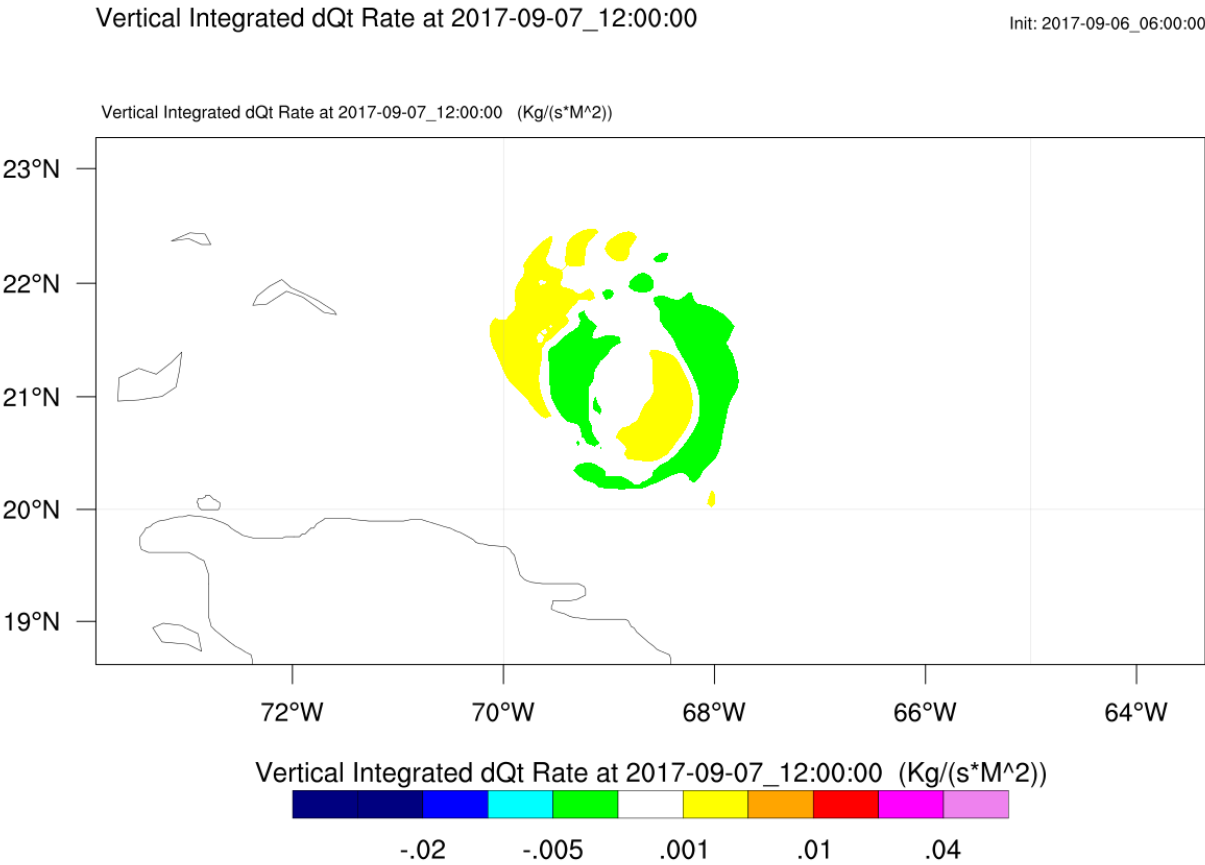
Water Vapor

Vertical Integrated dQv Rate at 2017-09-07_12:00:00 Init: 2017-09-06_06:00:00



OUTPUT FROM WRF V3.9.1.1 MODEL
WE = 3100 ; SN = 1600 ; Levels = 46 ; Dis = 5.4km ; Phys Opt = 4 ; PBL Opt = 1 ; Cu Opt = 6

Vertical Integrated Water Components Change Rate



OUTPUT FROM WRF V3.9.1.1 MODEL
WE = 3100 ; SN = 1600 ; Levels = 46 ; Dis = 5.4km ; Phys Opt = 4 ; PBL Opt = 1 ; Cu Opt = 6

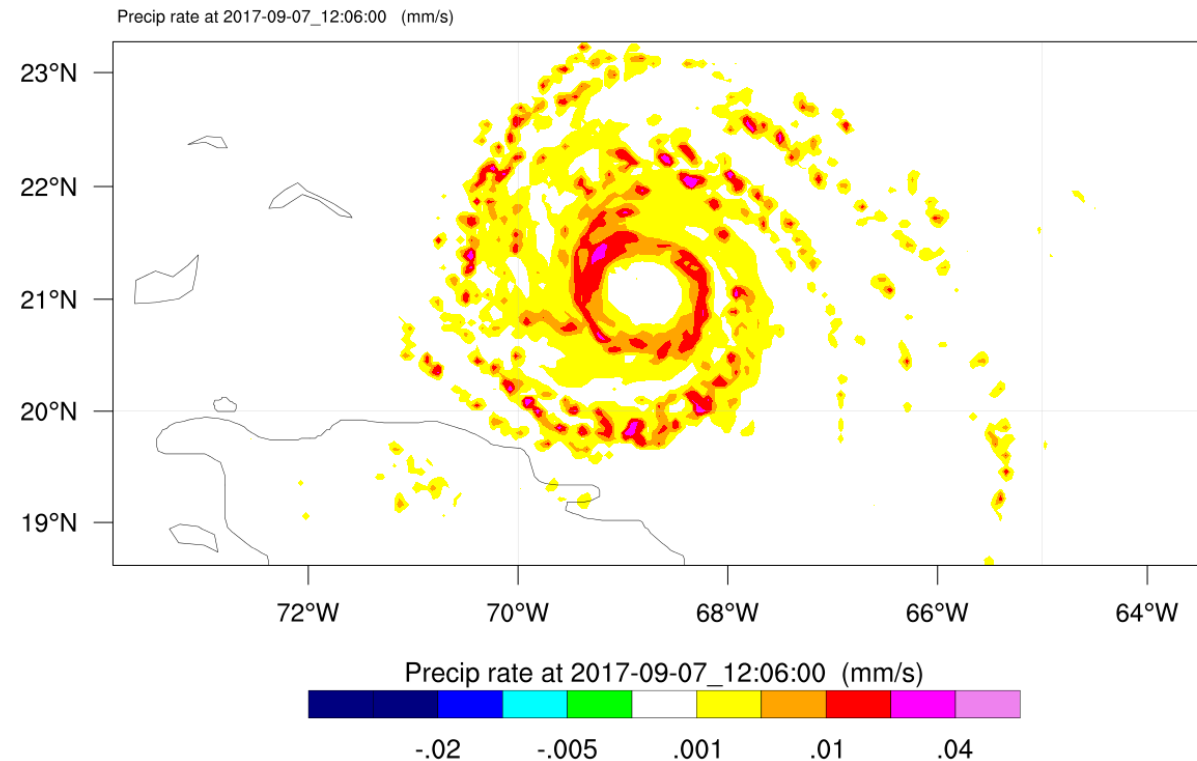
Compare Density Flux Divergence with Precipitation, and Water Vapor, etc

- Density Flux Divergence has lots of small scale features
- Precipitation is two hours, which has not much small scale features.

Total Precipitation Rate

Precip rate at 2017-09-07_12:06:00

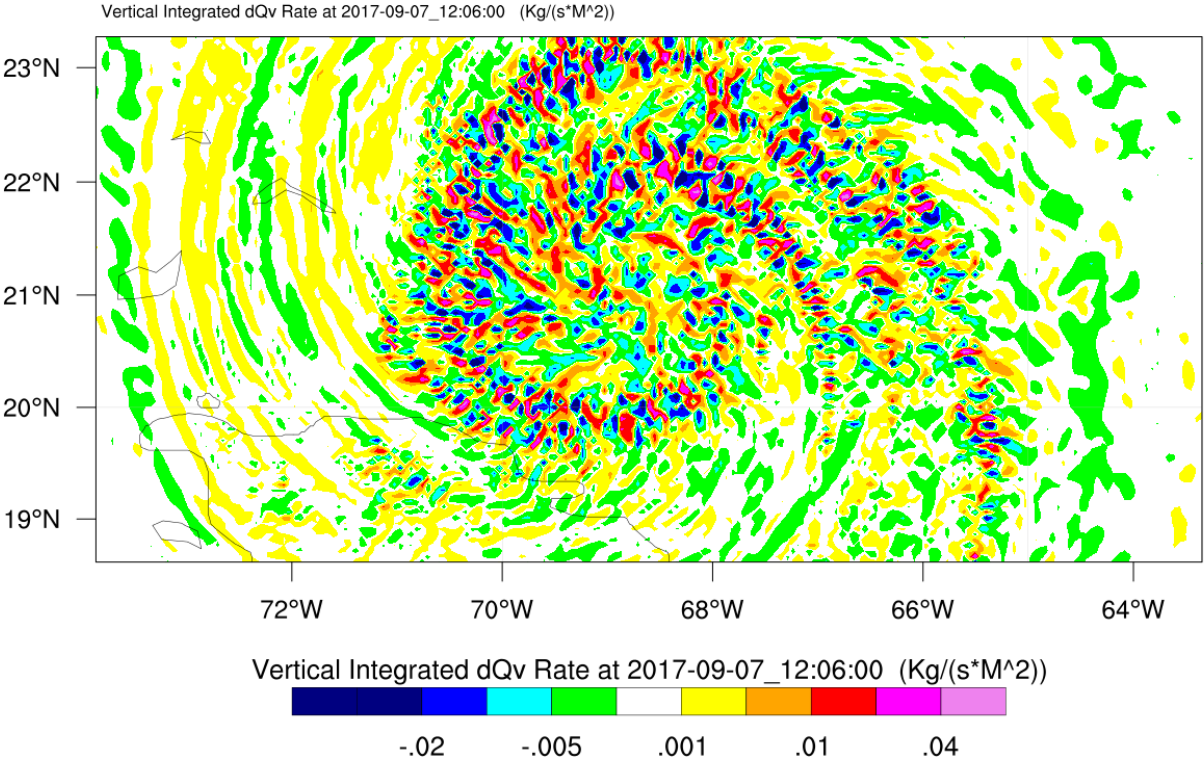
Init: 2017-09-07_12:00:00



OUTPUT FROM WRF V3.9.1.1 MODEL
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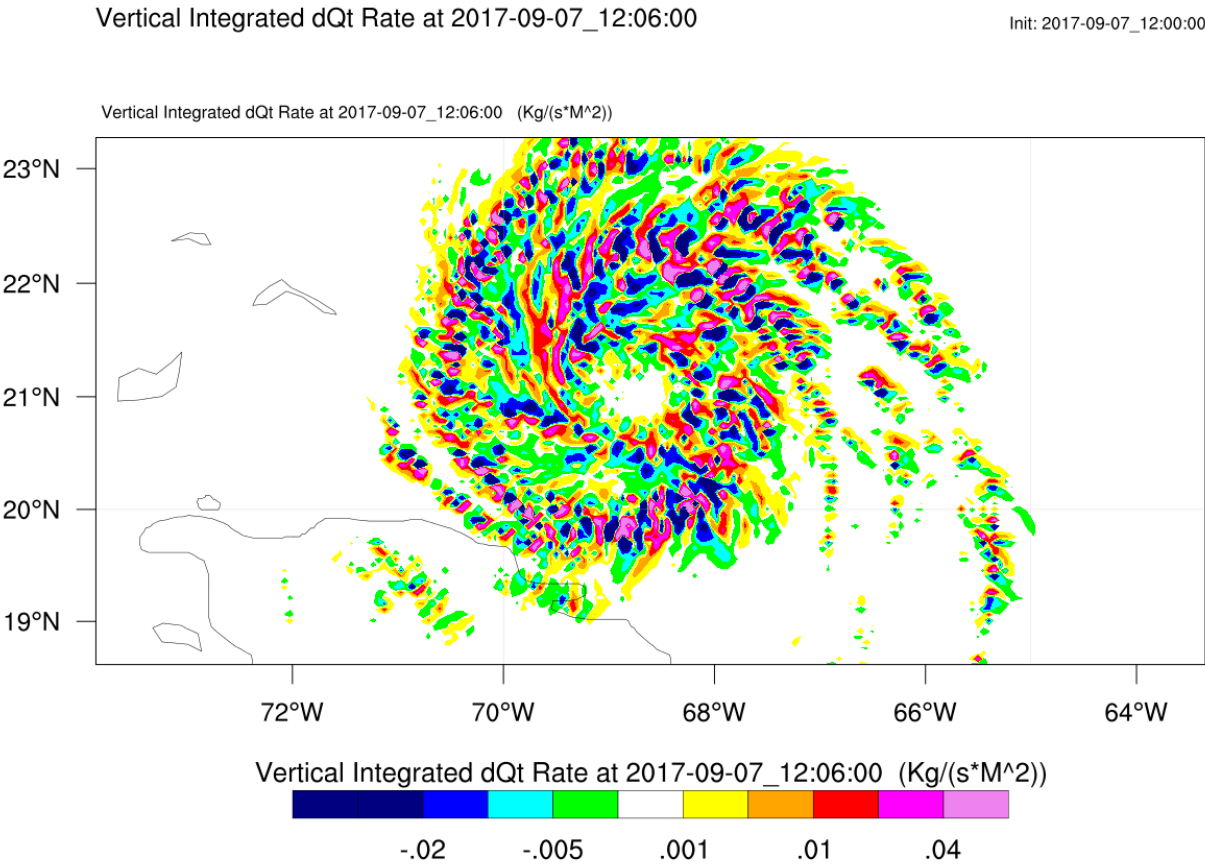
Water Vapor

Vertical Integrated dQv Rate at 2017-09-07_12:06:00 Init: 2017-09-07_12:00:00



OUTPUT FROM WRF V3.9.1.1 MODEL
WE = 3100 ; SN = 1600 ; Levels = 46 ; Dis = 5.4km ; Phys Opt = 4 ; PBL Opt = 1 ; Cu Opt = 6

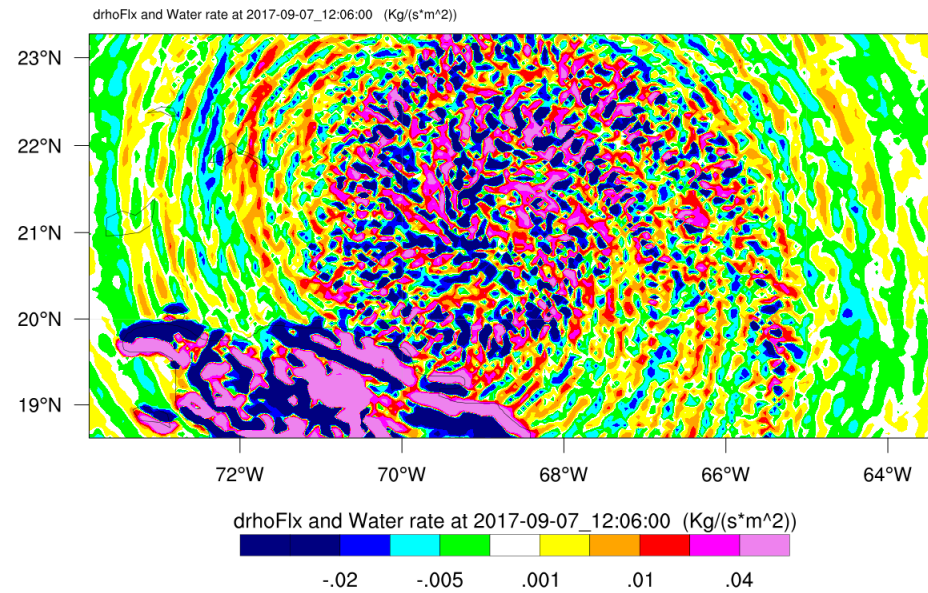
Vertical Integrated Water Components Change Rate



OUTPUT FROM WRF V3.9.1.1 MODEL
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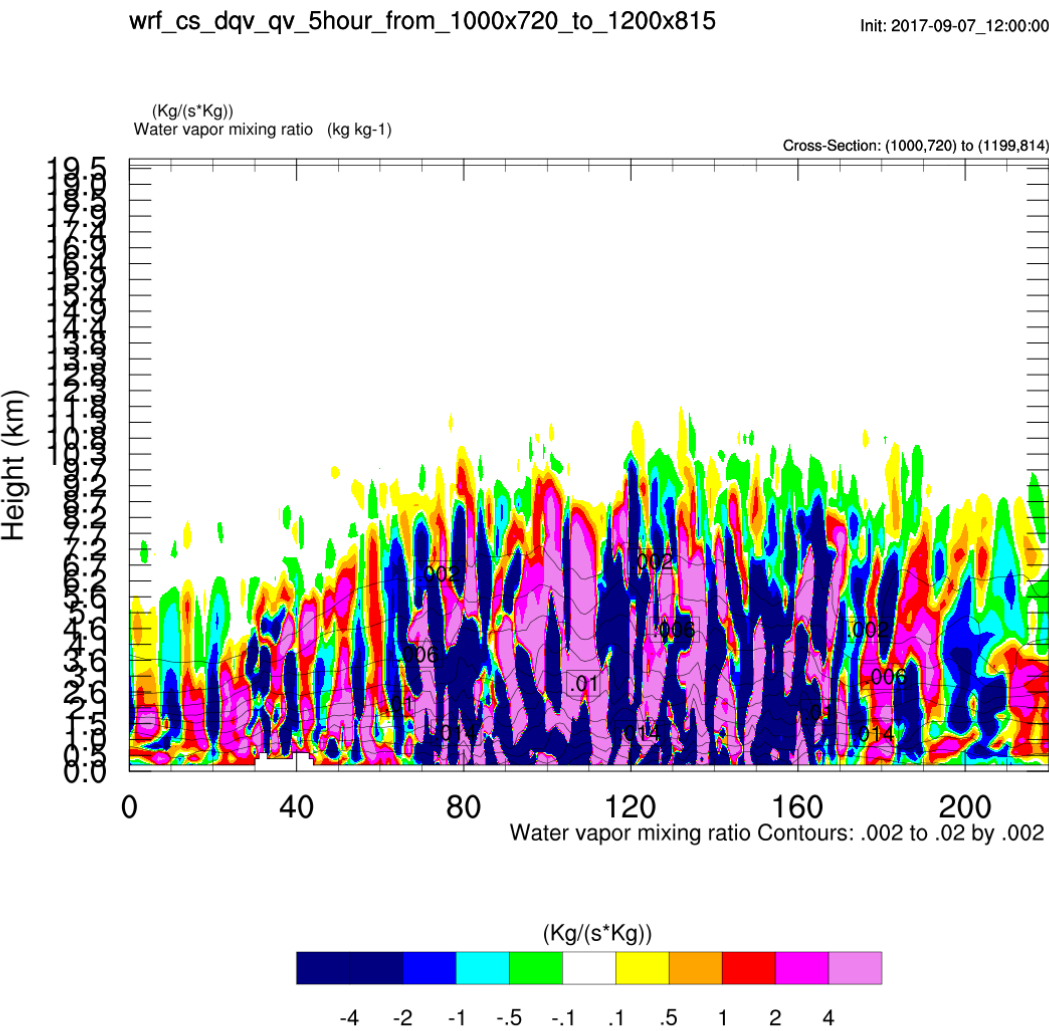
drhoFlx and Water rate at 2017-09-07_12:06:00

Init: 2017-09-07_12:00:00



OUTPUT FROM WRF V3.9.1.1 MODEL
WE = 3100 ; SN = 1600 ; Levels = 46 ; Dis = 5.4km ; Phys Opt = 4 ; PBL Opt = 1 ; Cu Opt = 6

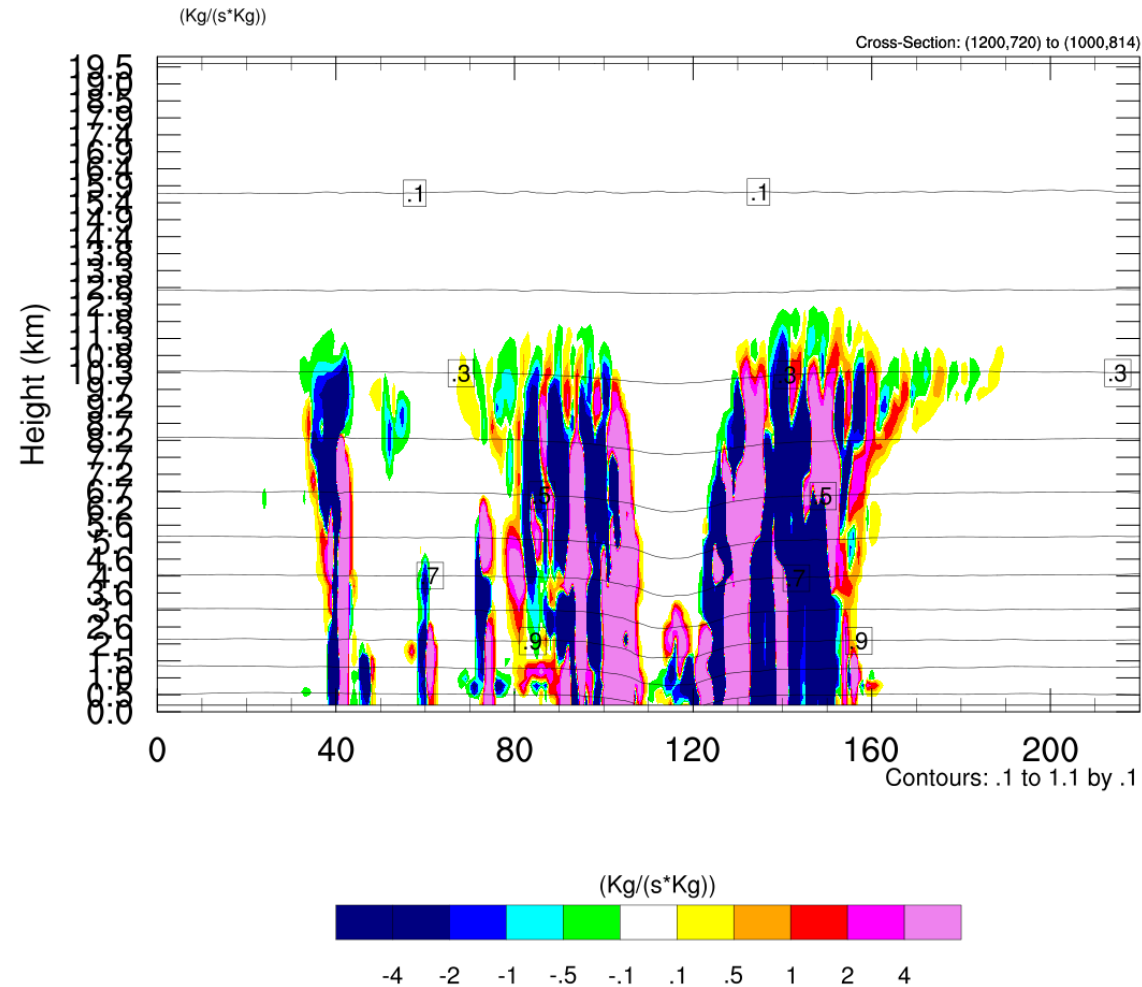
Water Vapor Change Rate



Total of Qc, Qr, Qi, and Qs Change Rate

wrf_cs_dqt_rho_5hour_from_1200x720_to_1000x815

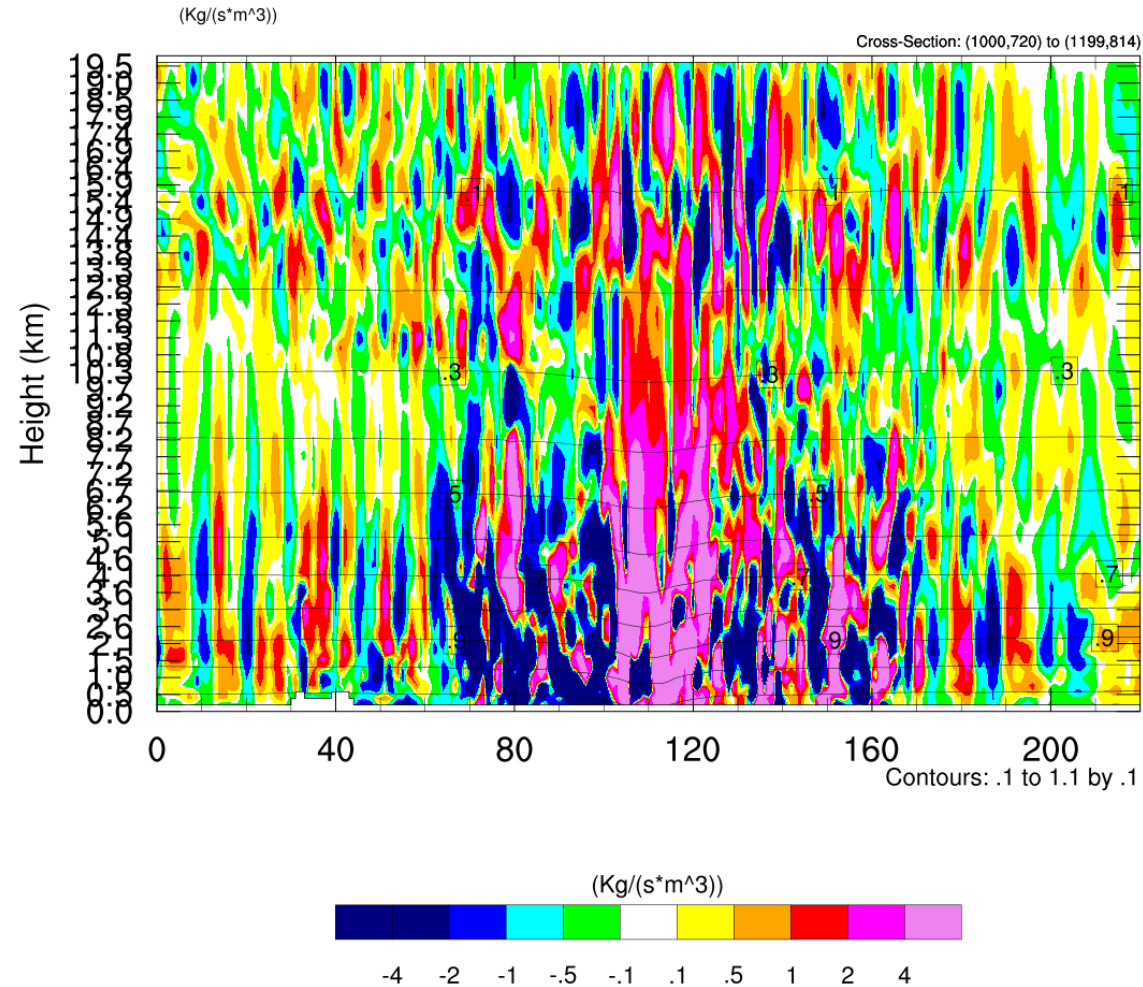
Init: 2017-09-07_12:00:00



Density Change Rate

wrf_cs_drho_rho_5hour_from_1000x720_to_1200x815

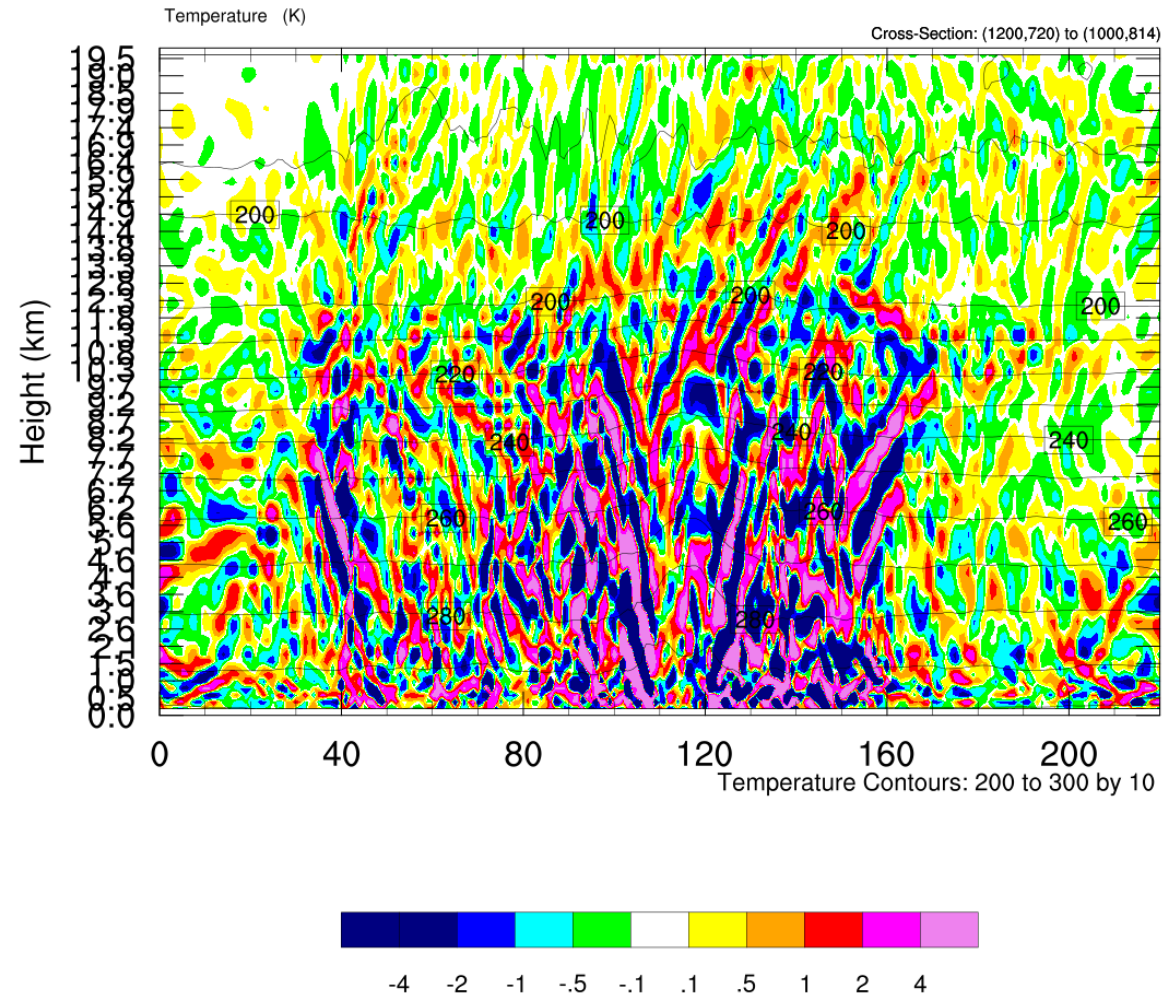
Init: 2017-09-07_12:00:00



Density Flux Divergence

wrf_cs_flx_tk_5hour_from_1200x720_to_1000x815

Init: 2017-09-07_12:00:00



The Vertical integrated Mass Flux

- More similar to water vapor, or cloud water, or rain water pattern.
- Why?

Mass Change in the Atmosphere

- When the air flow into the hurricane, it contains moisture/water vapor.
- Precipitation (more strictly, condensation) make atmosphere lose moisture, therefor the air lose mass.
- The positive vertical integrated mass flux did not change into air mass, but became precipitation, drop out of the atmosphere.

The Magnitude of Integrated Mass Flux and Precipitation

- From integrated mass flux figure, the positive flux is $0.01 \text{ Kg}/(\text{m}^2 \cdot \text{s})$.
- The precipitation $\sim 40 \text{ mm}$.
- If the mass flux all convert to precipitation, the depth of the water is:
 - $0.01 * 3600 \text{ (Kg/m}^2\text{)}$, which is $\sim 36 \text{ mm}$.

New Continuity Equation

–So we should change continuity equation 1 to:

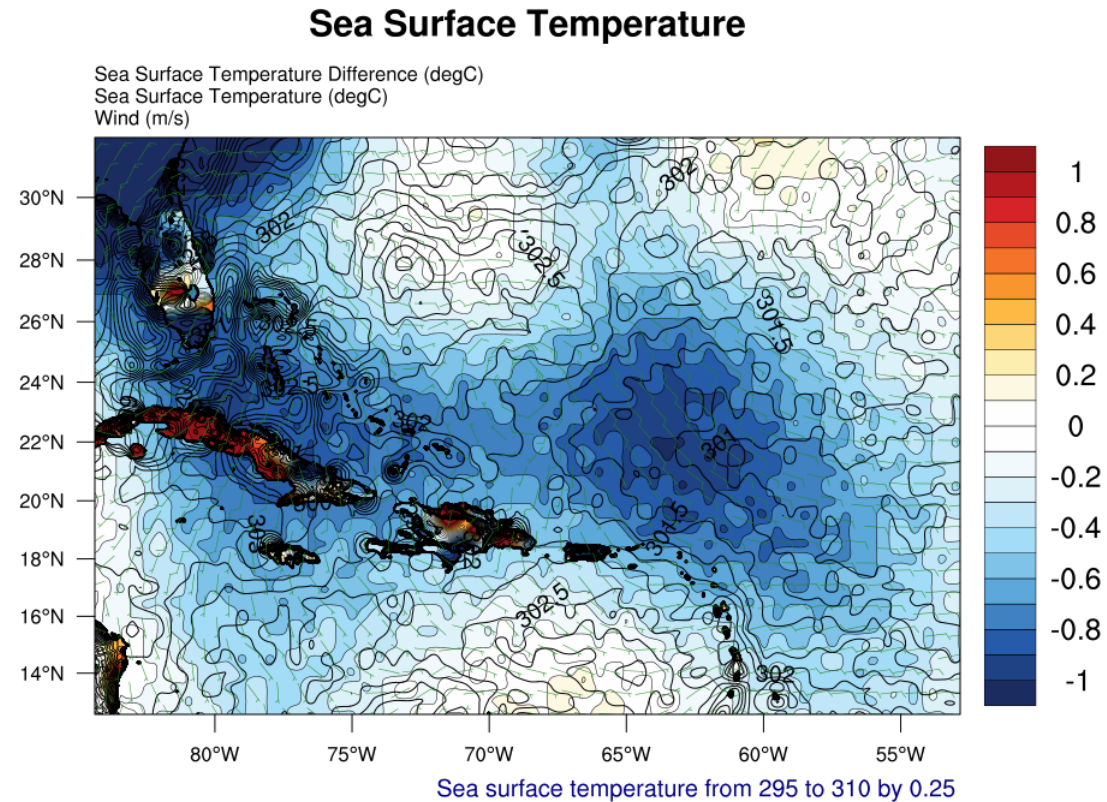
$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \vec{V}) = s \quad (3)$$

- Where “s” represents the combined air mass source and/or sink:
- For $s < 0$, which means air mass loss, or more precipitation than evaporation
 - For $s > 0$, which means are mass gain, or more evaporation than precipitation

Cold Sea Surface Temperature after Hurricane

- The passage of a tropical cyclone over the ocean causes the upper layers of the ocean to cool substantially, which can influence subsequent cyclone development.
- This cooling is primarily caused by wind-driven mixing of cold water from deeper in the ocean with the warm surface waters.
- https://en.wikipedia.org/wiki/Tropical_cyclone

Cold SST after Hurricane Irma (2017.09.08.18 – 2017.09.06.06)



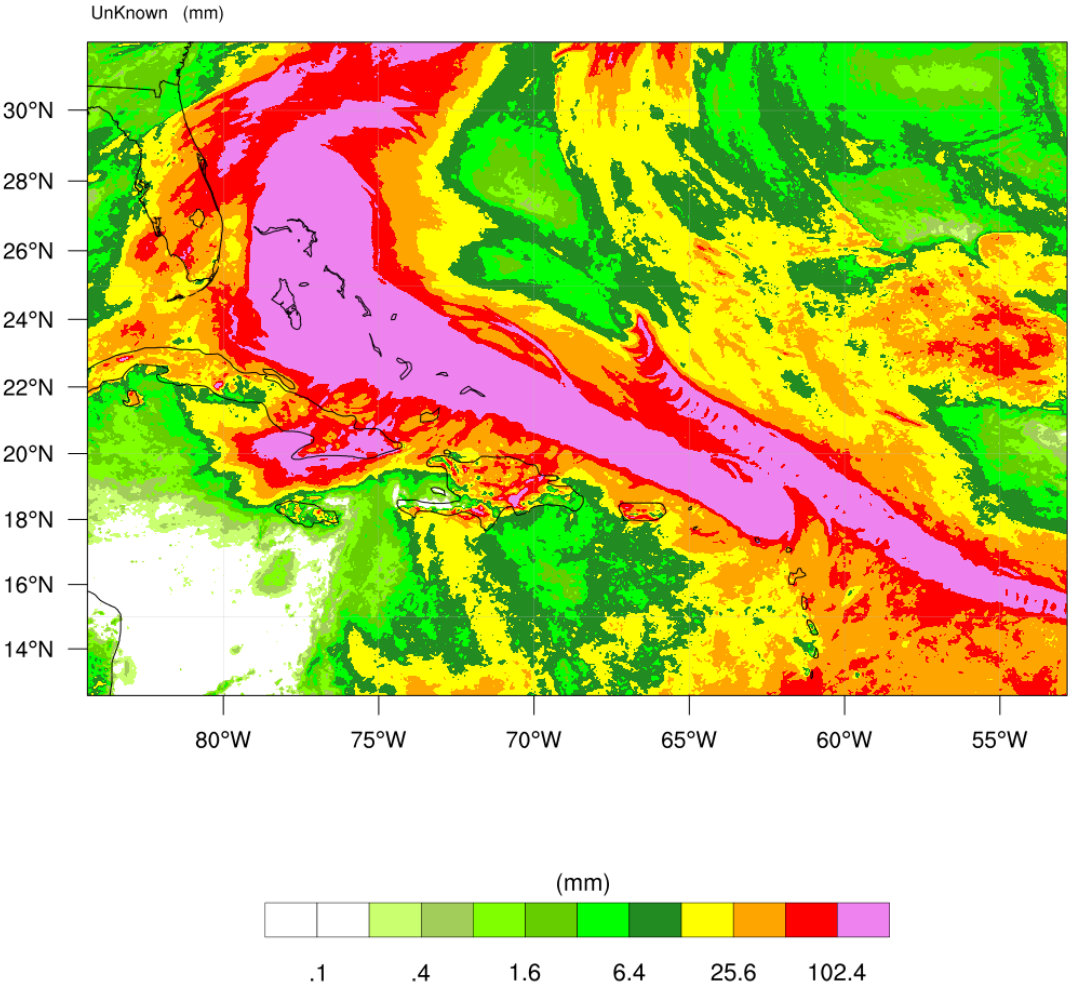
Questions

- If the cold SST after hurricane is caused by ocean mixing, then there should a warm pool in the ocean right under the cold pool, right?
- Have we observed any of those warm pools?
- Where did it go?
- We'd like to propose a different thought.

5 Days Accumulated Precipitation

Total Precipitaion at 2017-09-11_06:00:00

Init: 2017-09-06_06:00:00



Discussion

- 5 Days precipitation has a wide band of great than 100 mm, with maximum great than 1000 mm.
- We'd rather believe that the cool pool after hurricane is mostly contributed from precipitation, as:
 - Ignore the density difference between precipitation and sea water.
 - Assume ocean temperature 26 degree, and rain water temperature 22 degree
 - Then 100 mm precipitation, when mixing well, can:
 - Cool down sea surface temperature by 2 degrees up to 20 cm
 - Cool down SST by 1 degrees to 40 cm

Conclusions

- The continuity Equation should be modified with an additional term s :
 - Where $s > 0$, for evaporation, as it increases the atmospheric air mass.
 - And $s < 0$, for precipitation, as it reduces the air mass.
- The cold SST after hurricane is from the cold rain water.



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Thank You

Reference

- <https://ams.confex.com/ams/32Hurr/webprogram/Paper292465.html>
- <https://ams.confex.com/ams/32Hurr/webprogram/Paper292791.html>