

# **A new scale-aware 3DTKE scheme**

- **We have developed a scale-aware parameterization scheme based on the general form of the TKE equation in the WRF model to simulate 3D subgrid turbulent mixing;**
- **The scheme holds the promise of making the transition between the mesoscale and LES limits smooth, not only in the amount of subgrid mixing, but also in the parameterization formula.**

# Starting point of our development in WRF

$$\overline{u'_i u'_j} = -K_{ij}^M \left( \frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial \bar{u}_j}{\partial x_i} \right) + \overline{u'_i u'_j}^{NL} \quad (i \neq j)$$

$$\overline{u'_i \theta'} = -K_{ij}^H \frac{\partial \bar{\theta}}{\partial x_j} + \delta_{i3} \overline{u'_i \theta'}^{NL}$$

$$K^M = C e^{1/2} l$$

$$\frac{\partial e}{\partial t} = \bar{u}_j \frac{\partial e}{\partial x_j} - \overline{u'_i u'_j} \frac{\partial \bar{u}_i}{\partial x_j} + \frac{g}{\theta_0} \overline{w' \theta'} - \frac{\overline{\partial u'_i (e + p' / \rho_0)}}{\partial x_i} - \varepsilon$$

Minimal requirements for extending the 3D TKE LES subgrid model to the mesoscale limit include the three key elements:

- The nonlocal fluxes;
- The mixing length scales;
- Horizontal diffusion parameterization.

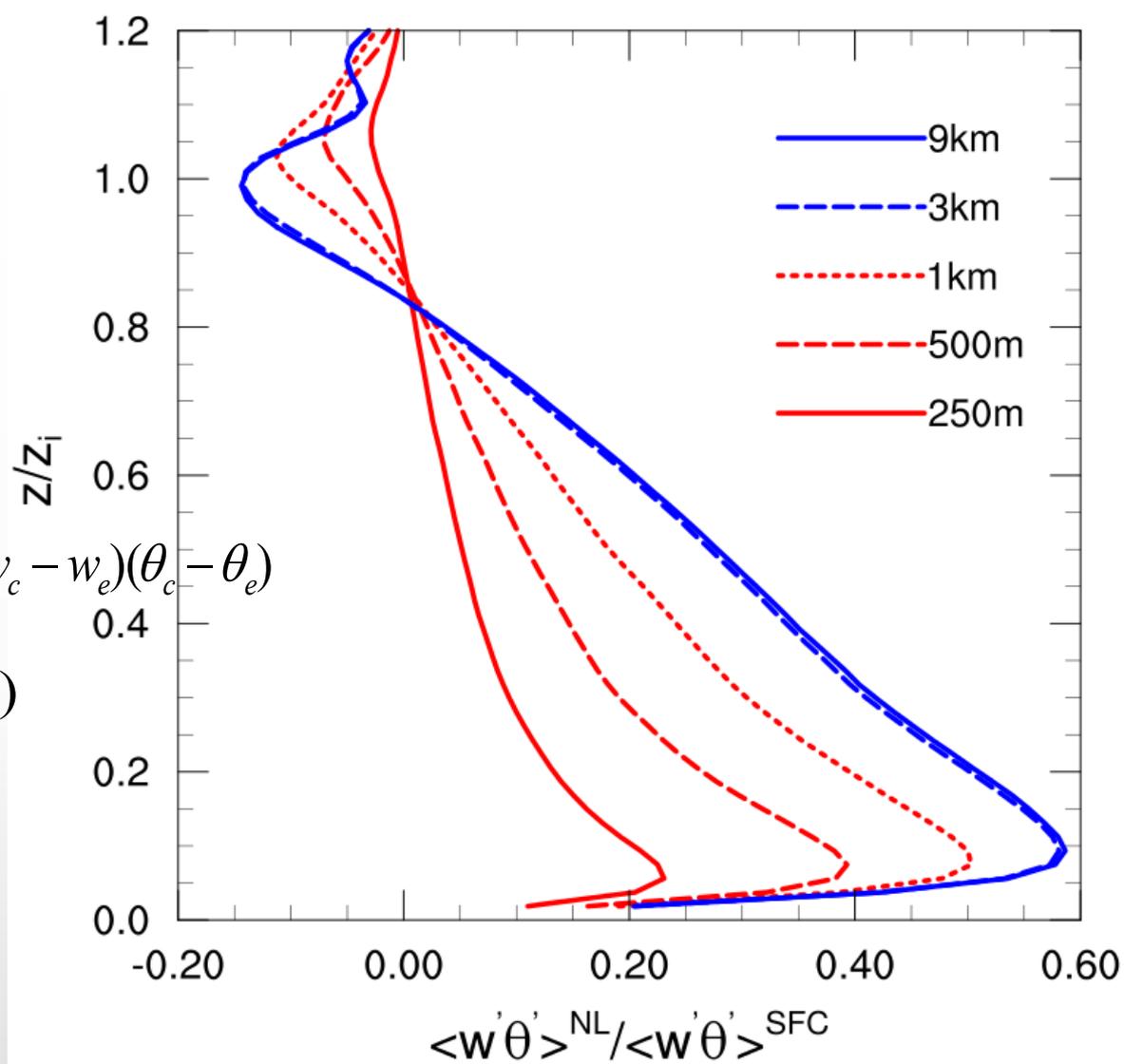
# Nonlocal heat flux

Conditional sampling  
based on LES data

$$\overline{w'\theta'} = a\overline{w'\theta'^c} + (1-a)\overline{w'\theta'^e} + a(1-a)(w_c - w_e)(\theta_c - \theta_e)$$

$$\overline{w'\theta'}^{NL} = a(1-a)(w_c - w_e)(\theta_c - \theta_e)$$

In mesoscale limit, the nonlocal heat flux gradually converges to a single profile (compare the profiles at resolutions 3km and 9km)



Vertical profile of SGS nonlocal heat flux for different resolutions normalized by surface heat flux.

# Mixing length scale

In the LES limit, Deardorff's length scale is applied:

$$l_{LES} = \begin{cases} \min \left[ 0.76e^{1/2} \left| \frac{g}{\theta} \frac{\partial \theta}{\partial z} \right|^{-1/2}, \Delta s \right] & \text{for } N^2 > 0 \\ \Delta s & \text{for } N^2 \leq 0 \end{cases}$$

$$\Delta s = (\Delta x \Delta y \Delta z)^{1/3}$$

In the mesoscale limit, following MYNN Level-3 scheme, the vertical length scale is given as:

$$\frac{1}{l_{MESO}} = \frac{1}{l_S} + \frac{1}{l_T} + \frac{1}{l_B}$$

$l_S$  is the length scale in the surface layer controlled by the effects of wall and stability,  $l_T$  the length scale depending on the turbulent structure of the PBL and  $l_B$  the length scale limited by the thermal stability.

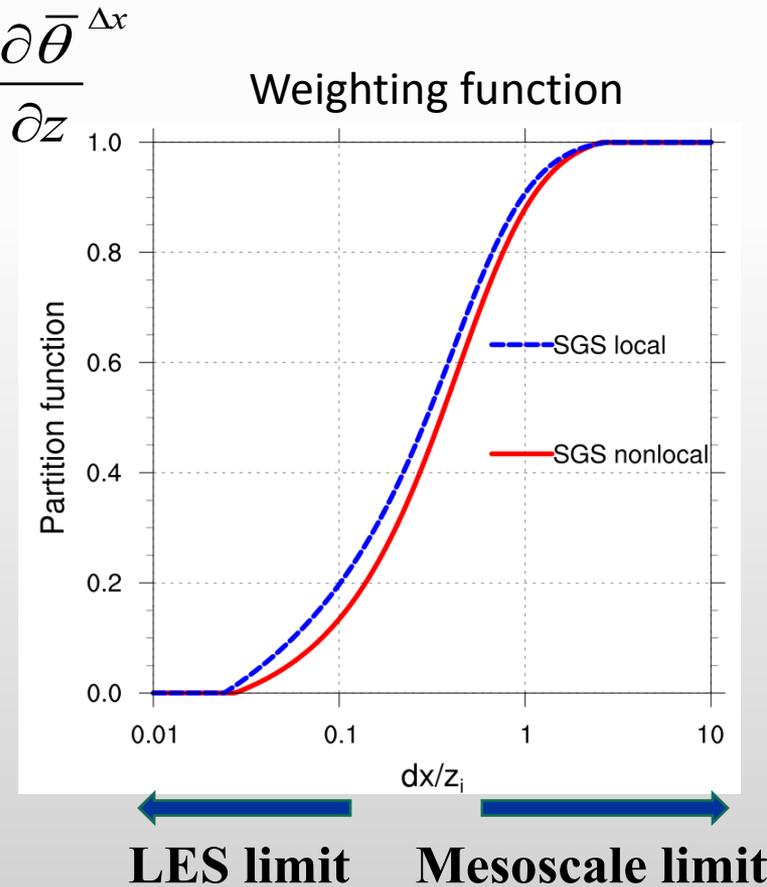
# Scale-aware transition between LES and mesoscale limit

$$\overline{w'\theta'}^{\Delta x} = -K_{\Delta x}^H \frac{\partial \bar{\theta}}{\partial z} + \overline{w'\theta'}^{\Delta x, NL} = \overline{w'\theta'}^{\Delta x, L} + \overline{w'\theta'}^{\Delta x, NL}$$

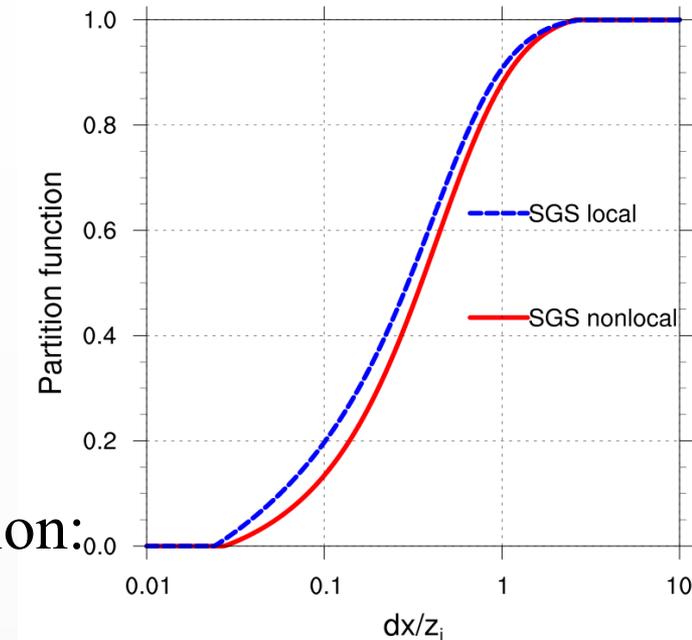
$$\overline{w'\theta'}^{\Delta x, NL} = \overline{w'\theta'}^{NL} P_{NL}(\Delta x/z_i) \quad \overline{w'\theta'}^{\Delta x, L} = -K_{\Delta x}^H \frac{\partial \bar{\theta}}{\partial z}$$

$$K_{\Delta x}^H = C_{vertical} l_{\Delta x} e^{1/2}$$

$$l_{\Delta x} = P_L(\Delta x/z_i) l_{MESO} + [1 - P_L(\Delta x/z_i)] l_{LES}$$



# Horizontal diffusion



The scale-aware transition of horizontal diffusion:

$$\begin{aligned} K_h &= K_D + K_T \\ &= P_L(\Delta x/z_i) (C_s \Delta)^2 D / \sqrt{2} + [1 - P_L(\Delta x/z_i)] C_k l e^{1/2} \end{aligned}$$

$K_D$  is the diffusivity based on the deformation (2D Smag).

$K_T$  is the diffusivity based on the 1.5-order TKE.

# Improvements on numerics

- We have found that the new scale-aware 3DTKE scheme can be unstable when it is used in mesoscale simulations in which  $dx, dy \gg dz$  (highly anisotropic grid).
- To make the model stable, I have used the implicit method instead of original explicit method to solve the TKE equation and model diffusion equations.

$$\frac{\partial e}{\partial t} + \overline{U_j} \frac{\partial e}{\partial x_j} = -(\overline{u'_i u'_j}) \frac{\partial \overline{U_i}}{\partial x_j} + \delta_{i3} \frac{g}{\theta_v} \overline{u'_i \theta'_v} - \frac{1}{\rho} \frac{\partial (\overline{p' u'_i})}{\partial x_i} - \frac{\partial (\overline{u'_j e})}{\partial x_j} - \varepsilon$$

$$e_k^{n+1} - e_k^n = \Delta t (D_h - A_h + P)_k^n + \Delta t \left( D_v - A_v - \frac{c_e e^{1/2}}{l} e \right)_k^{n+1}$$

# A real case of fair weather

From: 2016.08.29.08

To: 2016.08.30.08

**D01:3km**

**D02:1km**

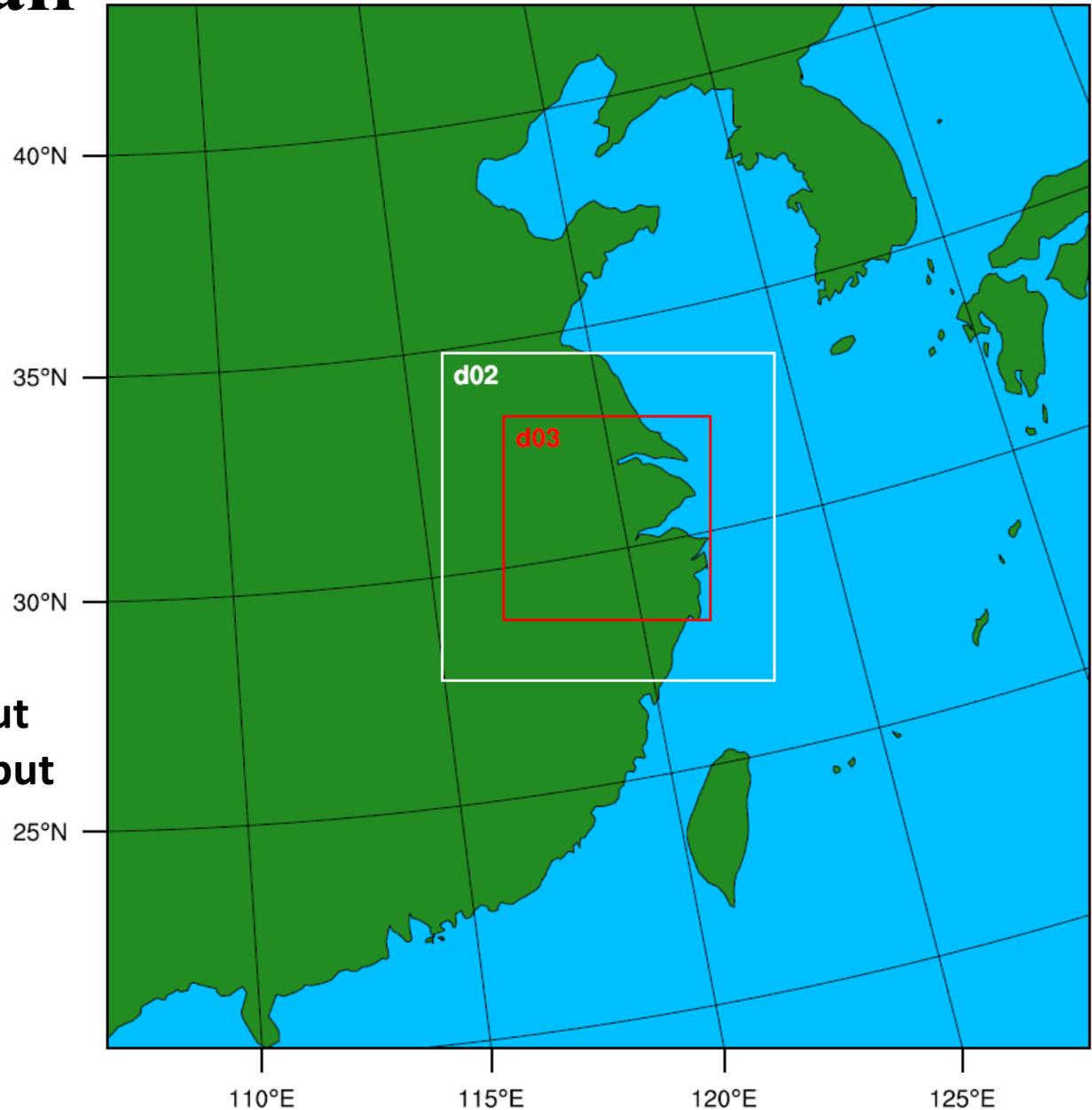
**D03:500m**

**3km: GFS analysis**

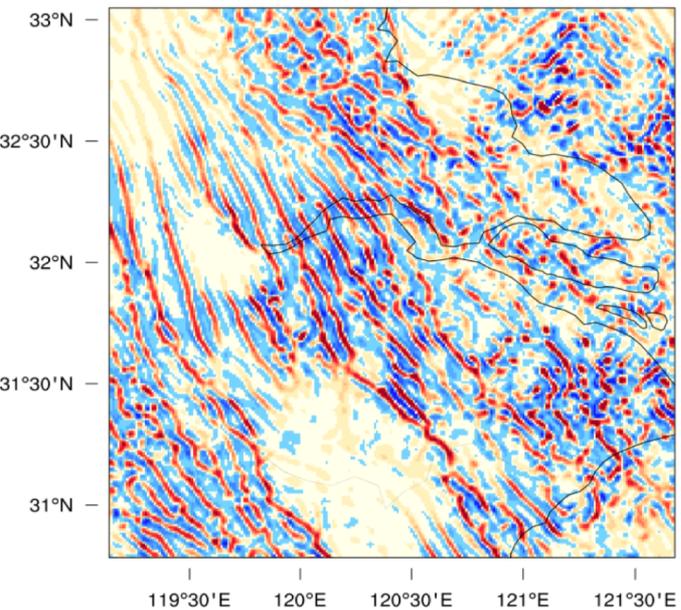
**1km: ndown from 3km output**

**500m: ndown from 1km output**

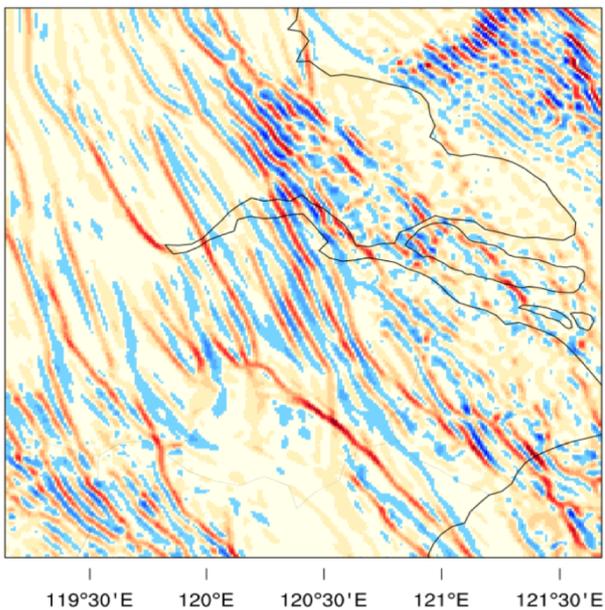
Res	$n_x * n_y$	dt
3km	793*853	15s
1km	805*805	5s
500m	1001*1001	2s



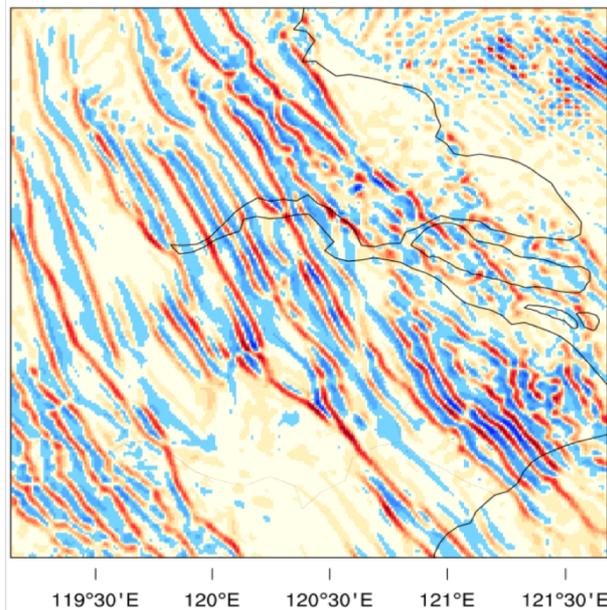
a) MYNN2.5 1km



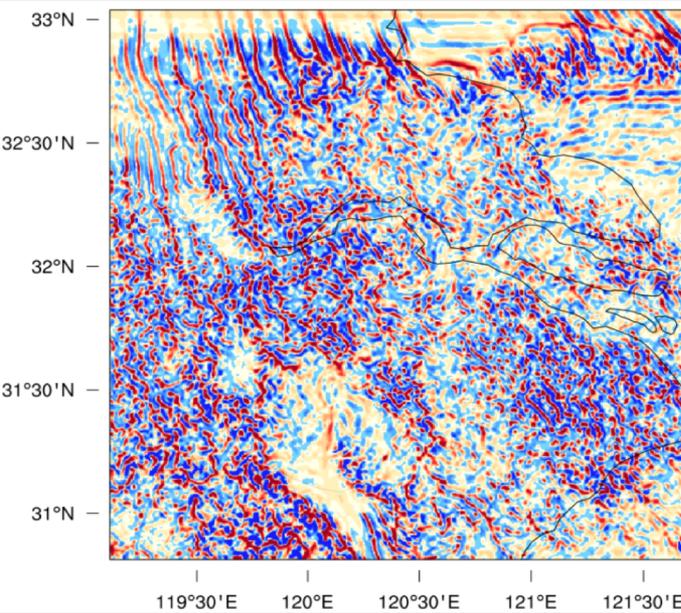
b) YSU 1km



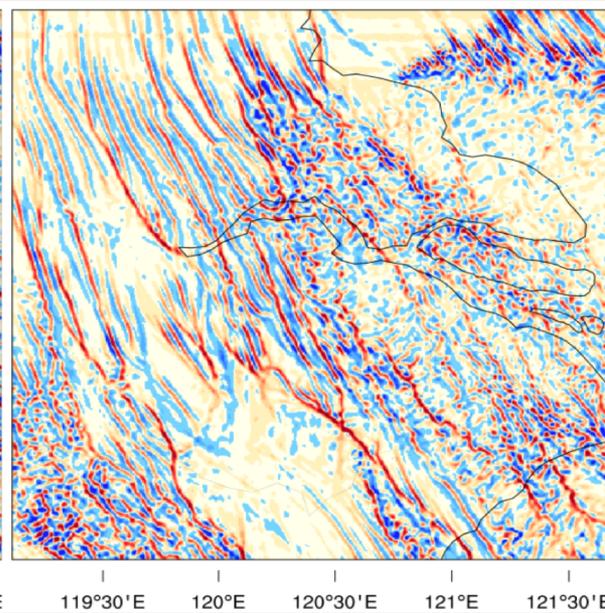
c) New 3dTKE 1km



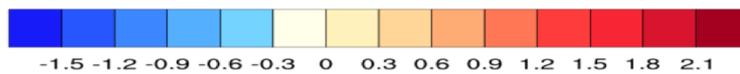
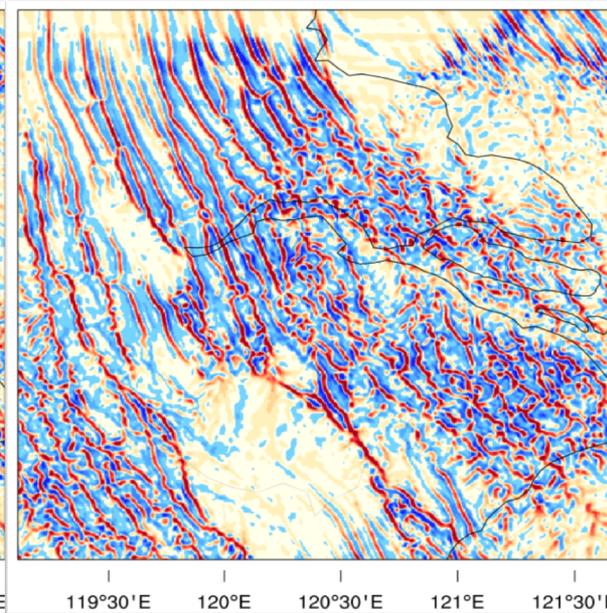
d) MYNN2.5 500m



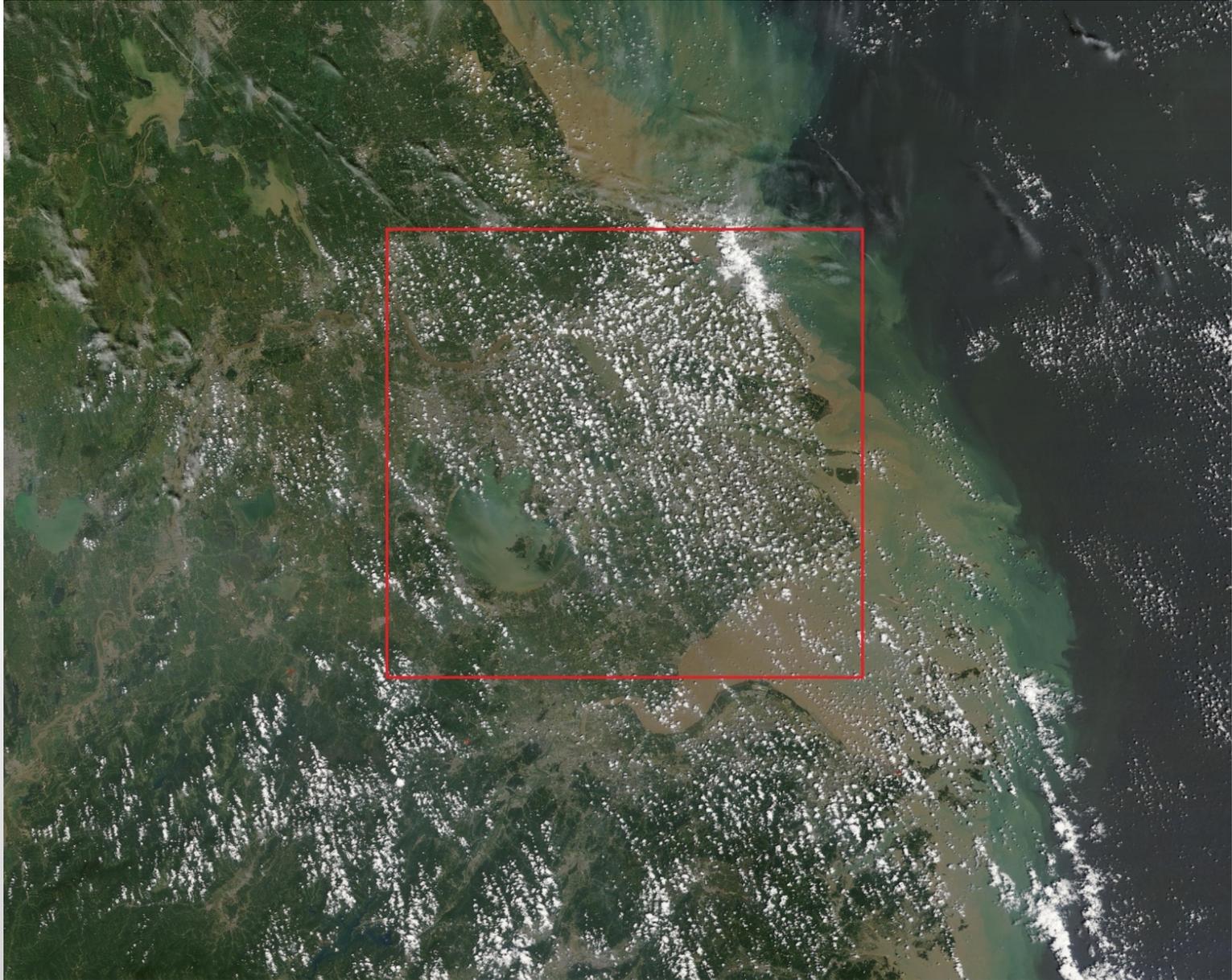
e) YSU 500m



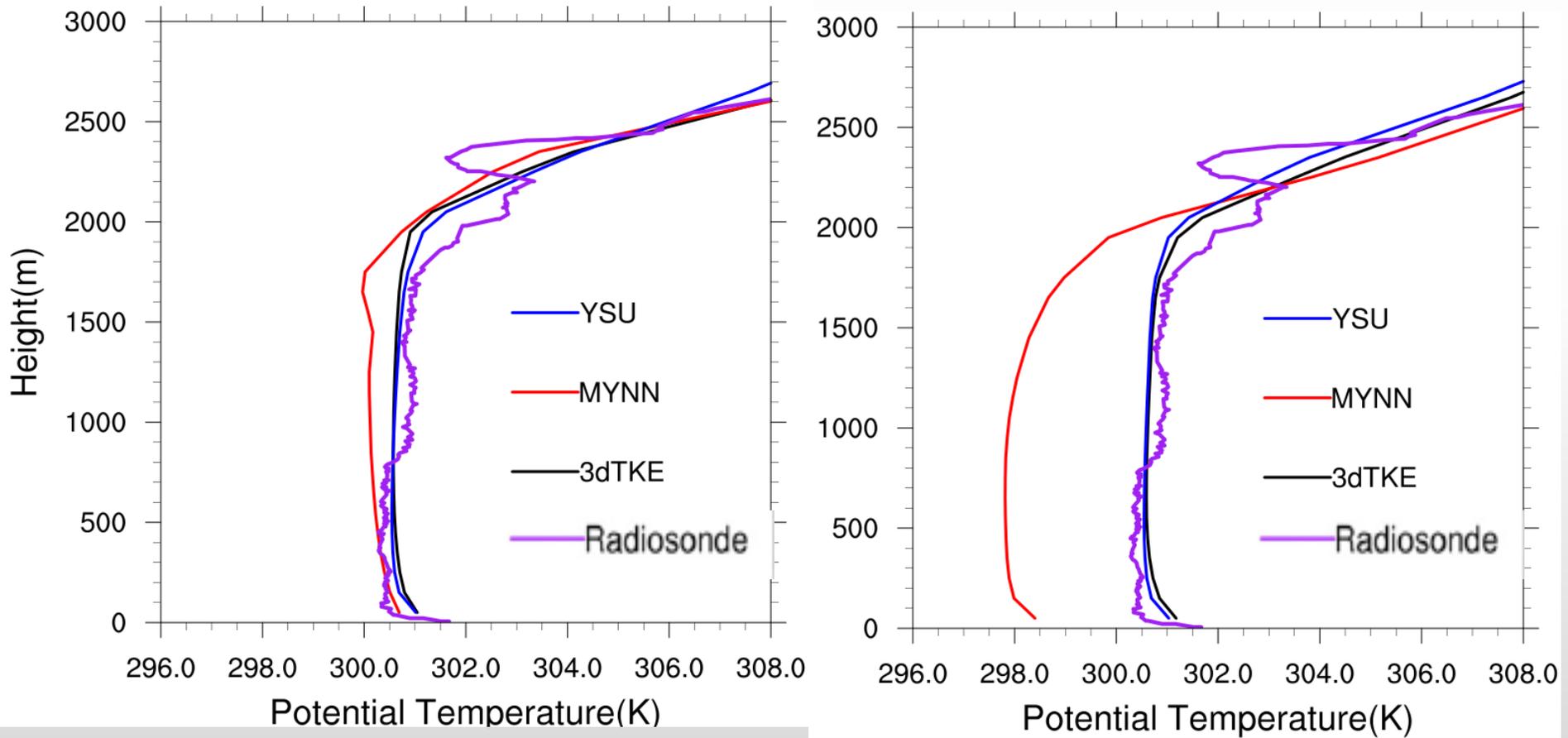
f) New 3dTKE 500m



**250-m resolution visible MODIS-*Terra* image at 02:40  
UTC 29 Aug 2016**



# Vertical profiles of simulated potential temperature at 0500 UTC 29 Aug 2016 for the Station Baoshan (31.40°N, 121.45 °E)

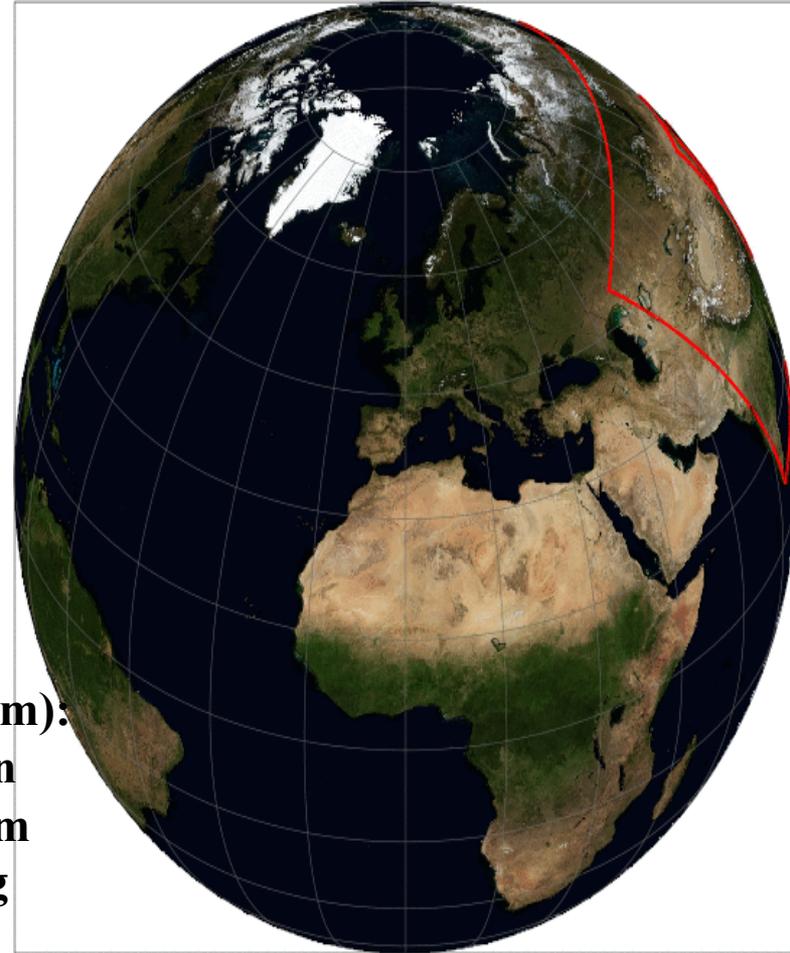
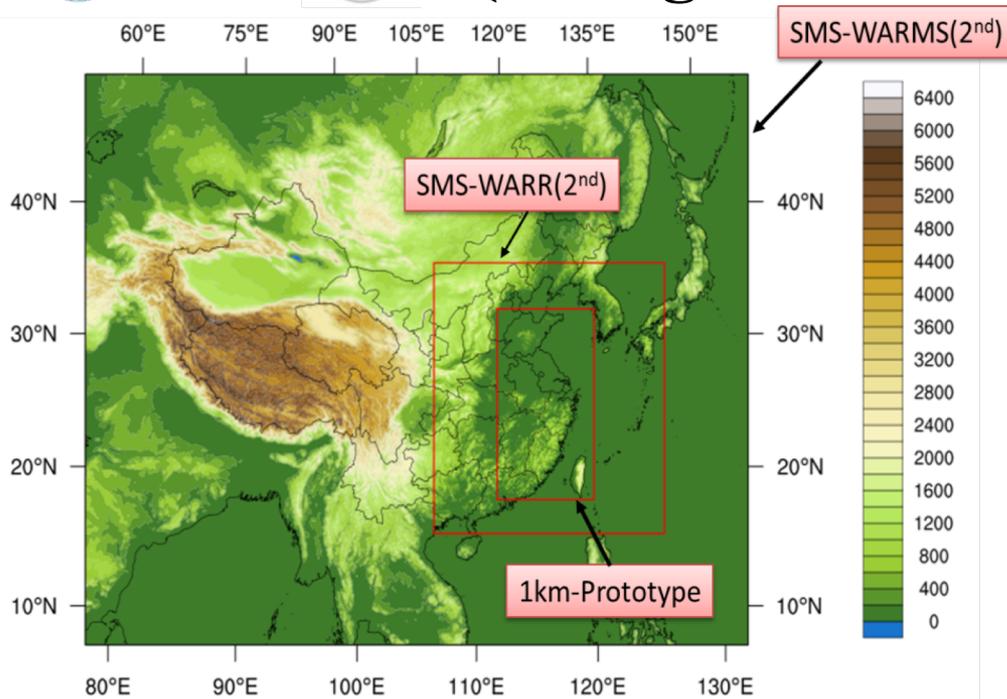


1km

500m



# Operational NWP system in SMS (Shanghai Meteorological Service)

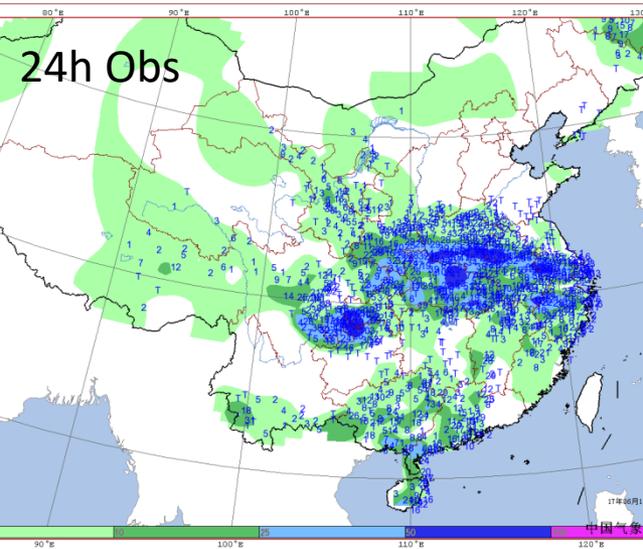


**SMS-WARMS (WRF-ADAS Realtime Modeling System):**

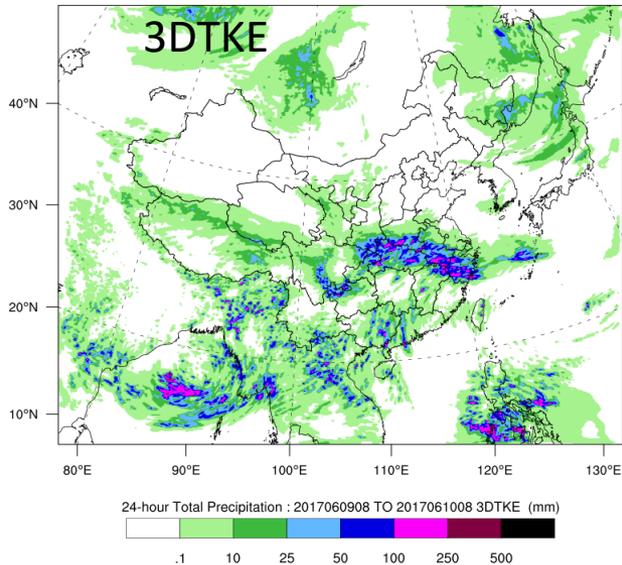
9km resolution, WRF3.5.1+ADAS 5.3.3, 72h prediction

**SMS-WARR(WRF-ADAS Rapid Refresh System):** 3km resolution, cooling starting at 02 am (local time), doing data assimilation every hour, and making 12-hour prediction, boundary condition from 9km system

**Precipitation event in Meiyu front  
on 9 June 2017**



24-hour Total Precipitation : 2017060908 TO 2017061008 3DTKE (mm)



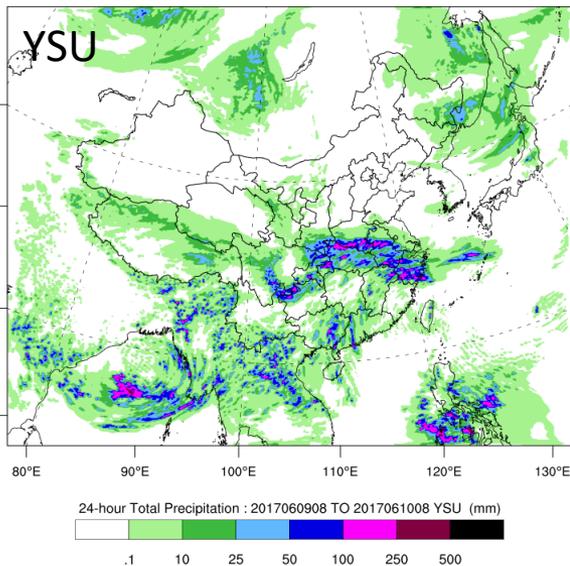
# 24h precipitation forecast in SMS-WARMS with 9-km resolution

SMS-WARMS (2nd) Prediction

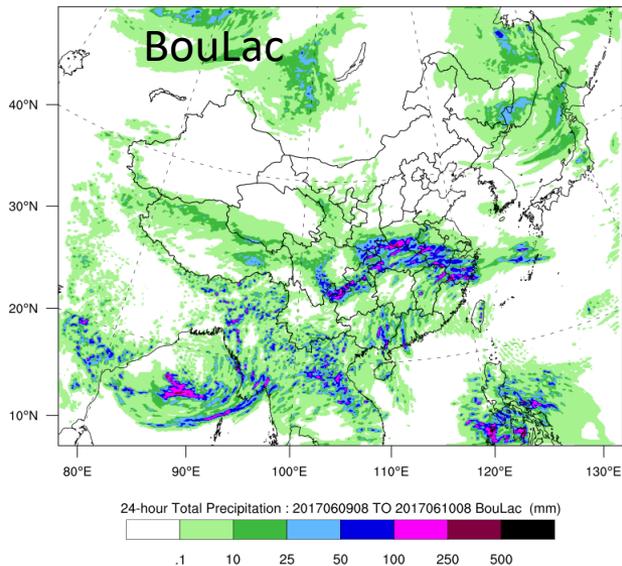
SMS-WARMS (2nd) Prediction

SMS-WARMS (2nd) Prediction

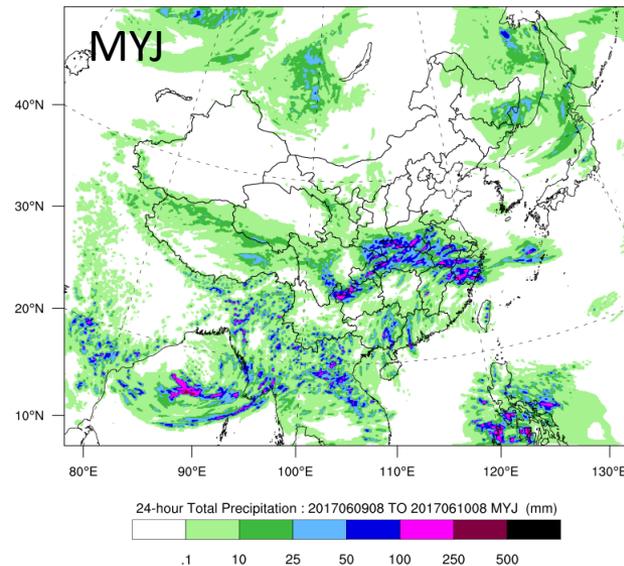
24-hour Total Precipitation : 2017060908 TO 2017061008 YSU (mm)

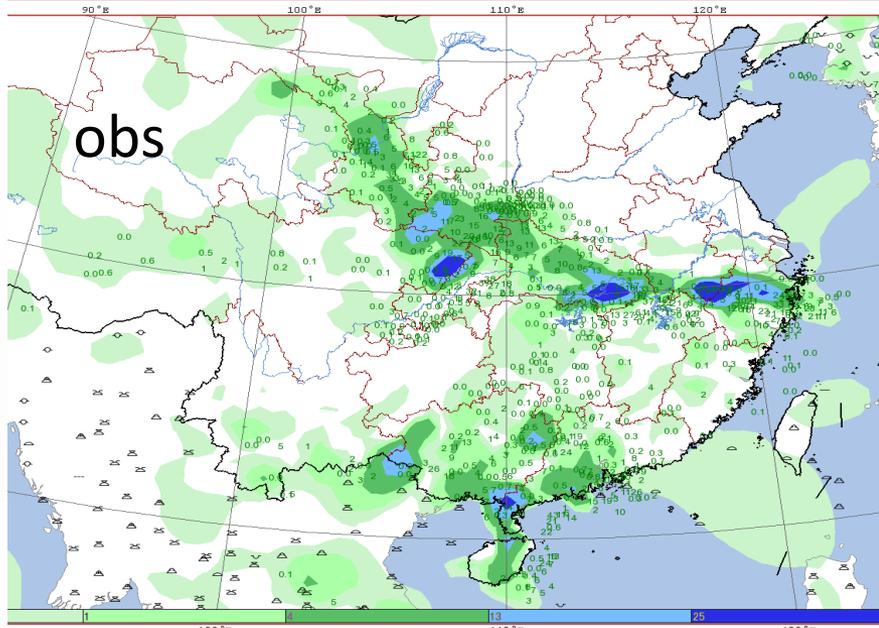


24-hour Total Precipitation : 2017060908 TO 2017061008 BouLac (mm)



24-hour Total Precipitation : 2017060908 TO 2017061008 MYJ (mm)





# 12h precipitation forecast in SMS-WARR with 3-km resolution

Prediction

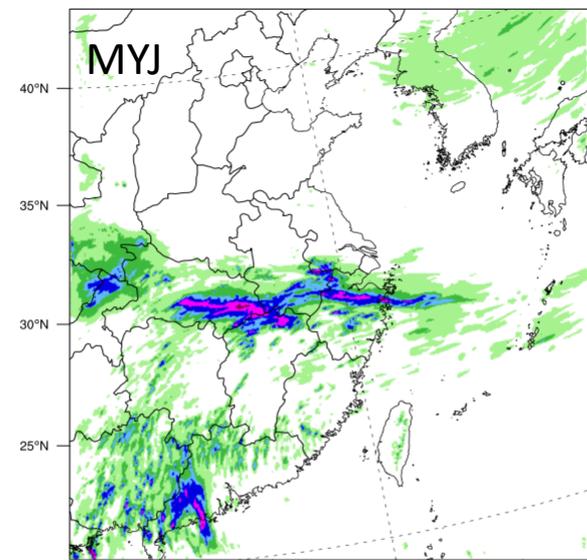
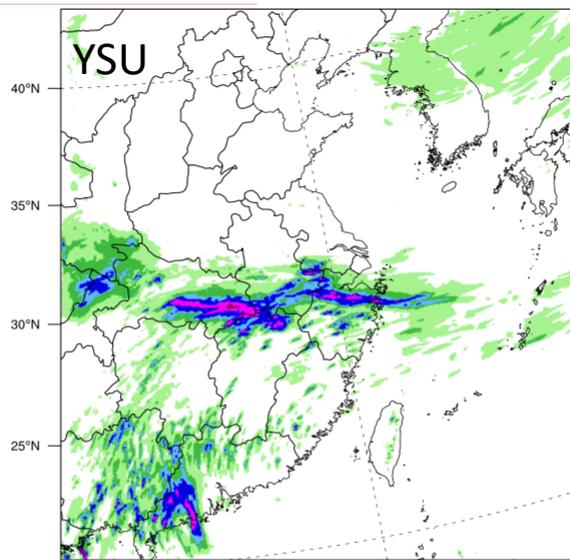
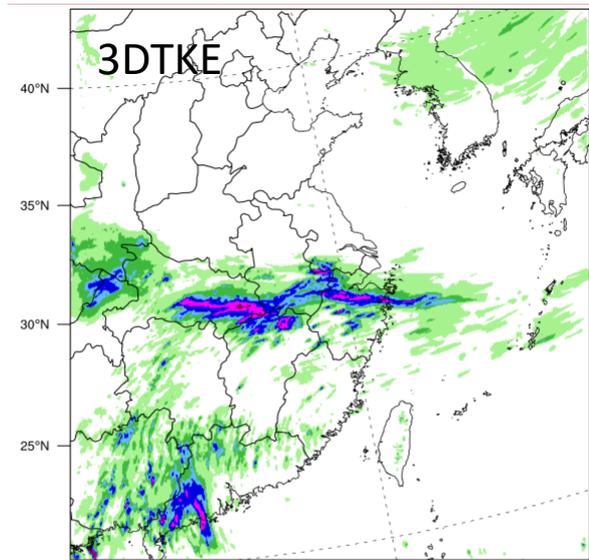
Init: 2017-06-09\_00:00:00  
Valid: 2017060914

SMS-WARMS (2nd) Prediction

Init: 2017-06-09\_00:00:00  
Valid: 2017060914

7060908 TO 2017060914 YSU (mm)

6-hour Total Precipitation : 2017060908 TO 2017060914 MYJ (mm)

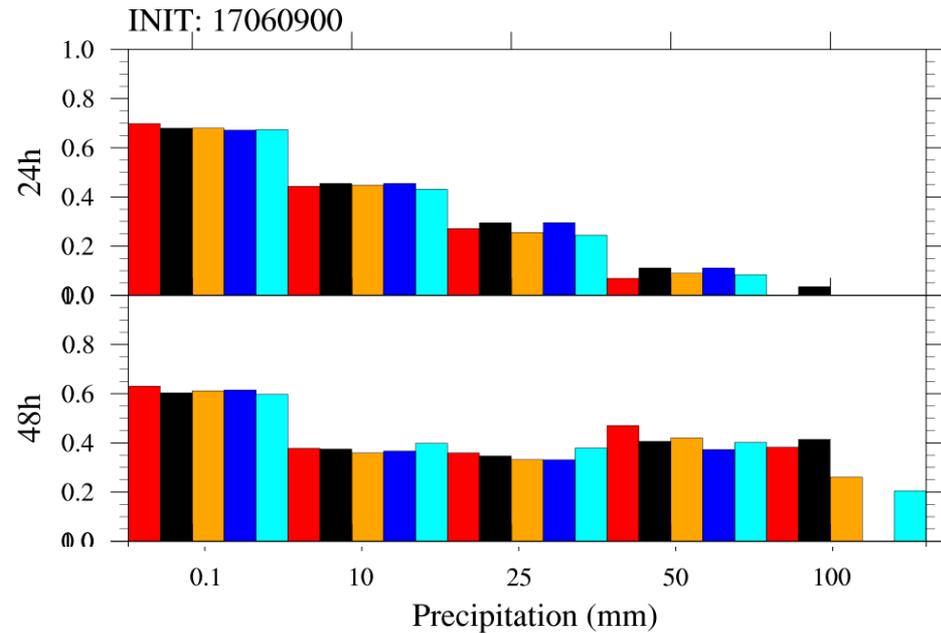
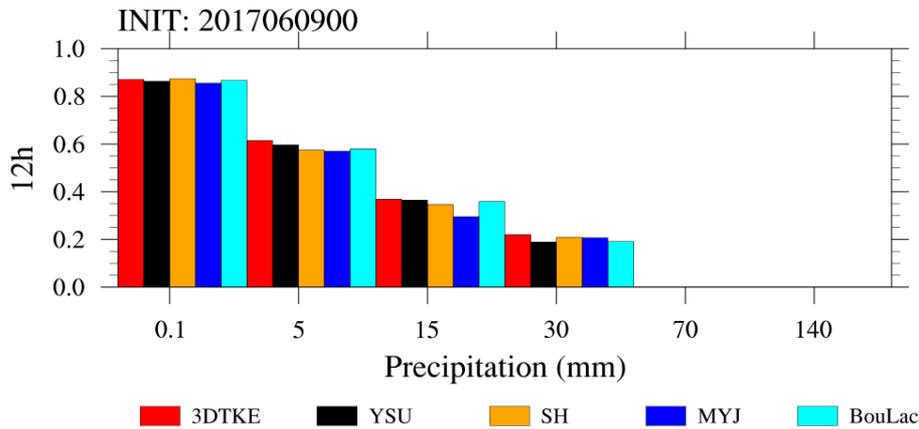


**The new scheme does not deteriorate the distribution and intensity of precipitation.**

# Threat Score of precipitation

## 24h and 48h precipitation forecast with 9km WARMs

### 12h precipitation forecast with 3km WARR



# **km\_opt in WRF namelist**

**km\_opt selects method to compute  $K$**

- 1: constant (khdif and kvdif used)**
  - 2: 1.5-order TKE prediction (Deardorff's model, usually used in LES, not recommended for  $dx > 2$  km, not appropriate for meso)**
  - 3: 3D Smagorinsky (usually used in LES)**
  - 4: 2D Smagorinsky (for horizontal diffusion only, this option is most often used with a PBL scheme)**
  - 5: New scale-aware 3DTKE scheme (SMS-3DTKE). This option extends original Deardorff's model ( $km\_opt = 2$ ) to the mesoscale, and can be used in LES, mesoscale and the gray zone in between. In the horizontal diffusion, the new scheme blends 2D Smag ( $km\_opt = 4$ ) and TKE-based  $K$  ( $km\_opt = 2$ ). In mesoscale limit, horizontal diffusion is recovered to 2D Smag ( $km\_opt = 4$ ). The new scheme can replace option 2 and convective PBL schemes. In LES limit, option 5 is recovered to option 2. Thus, option 5 unifies all diffusion effects into one framework.**
- bl\_pbl\_physics = 0**

# Thank you for your attention!

**Zhang X.**, Jian-Wen Bao, Baode Chen and Evelyn D. Grell, 2018: A Three-Dimensional Scale-adaptive Turbulent Kinetic Energy Model in ARW-WRF Model. *Mon. Wea. Rev.* DOI:10.1175/MWR-D-17-0356.1



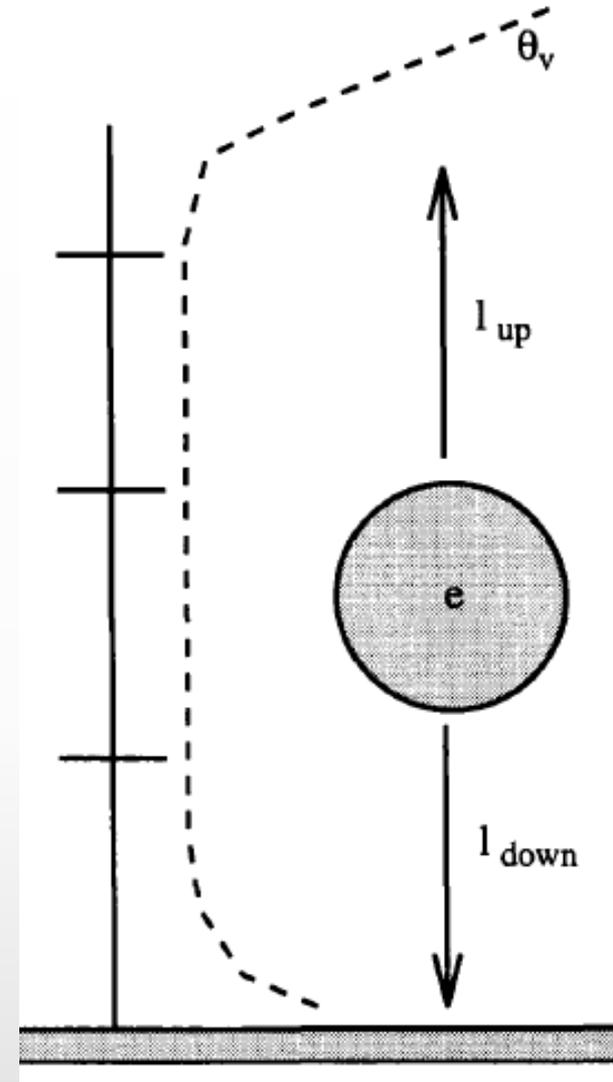
# Free atmosphere diffusion

The length scale at a given level is determined as a function of stability profile of the adjacent levels. The algorithm relies on the computation of the maximum vertical displacement allowed, for a parcel of air having the mean kinetic energy of the level as initial TKE.

$$\int_z^{z+l_{up}} \frac{g}{\theta_0} (\theta(z') - \theta(z)) dz' = e(z)$$

$$\int_{z-l_{down}}^z \frac{g}{\theta_0} (\theta(z) - \theta(z')) dz' = e(z)$$

$$l = \min(l_{up}, l_{down})$$



**The BouLac mixing length is blended with MYNN length scale in a transition layer above PBL.**

*Bougeault-Lacarrere (1989)*

**The calculation of TKE in new scheme is not only confined in PBL.**

# The differences of 3DTKE compared to conventional PBL schemes

$$\frac{\partial e}{\partial t} + \boxed{\overline{U_j} \frac{\partial e}{\partial x_j}} = \boxed{-\overline{(u'_i u'_j)} \frac{\partial \overline{U_i}}{\partial x_j}} + \delta_{i3} \frac{g}{\theta_v} \overline{u'_i \theta'_v} - \frac{1}{\rho} \frac{\partial(\overline{p' u'_i})}{\partial x_i} - \frac{\partial(\overline{u'_j e})}{\partial x_j} - \varepsilon$$

$$-\overline{(u'_i u'_j)} \frac{\partial \overline{U_i}}{\partial x_j} = -\overline{u'^2} \frac{\partial \overline{u}}{\partial x} - \overline{u'v'} \frac{\partial \overline{u}}{\partial y} - \boxed{\overline{u'w'} \frac{\partial \overline{u}}{\partial z}}$$

$$-\overline{v'u'} \frac{\partial \overline{v}}{\partial x} - \overline{v'^2} \frac{\partial \overline{v}}{\partial y} - \boxed{\overline{v'w'} \frac{\partial \overline{v}}{\partial z}}$$

$$-\overline{w'u'} \frac{\partial \overline{w}}{\partial x} - \overline{w'v'} \frac{\partial \overline{w}}{\partial y} - \overline{w'^2} \frac{\partial \overline{w}}{\partial z}$$

1. The 3DTKE scheme uses the complete form of TKE prognostic equation without any approximations;
2. The advection of TKE is calculated in the model dynamics framework, which insures the numerical consistency between subgrid mixing and model dynamics.

# The differences of 3DTKE compared to conventional PBL schemes

$$\begin{aligned}
 \frac{\partial \bar{u}}{\partial t} &= -\bar{u} \frac{\partial \bar{u}}{\partial x} - \bar{v} \frac{\partial \bar{u}}{\partial y} - \bar{w} \frac{\partial \bar{u}}{\partial z} - \frac{1}{\rho} \frac{\partial p}{\partial x} - f\bar{v} - \frac{\overline{\partial u'u'}}{\partial x} - \frac{\overline{\partial u'v'}}{\partial y} - \frac{\overline{\partial u'w'}}{\partial z} \\
 \frac{\partial \bar{v}}{\partial t} &= -\bar{u} \frac{\partial \bar{v}}{\partial x} - \bar{v} \frac{\partial \bar{v}}{\partial y} - \bar{w} \frac{\partial \bar{v}}{\partial z} - \frac{1}{\rho} \frac{\partial p}{\partial y} + f\bar{v} - \frac{\overline{\partial v'u'}}{\partial x} - \frac{\overline{\partial v'v'}}{\partial y} - \frac{\overline{\partial v'w'}}{\partial z} \\
 \frac{\partial \bar{w}}{\partial t} &= -\bar{u} \frac{\partial \bar{w}}{\partial x} - \bar{v} \frac{\partial \bar{w}}{\partial y} - \bar{w} \frac{\partial \bar{w}}{\partial z} - \frac{1}{\rho} \frac{\partial p}{\partial z} + g - \frac{\overline{\partial w'u'}}{\partial x} - \frac{\overline{\partial w'v'}}{\partial y} - \frac{\overline{\partial w'w'}}{\partial z}
 \end{aligned}$$

- 3. The 3DTKE scheme combines the horizontal and vertical subgrid turbulent mixing into a single energetically consistent framework;
- 4. The 3DTKE scheme includes the tendency from subgrid mixing in vertical velocity equation. In hydrostatic model, there is no prognostic equation of vertical velocity.