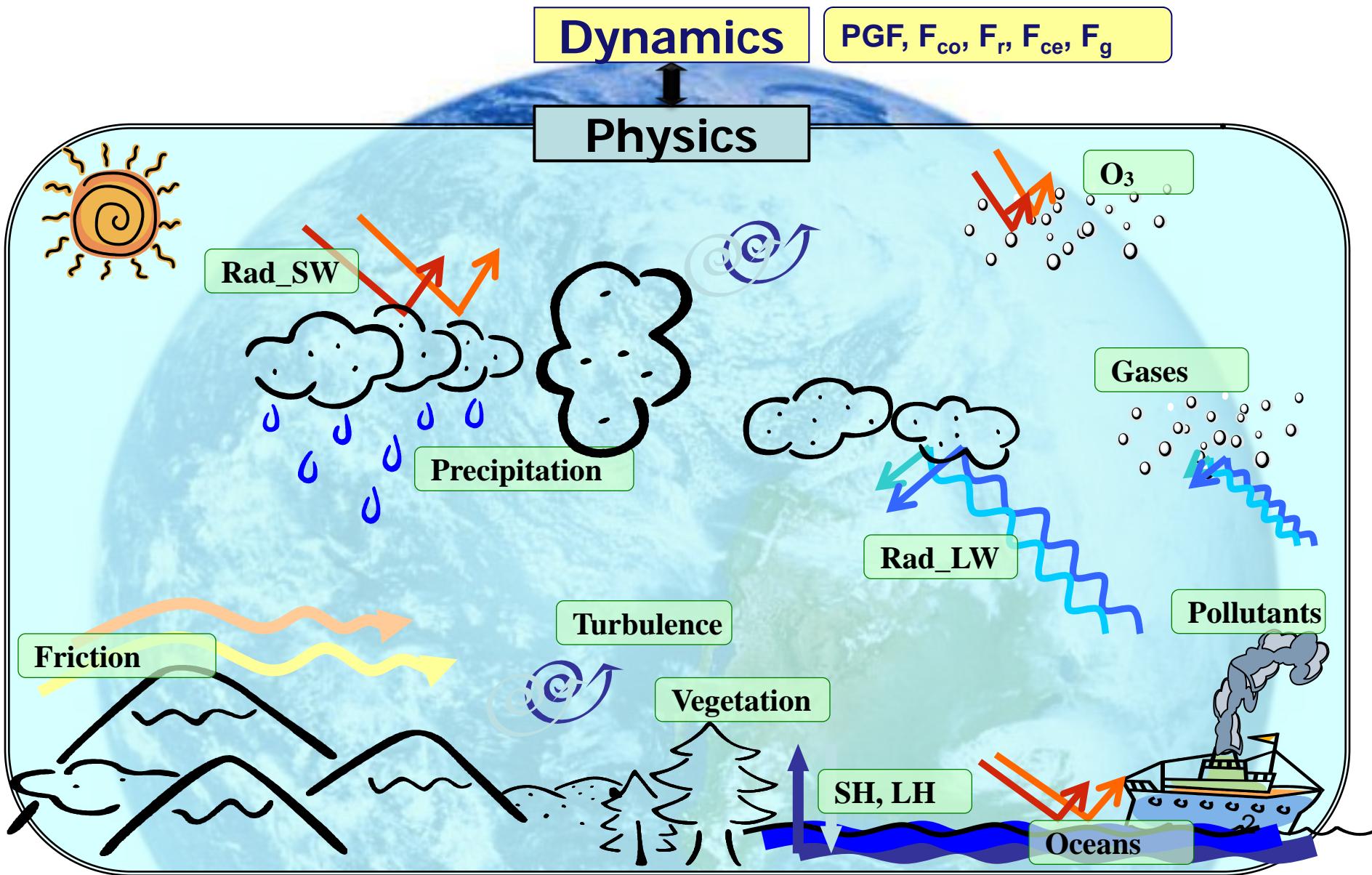


# **Physics Algorithms : Overview**

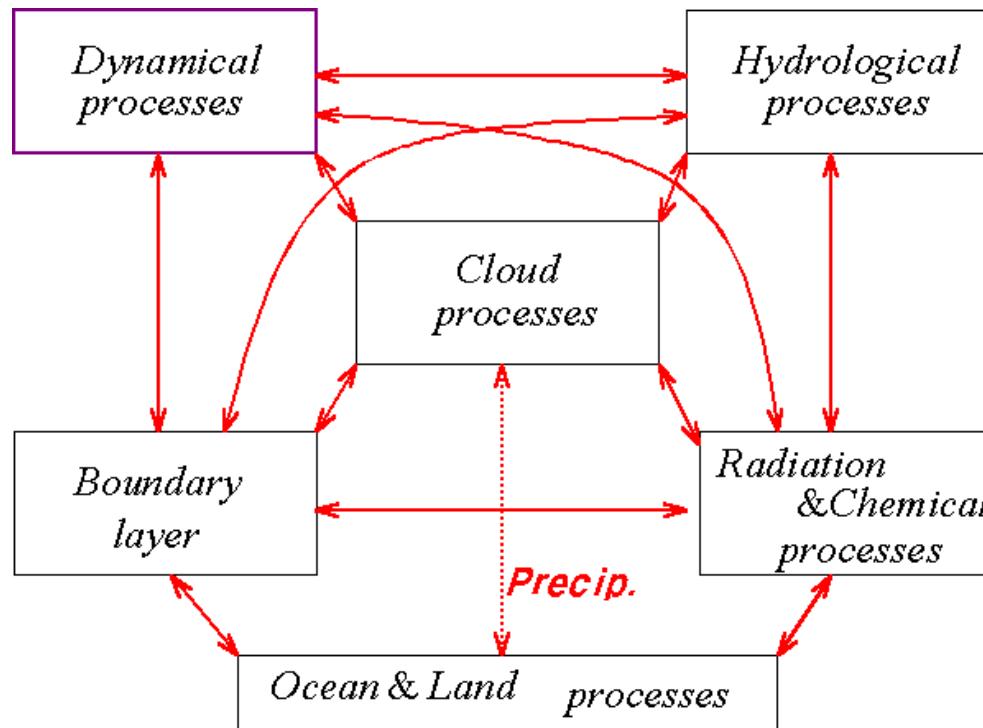
**Song-You Hong**

Yonsei University

# 0. Introduction



# Schematic configuration of physics



## \* Physical process in the atmosphere

: Specification of heating, moistening and frictional terms in terms of dependent variables of prediction model  
→ Each process is a specialized branch of atmospheric sciences.

## \* Parameterization

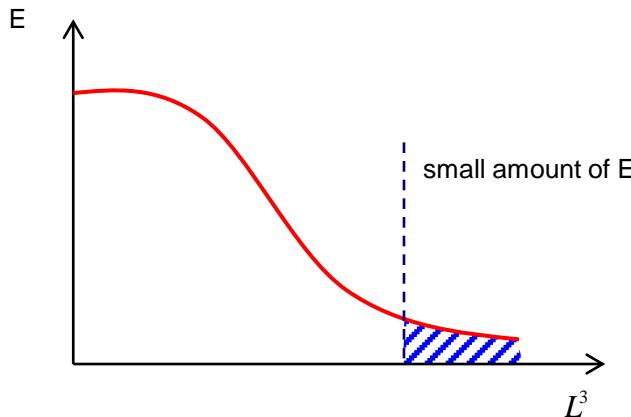
The formulation of physical process in terms of the model variables as parameters.  
(constants or functional relations)

# 1) Subgrid scale process

## \* Subgrid scale process

Any numerical model of the atmosphere must use a finite resolution in representing continuum certain physical & dynamical phenomena that are smaller than computational grid.

- Subgrid process (Energy perspective)

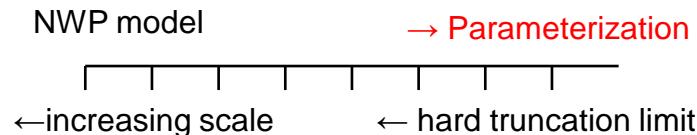
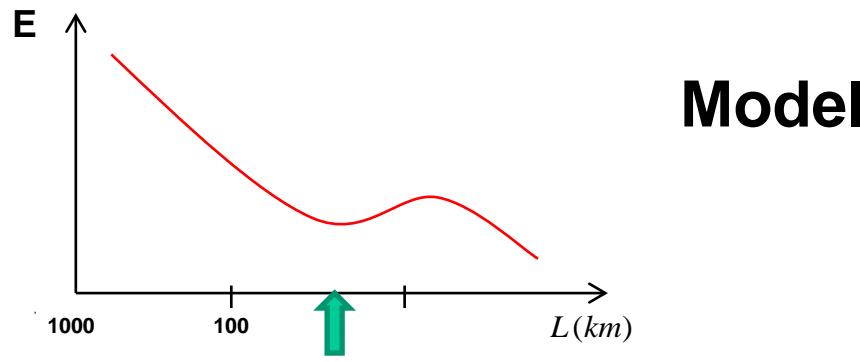


- $\Delta x \rightarrow 0$ , the energy dissipation takes place by molecular viscosity (smallest grid size  $\gg$  idealized situation)

## • Objective of subgrid scale parameterization

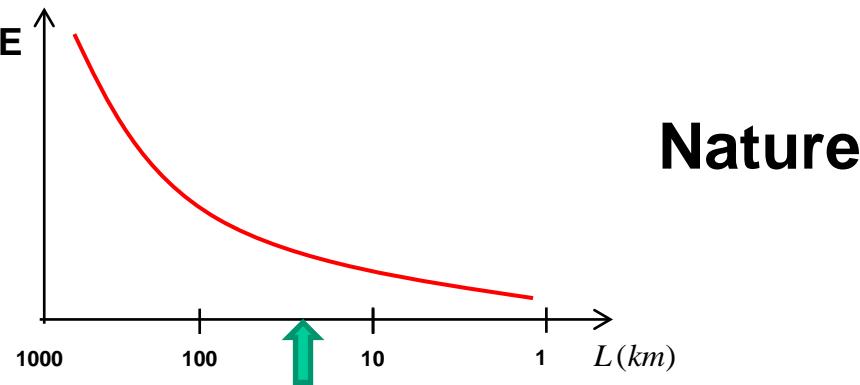
"To design the physical formulation of energy sink, withdrawing the equivalent amount of energy comparable to cascading energy down at the grid scale in an ideal situation."

※ Parameterization that are only somewhat smaller than the smallest resolved scales.



Where truncation limit ; spectral gap

Unfortunately, there is no spectral gap



## 2) Subgrid scale process & Reynolds averaging

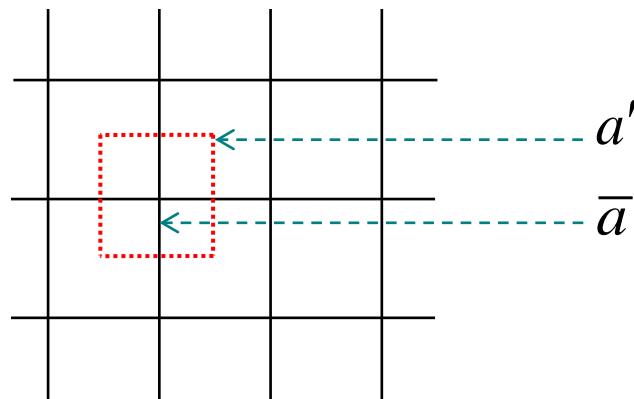
Consider prognostic water vapor equation

$$\frac{\partial \rho q}{\partial t} = -\frac{\partial \rho u q}{\partial x} - \frac{\partial \rho v q}{\partial y} - \frac{\partial \rho w q}{\partial z} + \rho E - \rho C \quad \dots(1)$$

In the real atmosphere,

$$u = \bar{u} + u', \quad q = \bar{q} + q' \quad \left( \begin{array}{l} \text{*} \bar{a} : \text{grid-resolvable} \\ a' : \text{subgrid scale perturbation} \end{array} \right)$$

$\rho'$  is neglected



\* **Rule of Reynolds average** :  $\overline{q'} = 0, \overline{u'q} = 0, \overline{\bar{u}q} = \bar{u}\bar{q}$

then eq.(1) becomes

$$\frac{\partial \rho \bar{q}}{\partial t} = -\frac{\partial \rho \bar{u}q}{\partial x} - \frac{\partial \rho \bar{v}q}{\partial y} - \frac{\partial \rho \bar{w}q}{\partial z} - \frac{\partial \rho \bar{u}'q'}{\partial x} - \frac{\partial \rho \bar{v}'q'}{\partial y} - \frac{\partial \rho \bar{w}'q'}{\partial z} + \rho E - \rho C \quad \dots(2)$$

..... : .....

①                    ②

- ① grid-resolvable advection (dynamical process)
- ② turbulent transport

\* **How to parameterize the effect of turbulent transport**

- a)  $-\rho \overline{w'q'} = 0$  : 0th order closure
- b)  $-\rho \overline{w'q'} = K \frac{\partial \bar{q}}{\partial z}$  : 1st order closure (K-theory)
- c) obtain a prognostic equation for  $\overline{w'q'}$  from (1), (2)

$$\frac{\partial \rho w q}{\partial t} = -\frac{\partial \rho u w q}{\partial x} + \dots$$

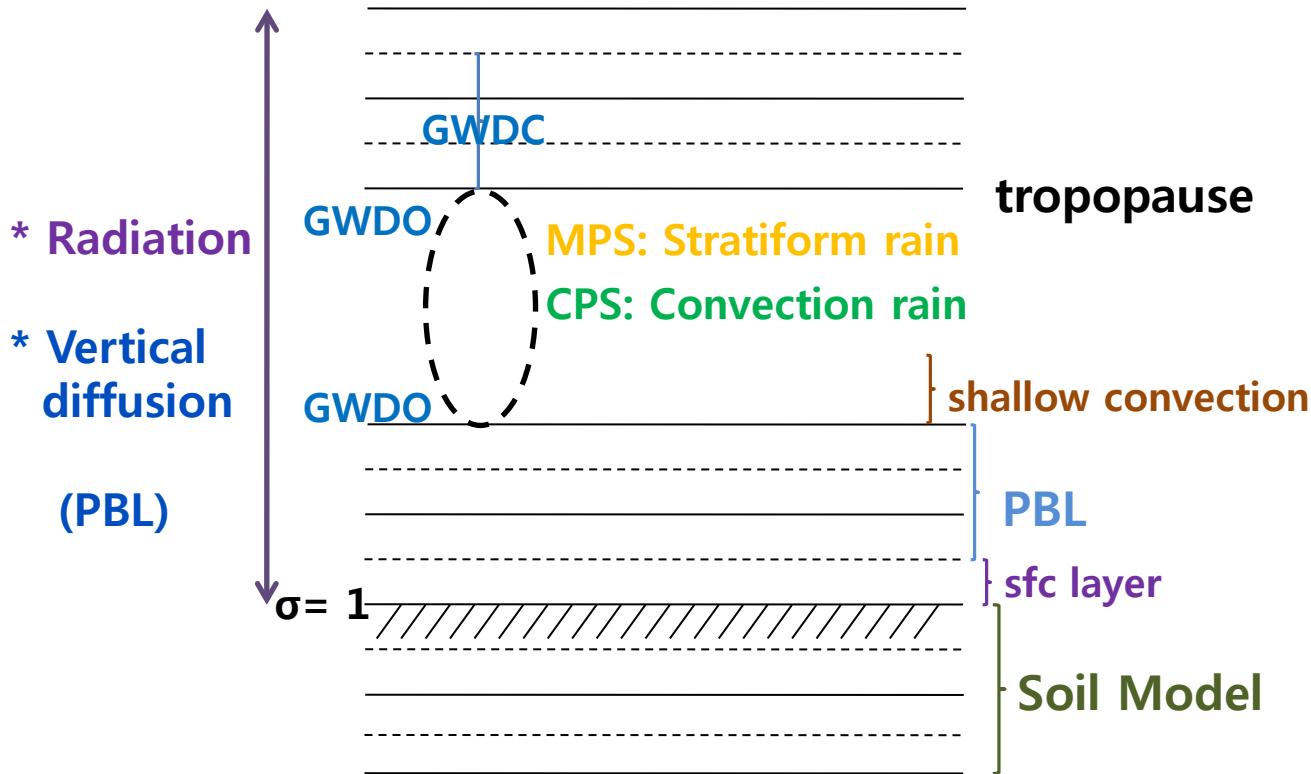
taking Reynolds averaging,

$$\frac{\partial \overline{\rho w'q'}}{\partial t} = \frac{\partial \overline{\rho w'w'q'}}{\partial z}$$

$$-\rho \overline{w'w'q'} = K' \frac{\partial \overline{\rho w'q'}}{\partial z} \quad : \text{2nd order closure}$$

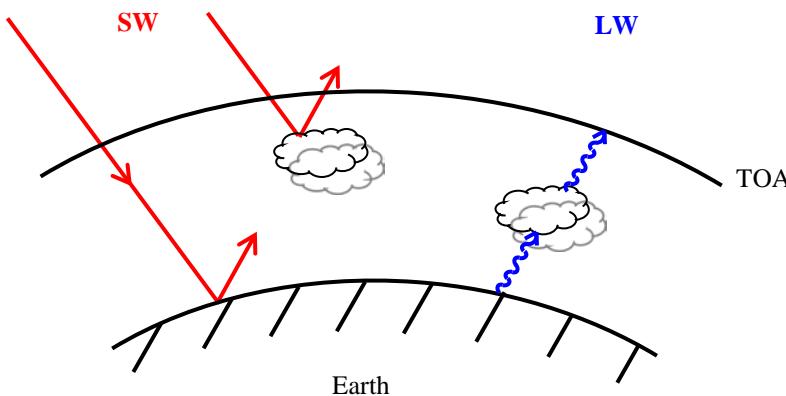
# In modeled atmosphere : 7 or more

$$\frac{d \ln \theta}{dt} = \frac{H}{c_p T}, \quad \frac{dq}{dt} = S, \quad \frac{d\vec{u}}{dt} = \nabla_z \vec{\tau}$$



# 1. Radiation

## 1.1 Concept



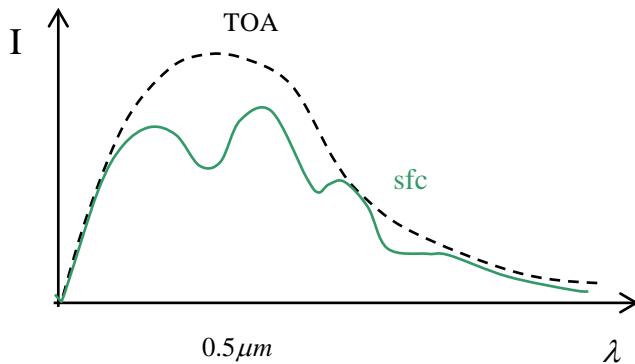
TOA :  $S = 1360 \text{ Wm}^{-2}$  , Mean Flux :  $\frac{S}{4} = 340 \text{ Wm}^{-2}$  → Energy source for Earth

30% : reflected from the atmosphere clouds

$\left. \begin{array}{l} 25\% : \text{absorbed in the atmosphere} \\ 45\% : \text{absorbed at the earth surface} \end{array} \right\} \rightarrow \text{Back to space by terrestrial infrared radiation}$

At low latitude : energy gain  
At high latitude : energy loss

## 1.2 Solar radiative transfer



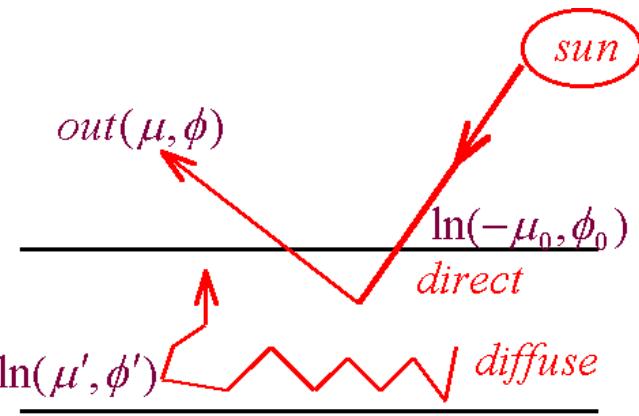
- At TOA,

$$F = S \left( \frac{dm}{d} \right)^2 \cos \theta_0 \quad (\theta_0 : \text{Zenith angle}) \quad \mu = \cos \theta \\ \text{(Insolation)}$$

- Basic equations

$$\mu \frac{dI(\tau, \mu, \phi)}{d\tau} = I(\tau, \mu, \phi) - J(\tau, \mu, \phi) \\ \text{absorption} \quad \text{source emission}$$

$$d\tau = -k_v \rho_a dz \quad \tau(\text{optical depth}) = \int_z^{z_\infty} k_v(z') \rho_a(z') dz' \\ = \int_0^p k_v(p') q(p') \frac{dp'}{g}$$



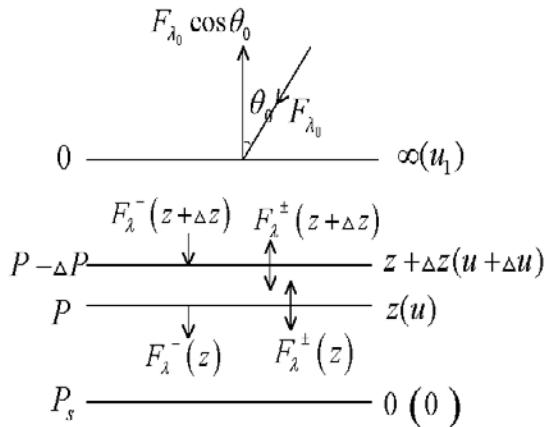
$$J = J(\tau, \mu, \phi) = \frac{\tilde{\omega}}{4\pi} \int_0^{2\pi} \int_{-1}^1 I(\tau, \mu', \phi') P(\mu, \phi; \mu', \phi') d\mu' d\phi' \text{ [diffuse (multiple) scattering]}$$

$$+ \frac{\tilde{\omega}}{4\pi} F_0 P(\mu, \phi; -\mu_0, \phi_0) e^{-\frac{\tau}{\mu_0}} \text{ [single(direct) scattering]}$$

$P$ : Scattering phase function : redirects  $(\mu', \phi') \rightarrow (\mu, \phi)$   
 $\tilde{\omega} = \frac{\sigma_s}{\sigma_e}$ : Scatteing albedo  
 scattering cross section/extinction(scattering + absorption) cross section

- \* remove  $\phi$  dependency using  $P(\cos \theta)$  function
- \*  $P, \tilde{\omega}$ , Albedo depend on  $\lambda$ , particle size & shape.

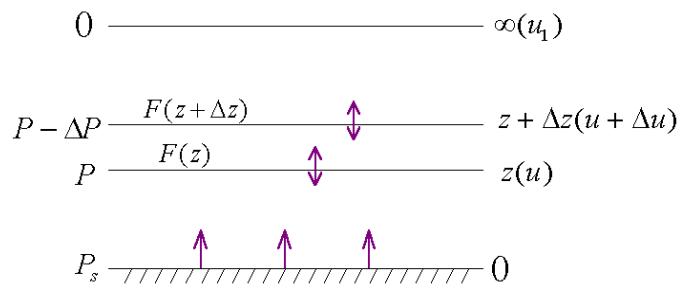
$$P(\cos \phi) = \sum_{l=0}^N \tilde{\omega}_l P_l(\cos \phi) \quad : \text{Legendre Polynomial}$$



Radiative transfer equation solver.

→  $\begin{cases} \text{Discrete - ordinates method} \\ \text{Two - Stream and Eddington's approximation} \\ \text{Delta - function adjustment and similarity principle} \\ \delta - \text{Four stream approximation} \end{cases}$

## 1.3 Terrestrial radiation

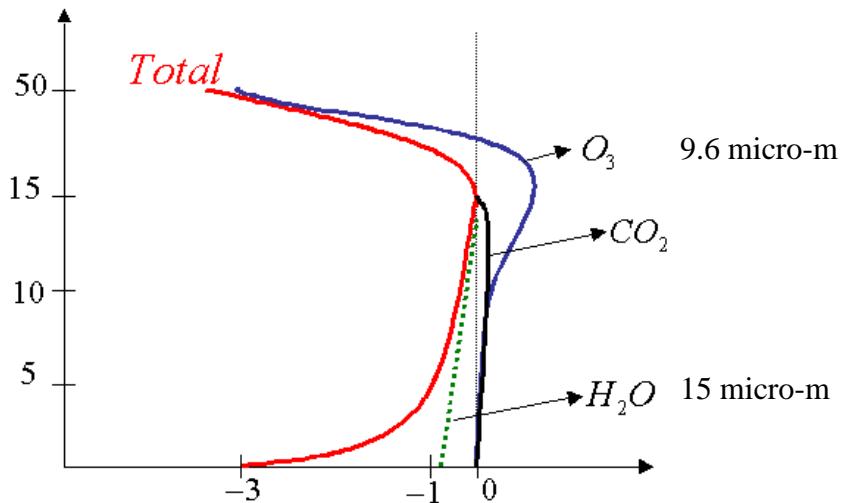


$0, \mu$	.....	$\tau_\infty, z_\infty, 0$
$\tau', \mu'$	.....	$\tau', z', P'$
$\tau, \mu$	.....	$\tau, z, P$
$\tau', \mu'$	.....	$\tau', z', P'$
$\tau, 0$	.....	$\tau_s, 0, P_*$

$$F(z) = F^\uparrow(z) - F^\downarrow(z)$$

$$\Delta F = F(z + \Delta z) - F(z)$$

$$\left. \frac{\partial T}{\partial t} \right|_{IR} = - \frac{1}{c_p \rho} \frac{\Delta F}{\Delta P} = - \frac{g}{c_p} \frac{\Delta F}{\Delta u}$$



In spectral bands (monochromatic)

$$\uparrow \mu \frac{dI_\nu(\tau, \mu)}{d\tau} = I_\nu(\tau, \mu) - B_\nu(T)$$

$$\downarrow -\mu \frac{dI_\nu(\tau, -\mu)}{d\tau} = I_\nu(\tau, -\mu) - B_\nu(T)$$

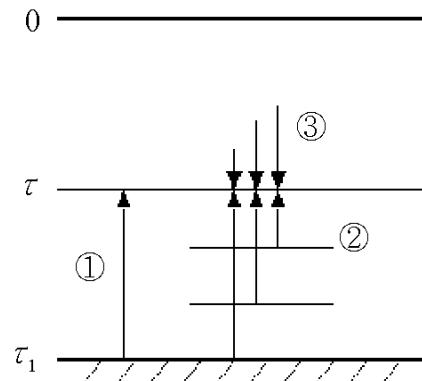
B.C.  $\begin{cases} SFC (\tau = \tau_1), I_\nu(\tau, \mu) = B_\nu(T_s) \\ TOP (\tau = 0), I_\nu(0, -\mu) = 0 \end{cases}$

$$F^\uparrow(\tau) = 2\pi B_\nu(T_s) \int_0^1 e^{-\frac{(\tau_1-\tau)}{\mu}} \mu d\mu + 2 \int_0^1 \int_{\tau}^{\tau_1} \pi B_\nu[T(\tau')] e^{-\frac{(\tau'-\tau)}{\mu}} d\tau' d\mu$$

$$F^\downarrow(\tau) = 2 \int_0^1 \int_0^\tau \pi B_\nu[T(\tau')] e^{-\frac{(\tau-\tau')}{\mu}} d\tau' d\mu$$

$$d\tau = -k_\nu \rho dz$$

$$\tau_1 = \int_0^{u_1} k_\nu du, \quad u_1 = \int_0^\infty \rho dz$$



# 1.4 Cloud fraction

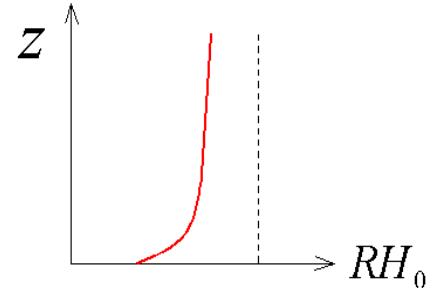
## 1) Conventional method

$$f = f_c + f_l$$

$f_c$  : depends on precipitation,  $p_{\text{top}}$ ,  $p_{\text{bottom}}$

$$f_l : \text{depends on RH} = 1 - \left[ \frac{1 - RH}{1 - RH_0} \right]^{0.5}$$

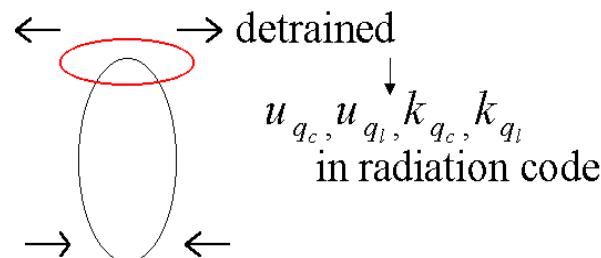
where  $RH_0$  is the critical value of RH which is optimized based on observations. (Slingo's method)



## 2) Advanced method

- inclusion of ice, liquid
- consistent treatment of water substance for both precipitation & radiative properties.

$f_c$  : uses information of detrainated water substances from sub-grid scale clouds in convective parameterizations



$f_l$

$q_c, q_s, q_i, \dots$

## i) with diagnostic microphysics (CCM3)

- cloud water scale height  $r_l$

$$h_l = a \ln(1.0 + \frac{b}{g} \int_{P_T}^{P_S} q dp)$$

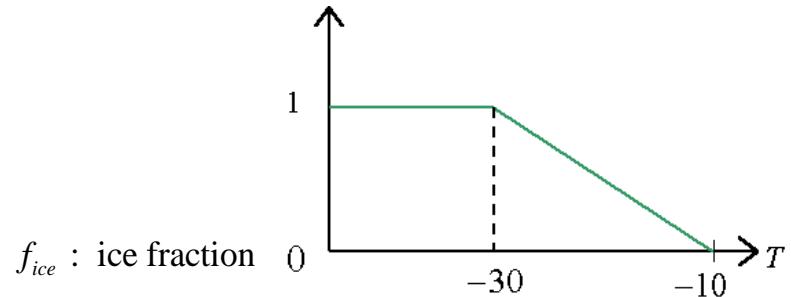
- cloud droplet size,

$$r_{ee} \begin{cases} = 10 \mu m & \text{over ocean} \\ < 10 \mu m & \text{over land} \end{cases}$$

... warm cloud

$$r_{ei} : \begin{matrix} 10 \mu m \sim 30 \mu m \\ (\text{low}) \quad (\text{high}) \end{matrix}$$

... ice cloud



- The radiation properties of ice cloud in the short wave spectral region :

$$\tau_i^c = \text{cwp} \left[ a_i + \frac{b_i}{r_{ei}} \right] f_{ice} \quad (\text{optical thickness})$$

$$w_i^c = 1 - c_i - d_i r_{ei} \quad (\text{co-albedo})$$

$$g_i^c = e_i - f_i r_{ei} \quad (\text{asymmetry factor})$$

$$f_i^c = (g_i)^2$$

a-f : coeff : depends upon band and k-

$$\bar{\tau}_c = \sum_i \tau_i \quad i : \text{each gas}$$

(The effective optical thickness for each spectral band)

- The long wave cloud emissivity (  $E_{cld}$  )

$$c_f' = E_{cld} c_f$$

$$E_{cld} = 1 - e^{-Dk_{abc}cwp}$$

$\approx D = 1.66$  : diffusivity factor

$k_{abc}$  : LW absorptivity coefficient.

$$= k_l (1 - f_{ice}) + k_i f_{ice}$$

## ii) with prognostic microphysics (MM5, WRF)

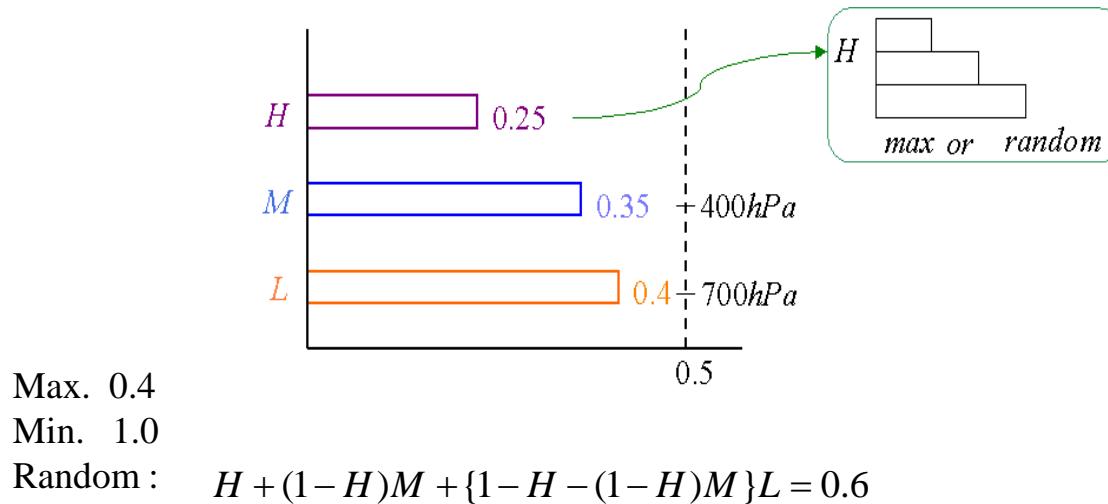
$\alpha_p$  (absorption coefficient)

$$= \frac{1.66}{2000} \left( \frac{\pi N_0}{\rho_{rs}^3} \right)^{\frac{1}{4}} m^2 g^{-1} = \begin{cases} 2.34 \times 10^{-3} & m^2 g^{-1} \text{ for snow} \\ 0.33 \times 10^{-3} & m^2 g^{-1} \text{ for rain} \end{cases}$$

-  $u_p$  (effective water path length)

$$= (\rho q_{rs})^{\frac{3}{4}} \Delta z \times 1000 \text{ } gm^{-2} \rightarrow \tau_p \text{ (transmission)} = \exp(-\alpha_p u_p)$$

### iii) Cloud overlapping



$\tau$  is scaled by  $A_c$  (cloud cover) at a given layer.



- Flux for each of  $A_c, (1-A_c)$   $\rightarrow$  summation

※ In very high resolution  $A_c = 0$  or  $1$  ↵ in WRF

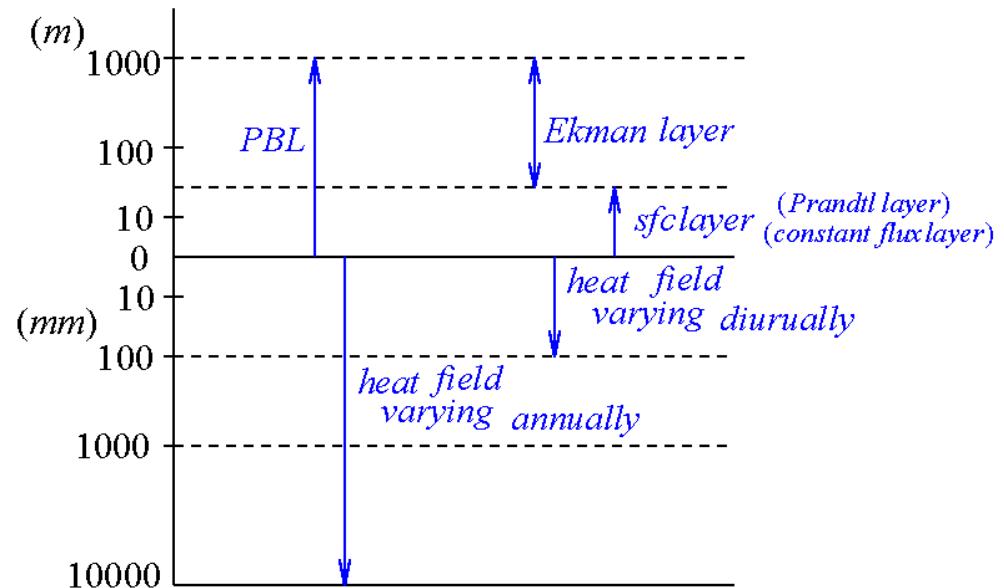


# 2. Land-surface processes

## 2.1 Concept

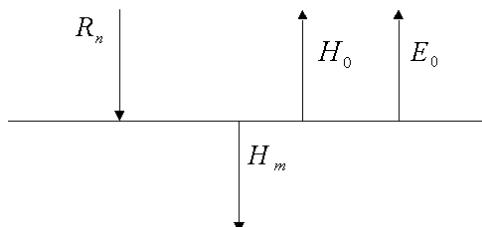
### 1) Surface layer

: compute surface fluxes and update surface temperature and humidity by solving soil model and surface energy budget



### 2) Surface energy budget

$$C_g \frac{\partial T_s}{\partial t} = R_n - H_m - H_0 - E_0$$



## 2.2 Surface layer

### 1) Bulk method

$$H_0 = \rho C_p C_H |\vec{V}_a| \Delta T$$

$$E_0 = \rho L C_H |\vec{V}_a| \Delta q M_a$$

$$\vec{\tau}_0 = \rho C_D |V_a| \vec{V}_a$$

$$C_D, C_H = fn(R_i, Z_0, \dots)$$

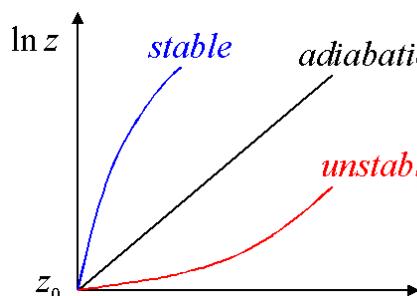
$$\begin{cases} \frac{\partial T}{\partial z} = \frac{\partial}{\partial z} \frac{H_0}{C_p} + \frac{T}{\theta} \rho k_z \frac{\partial \theta}{\partial z} & \text{at surface layer} \\ \frac{\partial T}{\partial t} = \frac{T}{\theta} \rho k_z \frac{\partial \theta}{\partial z} & \text{above sfc} \end{cases}$$

where  $k_z = fn(R_i, S)$   
  
 .....wind shear

### 2) Monin-Obukov similarity

$$\frac{k_z}{u_*} \frac{\partial u}{\partial z} = \phi_m(z/L), \quad \frac{k_z}{u_*} \frac{\partial \theta}{\partial z} = \phi_t(z/L)$$

$$\text{Integrate, } F_m = \int_{z_0}^{h_s} \frac{dz}{z} \phi_m dz = \ln\left(\frac{h_s}{z_0}\right) - \psi_m(h_s, z_0, L)$$



$$\bar{u} = C_u \left[ \ln \frac{z}{z_0} + \Phi \right] : \text{curving factor } \Phi$$

※ **Profile function** :  $\phi_m$  and  $\phi_t$

Dyer and Hicks formula for similarity  
(Businger formula : complex)

- unstable ( $L < 0$ )

$$\phi_m = (1 - 16 \frac{0.1h}{L})^{-\frac{1}{4}} \quad \text{for } u, v$$

$$\phi_t = (1 - 16 \frac{0.1h}{L})^{-\frac{1}{2}} \quad \text{for } \theta, q$$

- stable ( $L > 0$ )

$$\phi_m = \phi_t = (1 + 5 \frac{0.1h}{L})$$

$$\text{where } L = u_*^2 \bar{\theta} / (kg\theta_*) = -\frac{\rho C_p \theta_0 u_*^3}{kgH_0}$$

$$Ri = \frac{\frac{g}{\theta} \frac{\partial \theta}{\partial z}}{\left(\frac{\partial u}{\partial z}\right)^{-2}}$$

$$\frac{h_s}{L} = \frac{\phi_m^2 (hs/L)}{\phi_t (hs/L)} Ri$$

Given the  $F_m, F_H, C_D = k^2 / F_m^2, C_Q = C_H = k^2 / (F_m F_t), u_* = kU / F_m$

$$\tau_0 = \rho k_m \frac{du}{dz} = -\overline{u'w'} = \rho C_p U^2$$

$$H_0 = -\rho C_p k_h \frac{d\theta}{dz} = \rho C_p \overline{\theta'w'} = -\rho C_p C_H U \Delta \theta$$

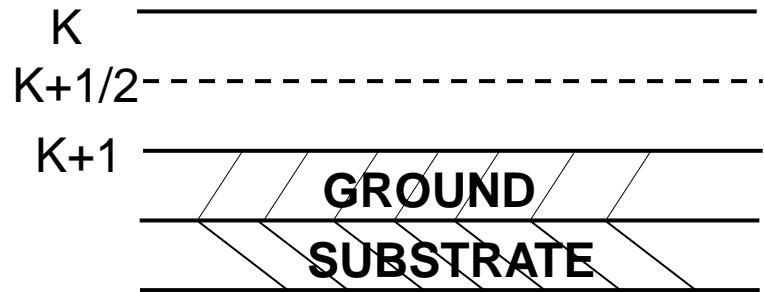
$$E_0 = -\rho L \overline{q'w'} = -\rho L C_q U \Delta q$$

## 2.3 Soil model

### 1) Slab model

$$\frac{\partial T_s}{\partial t} = \lambda_T(R_n - LE - H) - \frac{2\pi}{\tau}(T_s - T_2)$$

$$\frac{\partial T_m}{\partial t} = \frac{1}{\tau}(T_s - T_m)$$

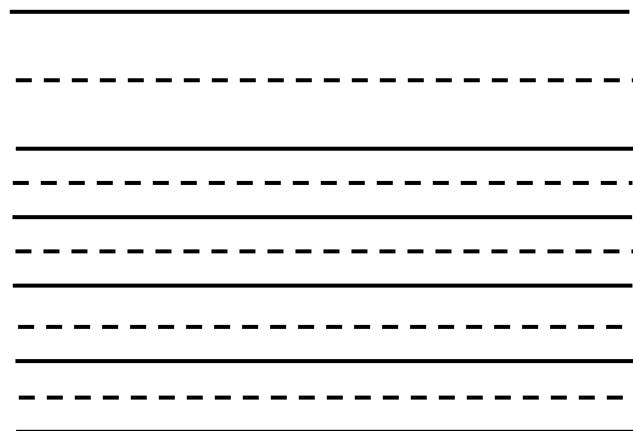


### 2) Multi-layer model

$$\frac{\partial T_s}{\partial t} = \lambda_T(R_n - LE - H)$$

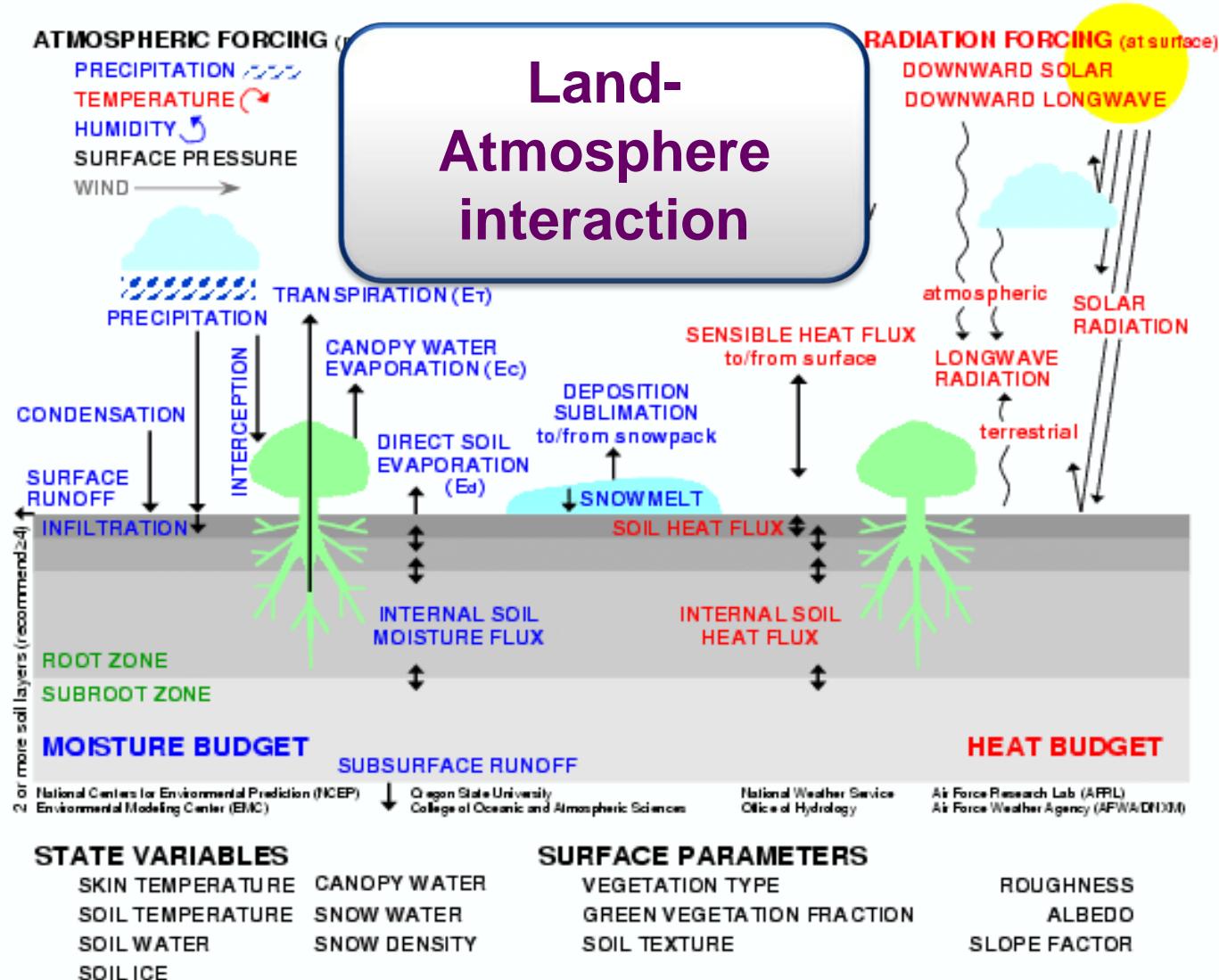
$$(\rho C)_i \frac{\partial T}{\partial t} = \frac{\partial}{\partial z} (\lambda_T \frac{\partial T}{\partial z})$$

$$\frac{\partial \eta}{\partial t} = \frac{\partial}{\partial z} (D \frac{\partial \eta}{\partial z}) + \frac{\partial K}{\partial z} + F_\eta$$



- NOAH, SIB, PLACE, VIC, CLM, etc

## 2.4. NOAH soil model (Chen and Dudhia 2001)



## **Method : Penman Approach**

A combination of the energy balance and bulk transfer formula

$$Evap: = E_{dir} + E_c + E_t$$

### **i) $E_{dir}$ (direct evaporation)**

: direct evaporation from the bare soil, using the soil water flux at the surface

$$E_{dir} = (1 - \sigma_f) \left[ -D(\Theta)_0 - K(\Theta)_0 \right]$$

vegetation fraction    diffusivity              conductivity

### **ii) $E_c$ (Canopy reevaporation)**

: when rain falls to the ground, the leaves first intercept the rain up to a S. The canopy water then reevaporates and the excess drips to the ground canopy water amount, n = 0.5

$$E_c = \sigma_f \left( \frac{C^*}{S} \right)^n E_p$$

canopy capacity (=0.002m)

### iii) $E_t$ (Transpiration)

: process whereby extracts water from the root zone and release it to the atmosphere from the leaf stomata during photosynthesis

$$E_t = \sigma_f \left(1 - \frac{C^*}{S}\right)^n \bar{\beta} E_{tp}, \quad \beta_i = \frac{\Theta_i - \Theta_{wilt}}{\Theta_{fc} - \Theta_{wilt}}$$

Saturation ratio

### iv) $E_p$ (Potential evaporation) and $E_{tp}$ (potential evapotranspiration)

$E_p$  : Maximum evaporation when soil is saturated

$E_{tp}$  : Maximum evaporation when plant has no water stress

$$R_{net} = G + H(T_s) + LE_p$$

$$LE_p = \frac{[R_{net} - G]\Delta + (1 + \gamma)LE_a}{\Delta + 1 + \gamma}$$

$$LE_{tp} = \frac{[R_{net} - G]\Delta + (1 + \gamma)LE_a}{\Delta + (1 + \gamma)(1 + C_h Vr_s)}$$

where  $\gamma = \frac{4\sigma T_a^3}{\rho_a C_p C_h U}$      $\Delta = \frac{L}{C_p} \frac{dq_s}{dT} \Big|_{T_a}$      $E_a = \rho_a C_h U [q_s(T_a) - q_a]$

drying power of air

## v) Soil hydrology : Darcy's law

$$\frac{\partial \Theta}{\partial t} = \frac{\partial}{\partial z} \left[ D(\Theta) \frac{\partial \Theta}{\partial z} \right] + \frac{\partial K(\Theta)}{\partial z}$$

Precipitation and direct evaporation form the water flux at the surface while deep layer drainage provides the bottom boundary condition. When precipitation rate exceeds the rate at which the soil can transport the water downward, runoff is assumed.

## vi) Canopy budget

$$\frac{dC^*}{dt} = \sigma_f \text{ Precip} - E_c$$

## vi) Soil thermodynamics

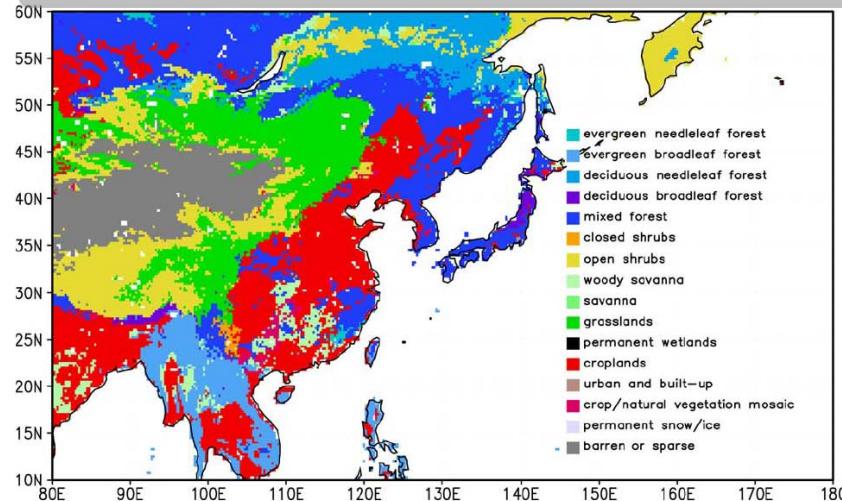
$$C(\Theta) \frac{\partial T}{\partial t} = \frac{\partial}{\partial z} \left[ K_T(\Theta) \frac{\partial T}{\partial z} \right]$$

heat capacity with the ground heat flux as the surface boundary condition, and prescribed deep soil temperature

## 2.5. Vegetation type → $z_0$ , albedo

### Vegetation types

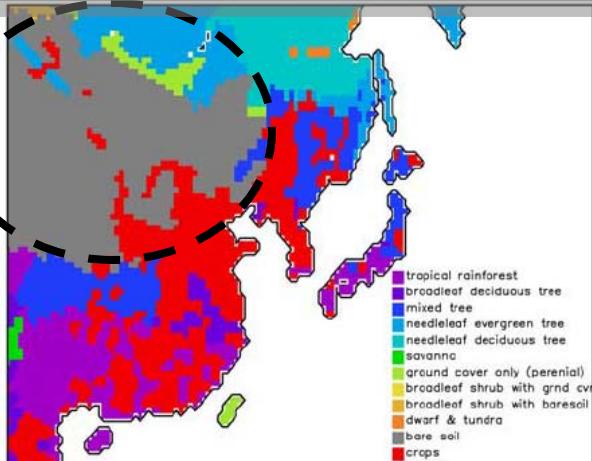
MODIS (satellite)



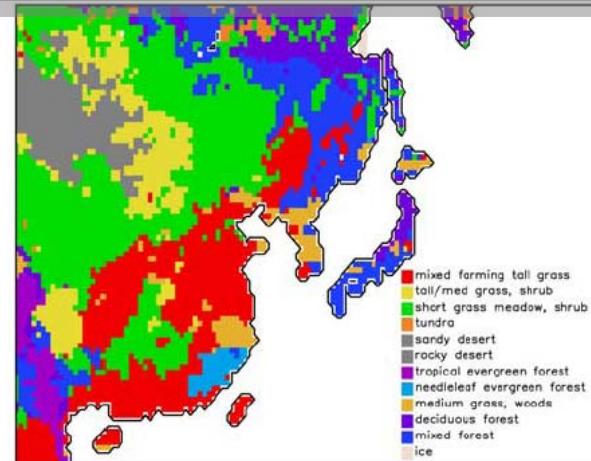
13 type data set  
1 degree

12 type data set  
20 min

The Simple Biosphere model (SiB)



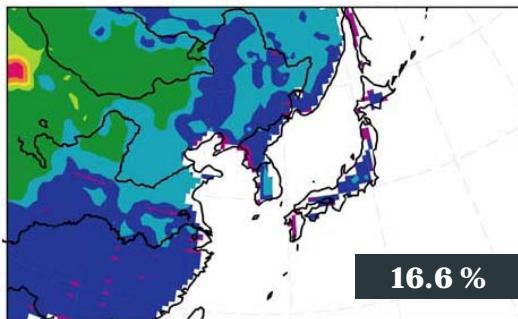
United States Geological Survey's (USGS)



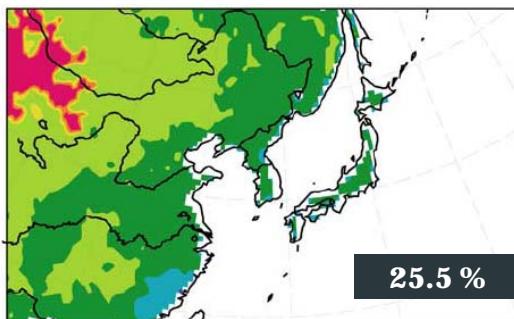
## Albedo and Roughness length ( $z_0$ )

Albedo

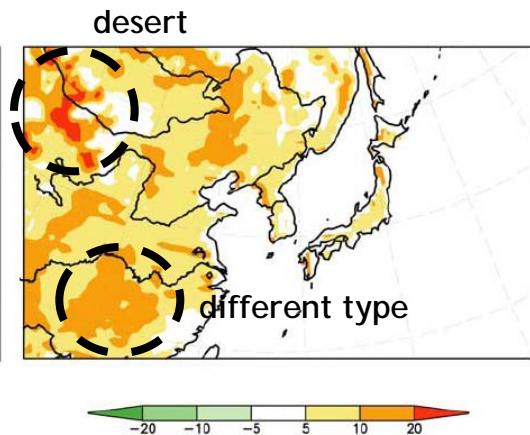
Sib



USGS

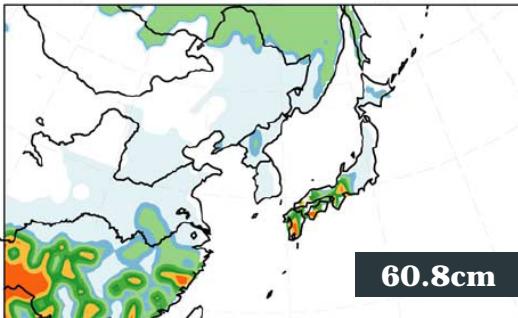


USGS-Sib

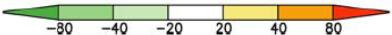
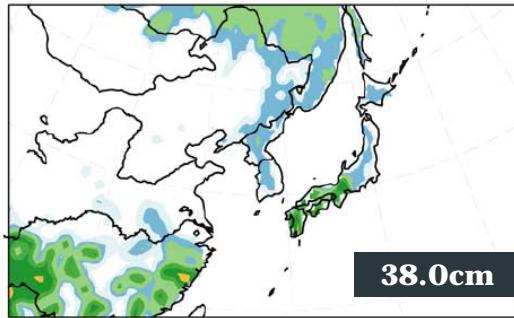


Roughness length

60.8cm



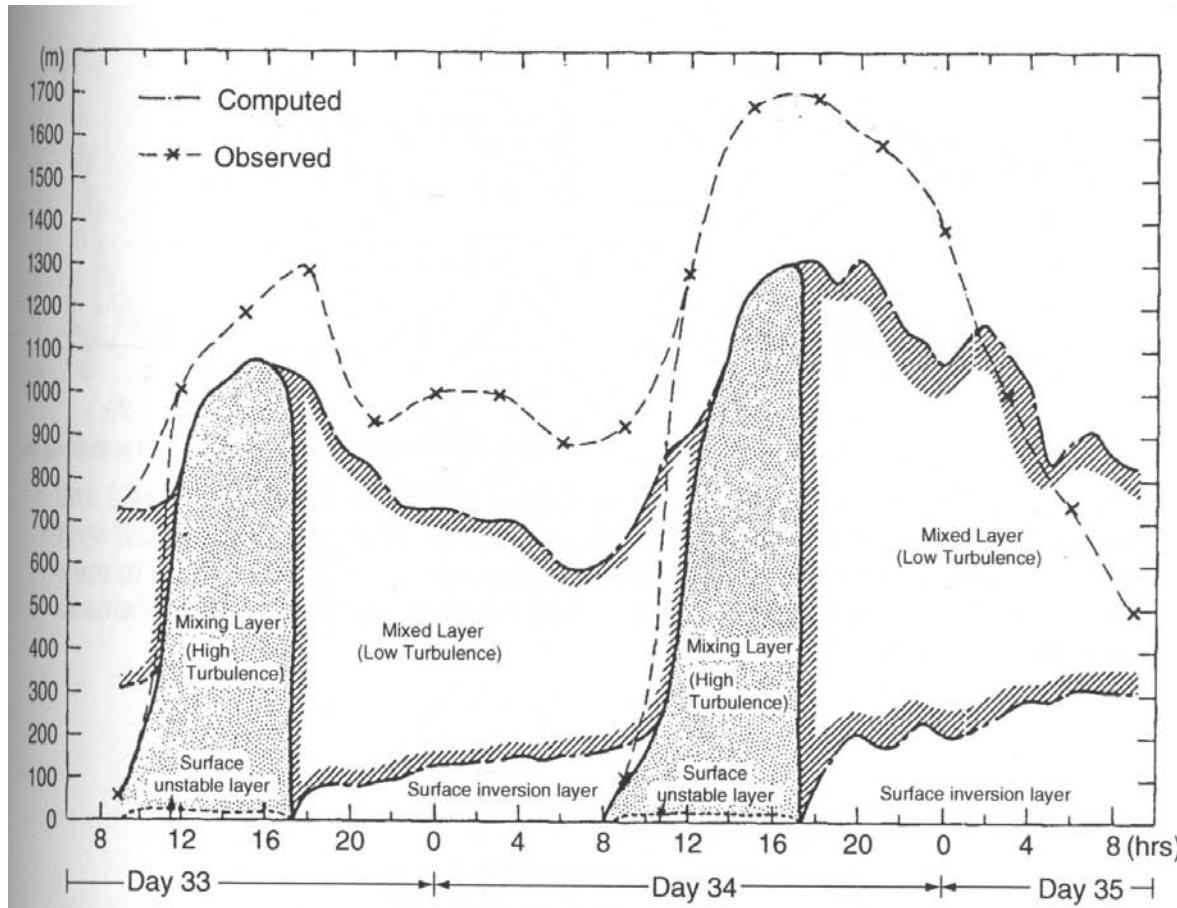
38.0cm



### 3. Vertical diffusion (PBL)

#### Purpose

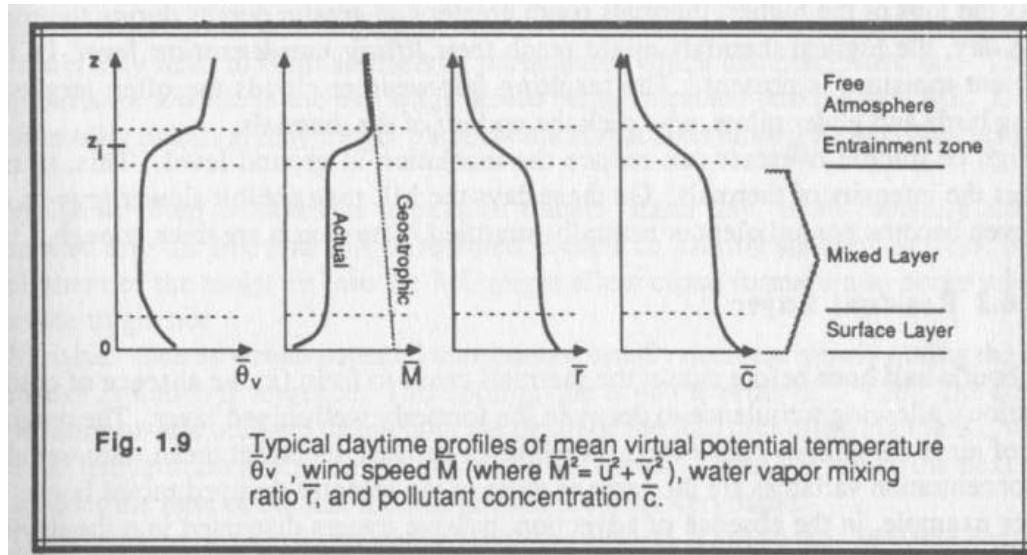
- computes the parameterized effects of vertical turbulent eddy diffusion of momentum water vapor and sensible heat



Yamada and Mellor(1975)

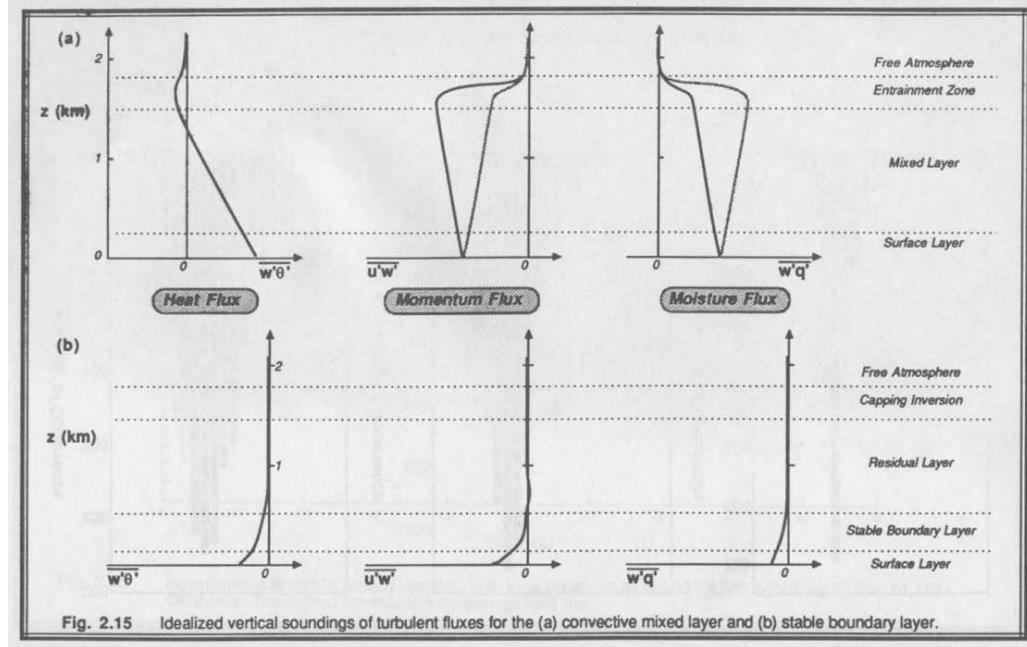
# Planetary Boundary Layer Structure

## Daytime profiles



## Daytime flux profiles

## Nighttime flux profiles



From Stull (1988)

## \* Classifications :

### 3.1 Local vertical diffusion

$$\frac{\partial c}{\partial t} = \frac{\partial}{\partial z} \left( k_c \frac{\partial c}{\partial z} \right) \quad \text{※ } k_c : \text{ diffusivity, } k_m, k_t = l^2 f_{m,t}(Ri) \left| \frac{\partial U}{\partial z} \right|$$

### 3.2 Nonlocal PBL

$$\frac{\partial c}{\partial t} = \frac{\partial}{\partial z} \left( k_c \left( \frac{\partial c}{\partial z} - \gamma_c \right) \right)$$

$$k_{zm} = k w_s z \left( 1 - \frac{z}{h} \right)^p$$

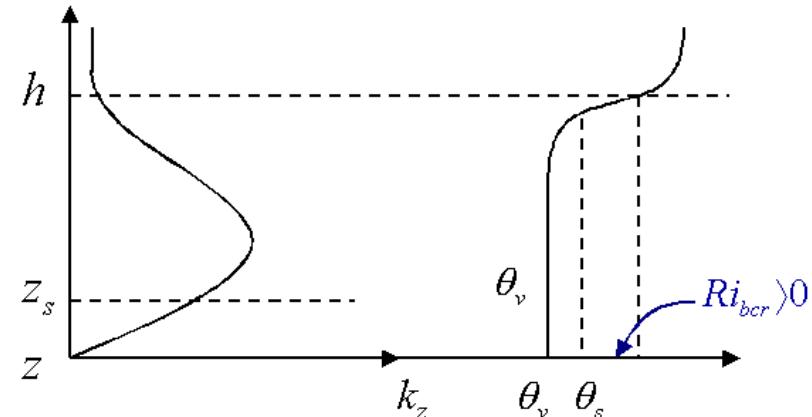
$$h = R_{ibcr} \frac{\theta_m}{g} \frac{U^2(h)}{(\theta_v(h) - \theta_s)}$$

$$\theta_s = \theta_{va} + \theta_T \quad (= b \frac{(\theta_v' w')_0}{w_s})$$

$$p_r = \left[ \frac{\phi_t}{\phi_m} + b k \frac{0.1 h}{h} \right]$$

$$w_s = u_* \phi_m^{-1}$$

Local Richardson number



### 3.3 TKE (Turbulent Kinetic Energy)

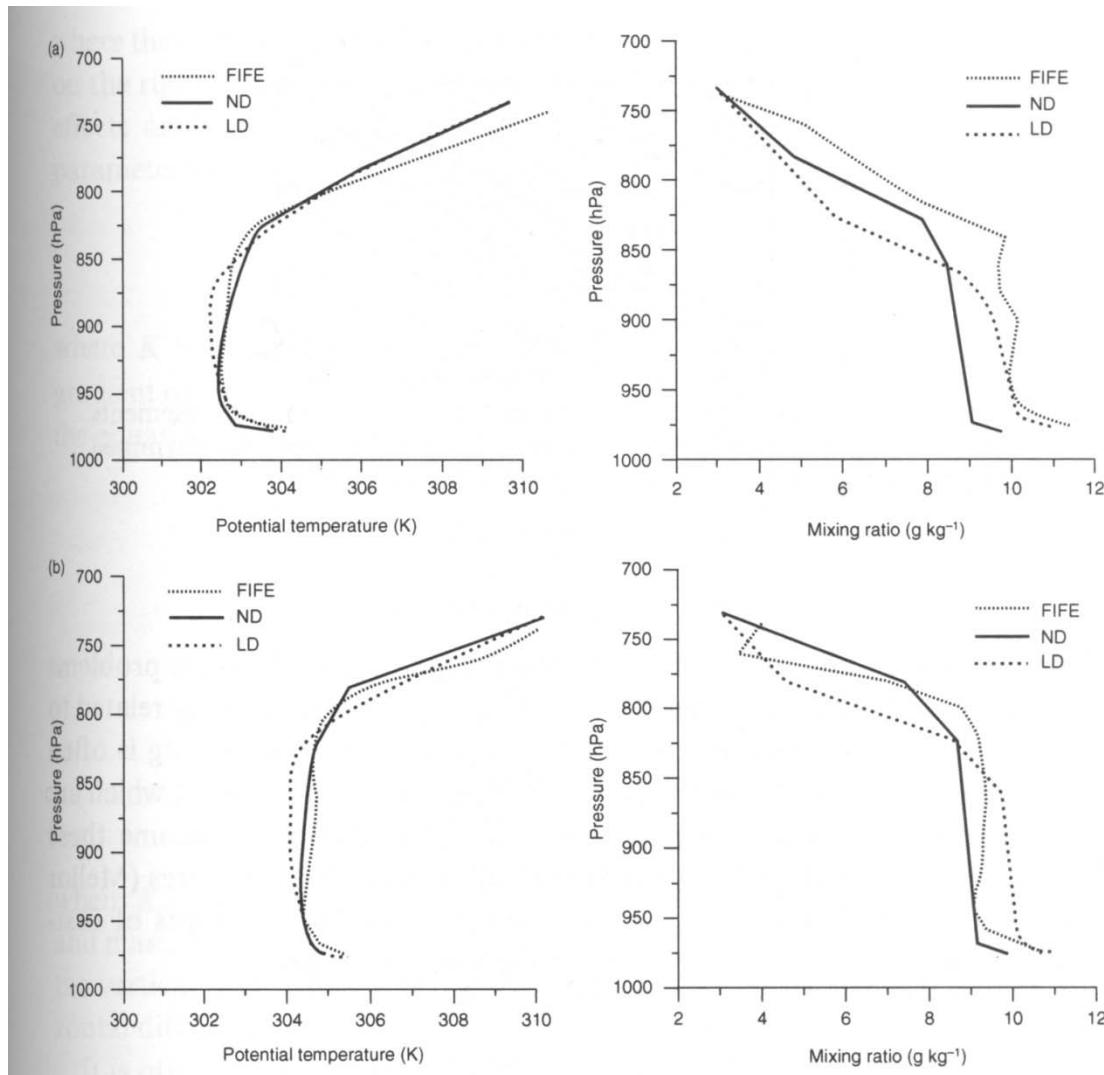
TKE eqn.

$$\frac{\partial \overline{u_i u_j}}{\partial t} + u_j \frac{\partial \overline{u_i u_j}}{\partial x_j} = - \frac{\partial}{\partial x_k} [\overline{u_i u_j u_k} + \frac{1}{\rho} \dots]$$

$$\rightarrow \overline{u_i u_j} \rightarrow k_z = fn(\overline{e_{ij}})$$

(Mellor & Yamada, 1982)

## From Hong and Pan (1996)



Local scheme  
typically produces  
unstable mixed layer

## 4. Gravity Wave Drag

- \* **GWDO : GWD induced by orography**
- \* **GWDC : GWD induced by convection**

### 4.1 Concept

This scheme includes the effect of mountain induced gravity wave drag from sub-grid scale orography including convective breaking, shear breaking and the presence of critical levels. Effects are strong in the presence of strong vertical wind shear and thermally stable layer.

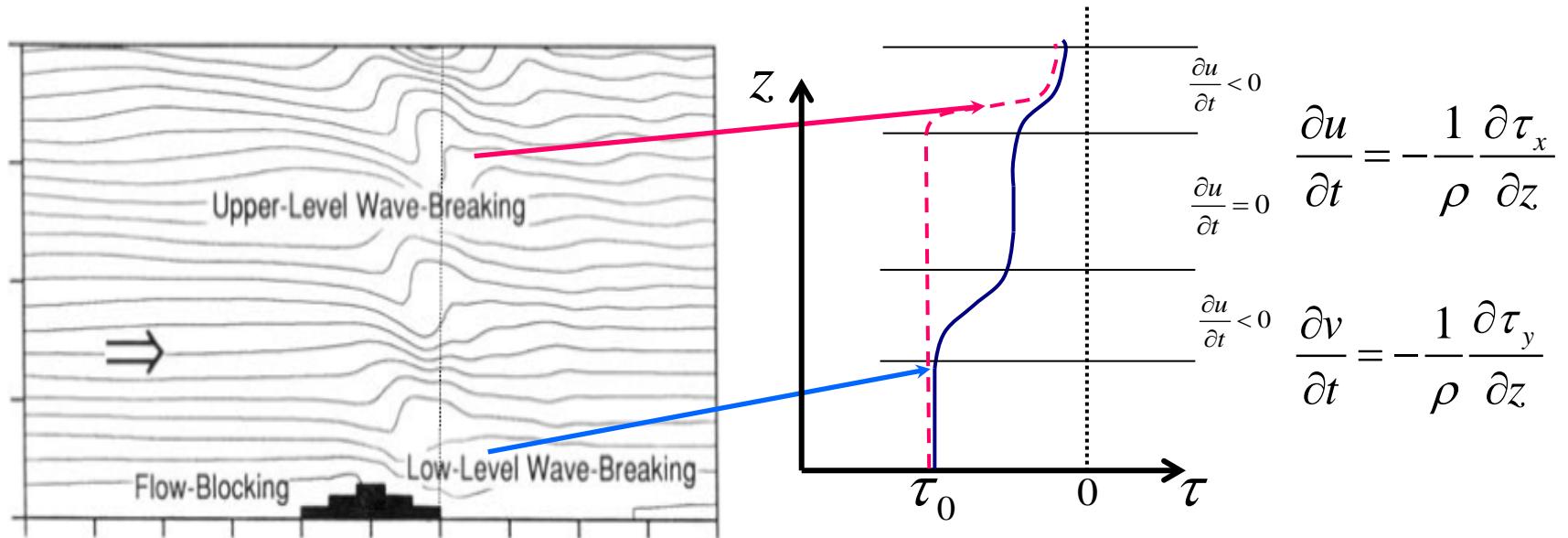
- Wave drag amount at reference level :

$$\tau_{GWD} = -E \frac{m}{\Delta x} \frac{\rho_0 U_0^3}{N_0} \frac{Fr^2}{Fr^2 + C_G / OC} \quad E \equiv (OA + 2) C_E Fr_0 / Fr_c$$

**Conventional** : the conventional Ri number-based wave- breaking mechanism using the saturation hypothesis, which works mainly in the upper atmosphere

**Advanced**: the new orographic statistics-based wave- breaking mechanism using half-theory (Scorer parameter  $\sim BVF^{**2} / U^{**2}$ ) and half-empiricism obtained from mesoscale mountain wave simulations, which works mainly in the lower atmosphere. **Flow blocking is also introduced recently.**

## 4.2 Enhanced lower tropospheric gravity wave drag (Kim and Arakawa 1995)



**Stress at reference level**

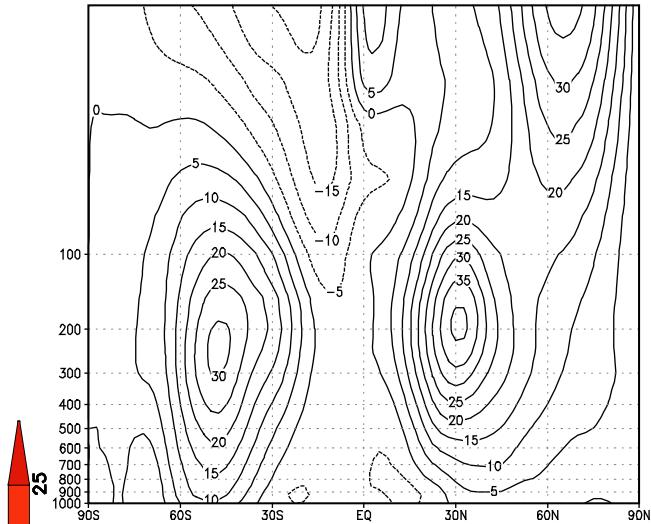
$$\tau_0 = -E \frac{1}{\Delta x} \frac{\rho_0 U_0^3}{N_0} \frac{Fr^2}{Fr^2 + 0.5/OC}, \quad U_0 = \frac{1}{h} \int_{k=1}^{k=k_{pbl}} U dz$$

**Reference level (KA95) : Max (2, KPBL)**

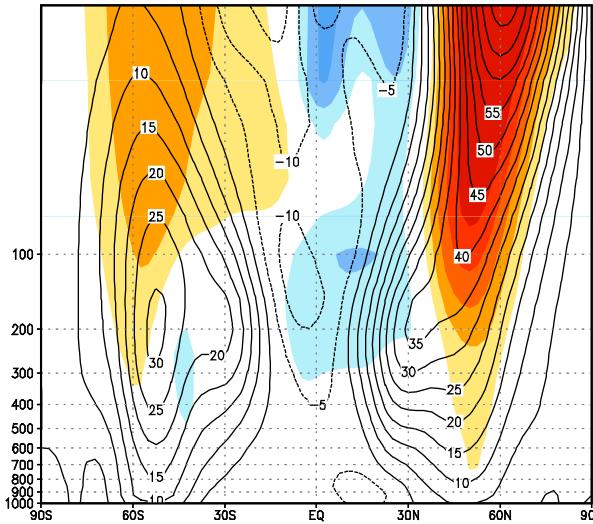
## 4.3 Impact of GWDO

### Zonal-averaged zonal wind (96/97 DJF)

RA2

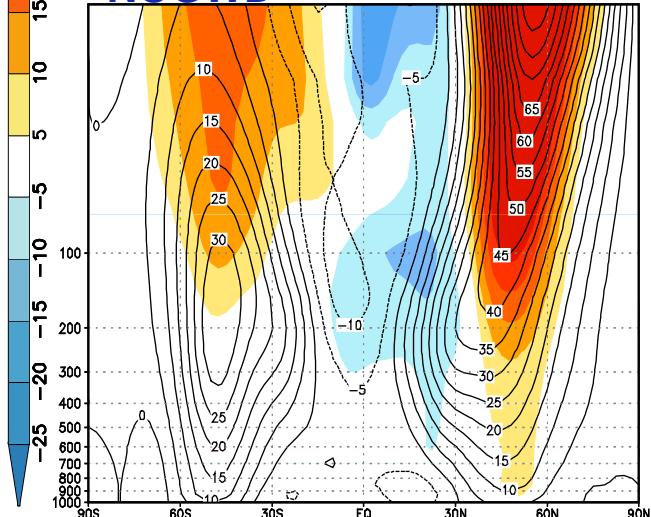


GWD-KA

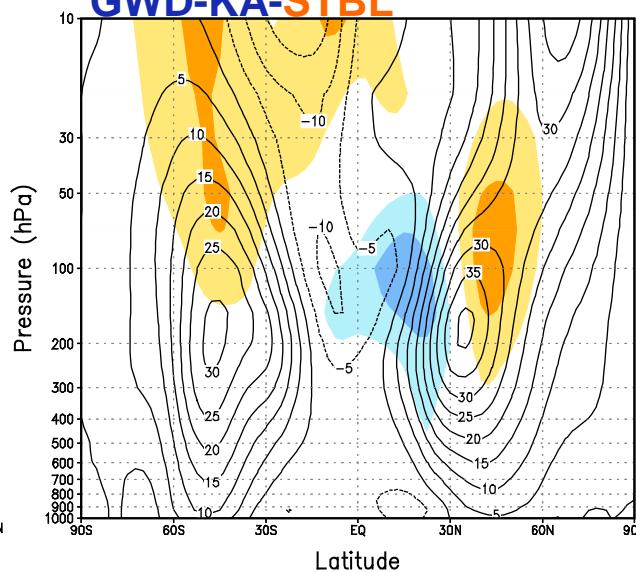


Contour : Zonal averaged  
zonal wind  
Shaded: Deviations from  
the RA2

NOGWD



GWD-KA-STBL



Kim and Arakawa  
→Improves upper level jets  
→Improves the sea level  
pressure

(Kim and Hong, 2009)

# Parameterizations of Convective GW Drag (CWDC)

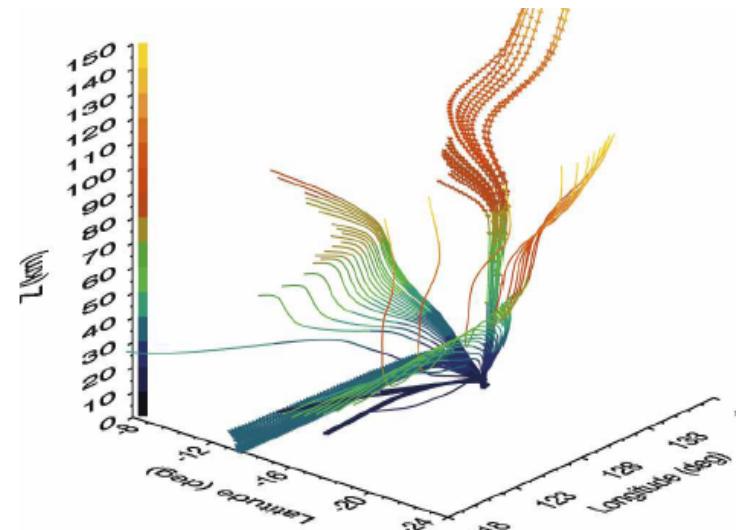
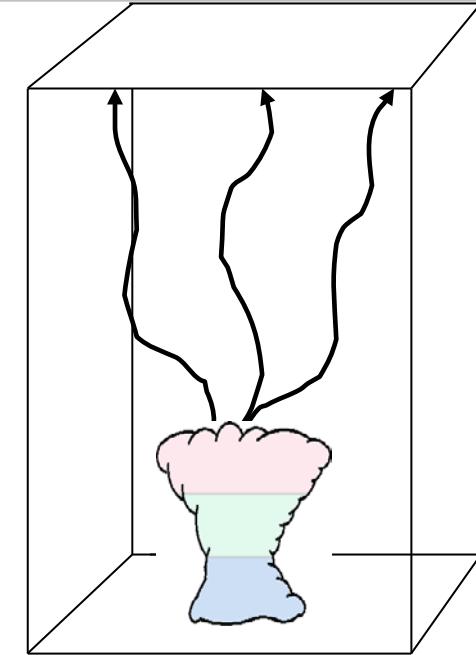
## Columnar CGWD parameterizations

- **Chun and Baik (1998, 2002):** The momentum flux spectrum for the CGWD parameterization was first analytically formulated
- **Chun et al. (2008):** A nonlinear source effect was included in the CGWD parameterization of Song and Chun (2005) that had taken account of a diabatic source alone

## Ray-based CGWD parameterization

- **Song and Chun (2008):** GW propagation properties were explicitly calculated and a three-dimensional propagation of GWs was realistically represented
- **Choi and Chun (2011):** Two free parameters, the moving speed of the convective source and wave-propagation direction, were determined

Prof. Chun, Hye-Young,  
[chunhy@yonsei.ac.kr](mailto:chunhy@yonsei.ac.kr)



# Cloud-top GW Momentum Flux Spectrum

## ■ Cloud-top GW momentum flux spectrum

Song and Chun (2005, JAS)

$$M_{ct}(c, \varphi, z_{ct}) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left( \frac{g}{c_p T_{ct} N_q^2} \right)^2 \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi)$$

✓  $c$  : phase speed (-100 m/s ~ 100 m/s, dc = 2 m/s)

✓  $\varphi$  : wave-propagation direction ( $0^\circ \leq \varphi < 180^\circ$ )

[ $\varphi = 0^\circ, 90^\circ$  in Song et al. 2007; Chun et al. 2008; Song and Chun 2008,

$\varphi = 45^\circ, 135^\circ$  in Choi and Chun 2011]

WFRF	Source

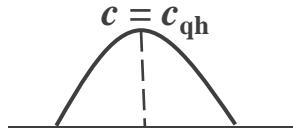
## ■ Wave-filtering-and-resonance-factor (WFRF)

✓ Wave filtering by the vertical propagation condition

✓ Resonance between the vertical harmonics consisting of convective source and natural wave modes with the vertical wave numbers given by the dispersion relation of internal GWs

## ■ Convective source spectrum

$$\Theta(c, \varphi) = q_0^2 \left( \frac{\delta_h \delta_t}{32\pi^{3/2}} \right)^2 \frac{1}{\sqrt{1 + (c - c_{qh})^2 / c_0^2}},$$



✓  $\delta_h, \delta_t$ : spatial and time scales of the convective source (= 5 km, 20 min),  $c_o = \delta_h / \delta_t$

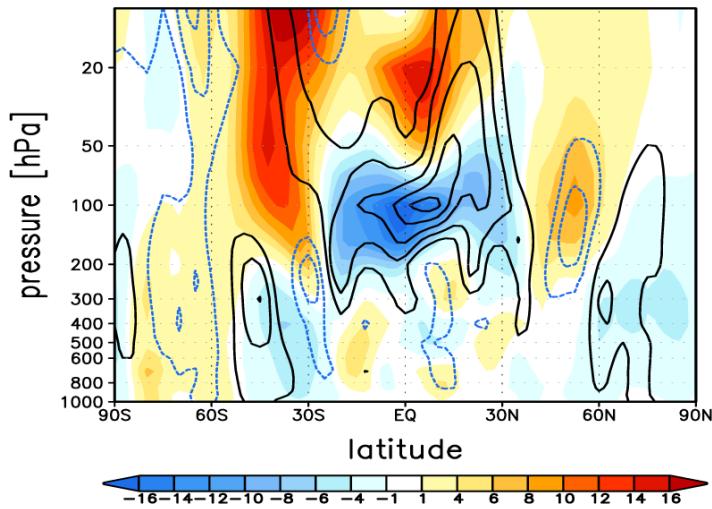
✓  $c_{qh}$  : moving speed of the convective source ( $= c_{qx} \cos \varphi + c_{qy} \sin \varphi$ )

[ $c_{qh}(\varphi) = (\bar{u}_{CL} - \bar{u}_{LL}) \cos \varphi + (\bar{v}_{CL} - \bar{v}_{LL}) \sin \varphi$  (Corfidi et al. 1996) in the original parameterizations

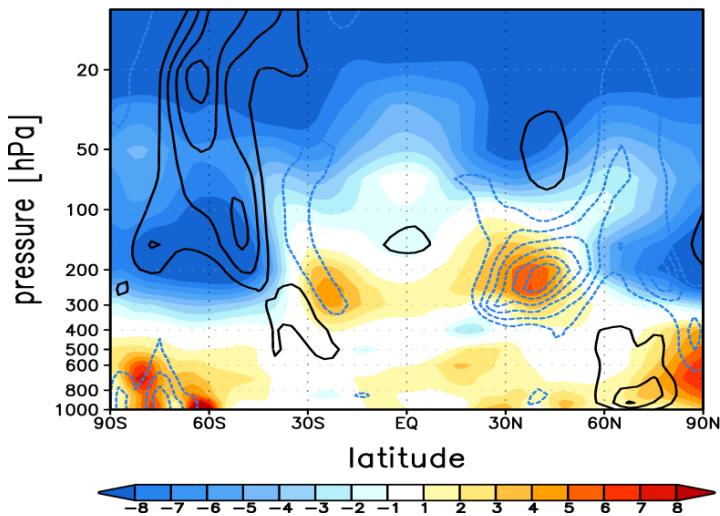
$c_{qh}(\varphi) = \bar{u}_{700} \cos \varphi + \bar{v}_{700} \sin \varphi$  in Choi and Chun (2011)]

# Improvement by GWDC

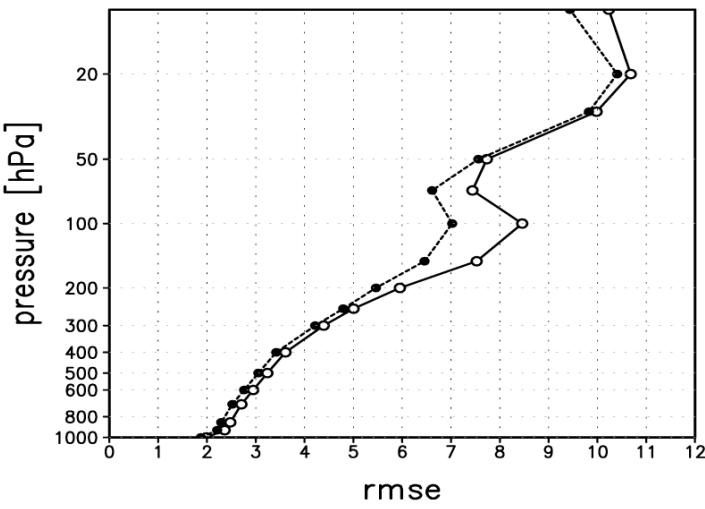
a) SAS\_CB98 Zonal wind difference



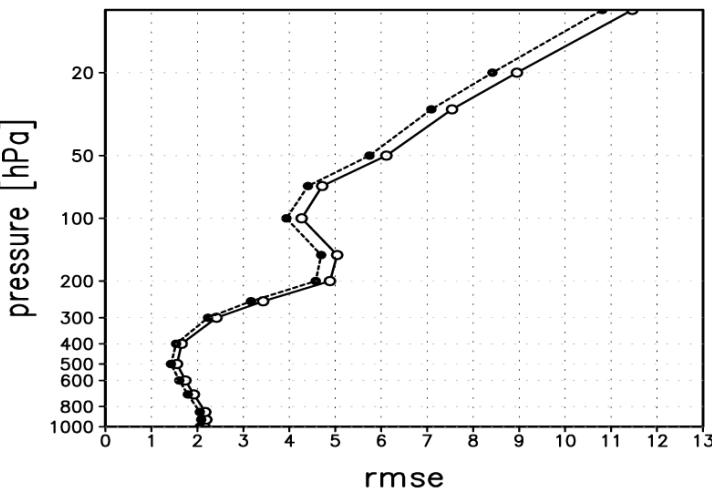
a) SAS\_CB98 Temperature difference



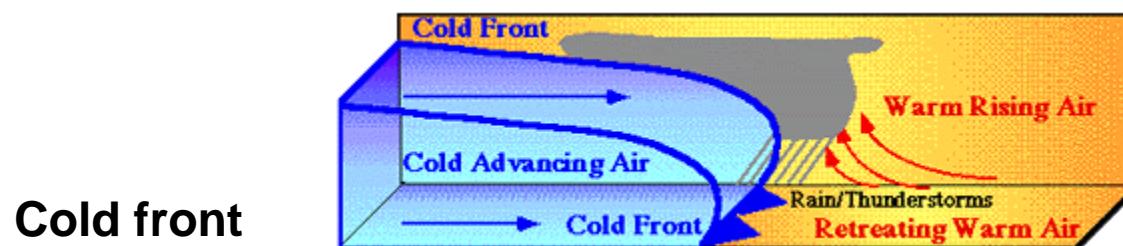
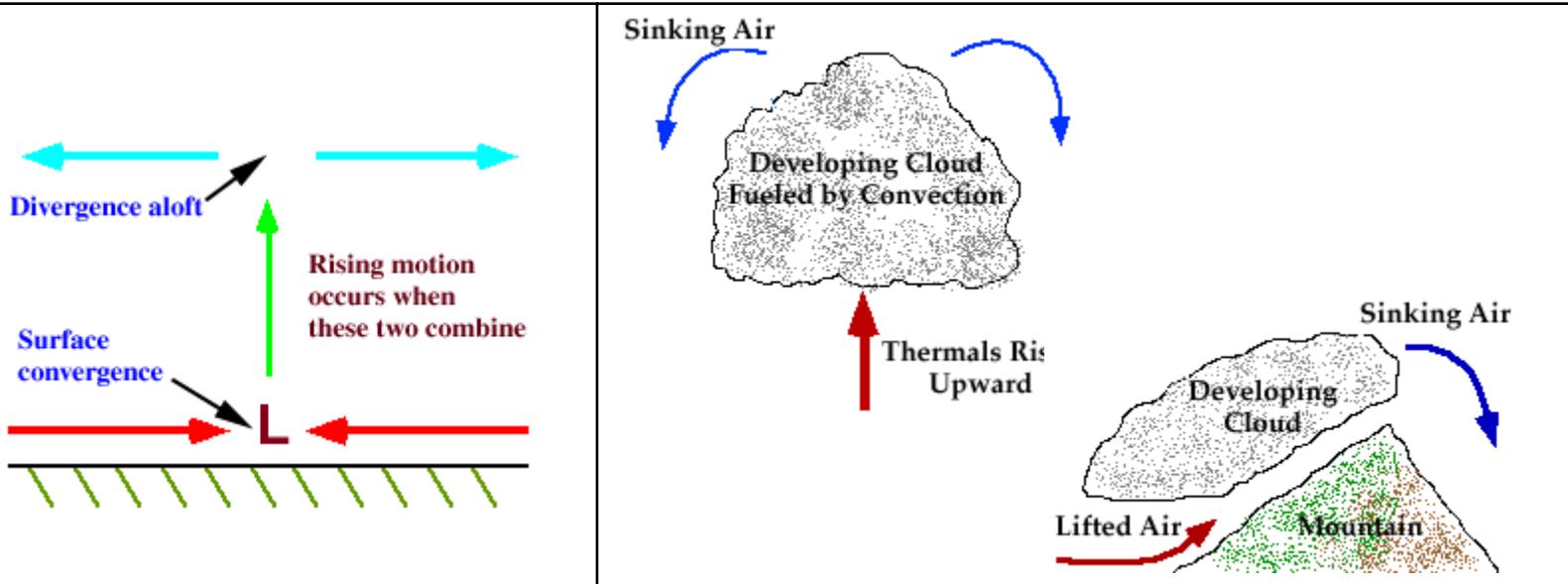
c)



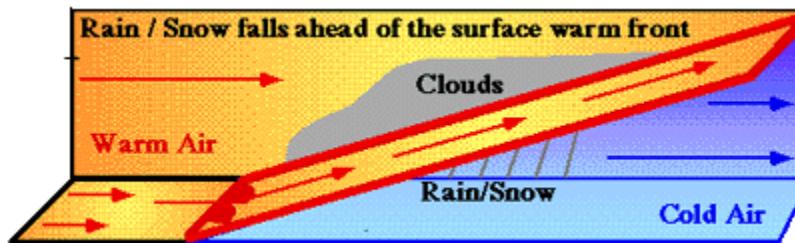
b)



# \* Precipitation Processes: Introduction



Cold front



Warm front

# Precipitation algorithms (CPS and MPS)

In real atmosphere, dynamical motion  $\rightarrow$  RH  $> 1 \Rightarrow$  clouds form  $\rightarrow$  produces rain

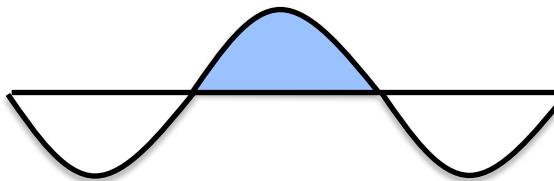
In modeled atmosphere, RH  $< 1$

But generate clouds by releasing CAPE  $\rightarrow$  requires parameterized precip. process

Deep convection : 1~10km



$$\overline{RH} < 1$$



$$\Delta x \rightarrow 0$$

, more grid-resolvable precipitation



Thus, we need the cumulus parameterization scheme to account for releasing conditional instability due to subgrid scale motion

- Grid-resolvable, explicit, large-scale, cloud, microphysics:  
Supersaturation  $\rightarrow$  clouds
- Subgrid scale, implicit, cumulus parameterization,  
parameterized convection, deep convection:  
Convectively unstable  $\rightarrow$  clouds

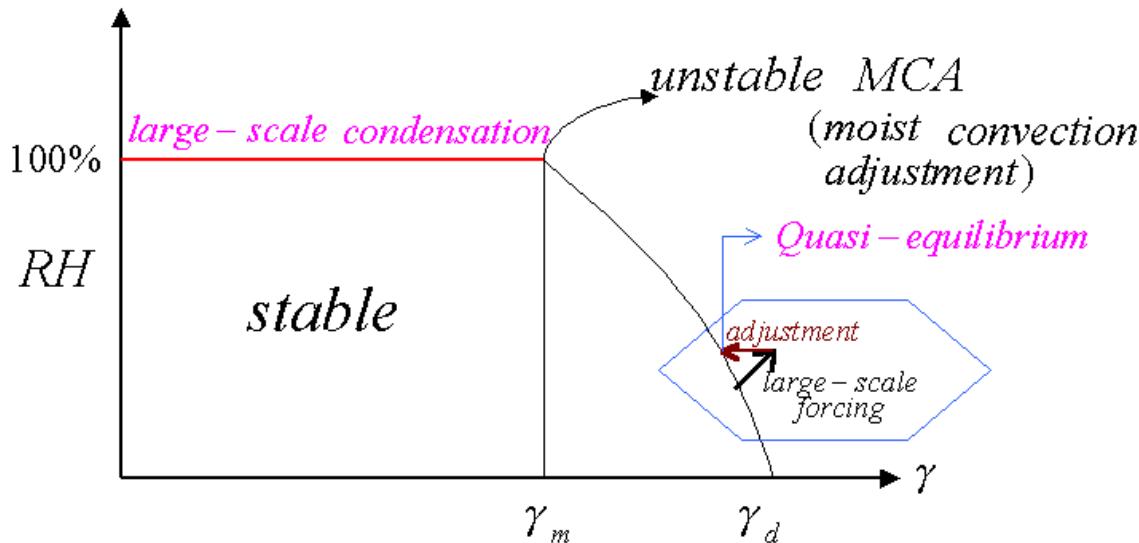
# 5. Deep Convection

Parameterized convection  
Cumulus convection  
Subgridscale precipitation  
Implicit precipitation

## 5.1 Concept

- represents deep precipitating convection and feedback to large-scale
- must formulate the collective effects of subgridscale clouds in terms of the prognostic variable of grid scale

- Closure assumption



## 5.2 Kuo scheme (1965)

$$M_t = -\frac{1}{g} \int_0^{P_s} \nabla \cdot (vq) dp + F_{g_s}$$

$$\int_0^{P_s} \frac{\partial q}{\partial t} dp = gbM_t \quad , \quad b : \text{moistening factor}$$

$$\int_0^{P_s} \theta_c dp = gL(1-b)M_t \quad \frac{\theta_c}{\pi} = \frac{\theta_a - \theta}{\tau} \quad \text{Adjusts to } \gamma_m$$

### - Modified Kuo

- Krishnamurti et al. (1980, 1983)

$$M_t = -\frac{1}{g} \left\{ \int_0^{P_s} \omega \frac{\partial q}{\partial p} dp + F_{q_s} \right\}$$

- Anthes (AK : 1977)

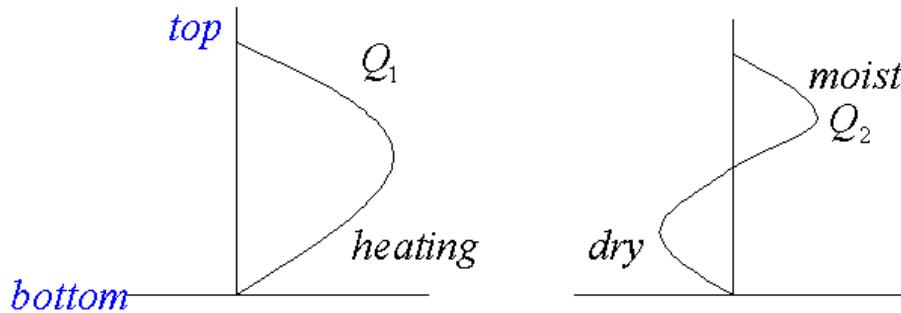
$$b = \left( \frac{1 - RH}{1 - RH_c} \right)^n, \quad \text{Check convective instability}$$

## - Heating and moistening profiles

$$\frac{d\theta}{dt} = \frac{1}{\pi} [gL(1-b)M_t Q_1 + Q_r]$$

$$\frac{dq}{dt} = -g(1-b)M_t Q_2$$

$$\int_0^{P_s} Q_1 dp = \int_0^{P_s} Q_2 dp = 1$$

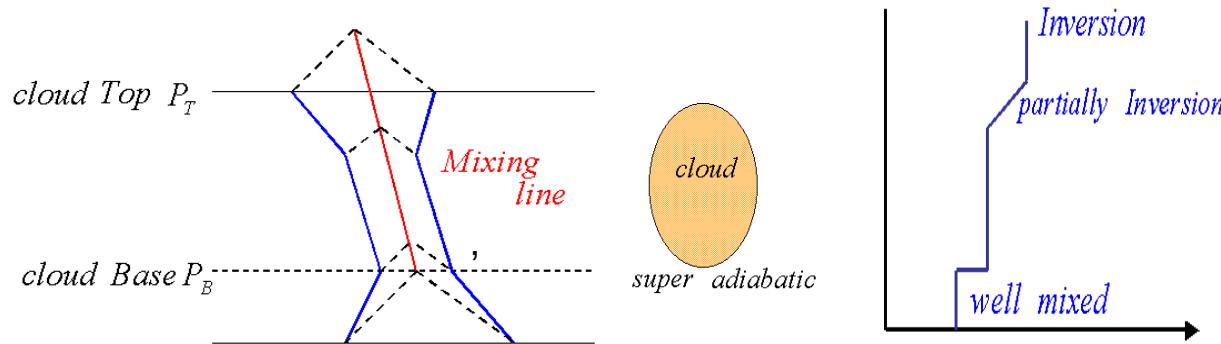


## - Remarks :

Kuo scheme produces NPS. Also, warm bias in the lower troposphere

## 5.3 Betts-Miller scheme (1986)

- Adjust toward reference profiles that are based on observational evidence of convective equilibrium



- Reference profile

$$\theta'_R(P) = \bar{\theta}(P_B) + \beta M_\theta (P - P_B)$$

$$\frac{\partial q}{\partial p} = \beta \left( \frac{\partial q}{\partial p^*} \right)_M \quad \beta = \frac{\partial p^*}{\partial p} \quad p^* : \text{saturation pressure } (= 1.2 \text{ for example})$$

$$M_\theta = 0.85 \left( \frac{\partial \theta^*}{\partial P^*} \right)_M \quad M : \text{Mixing line}$$

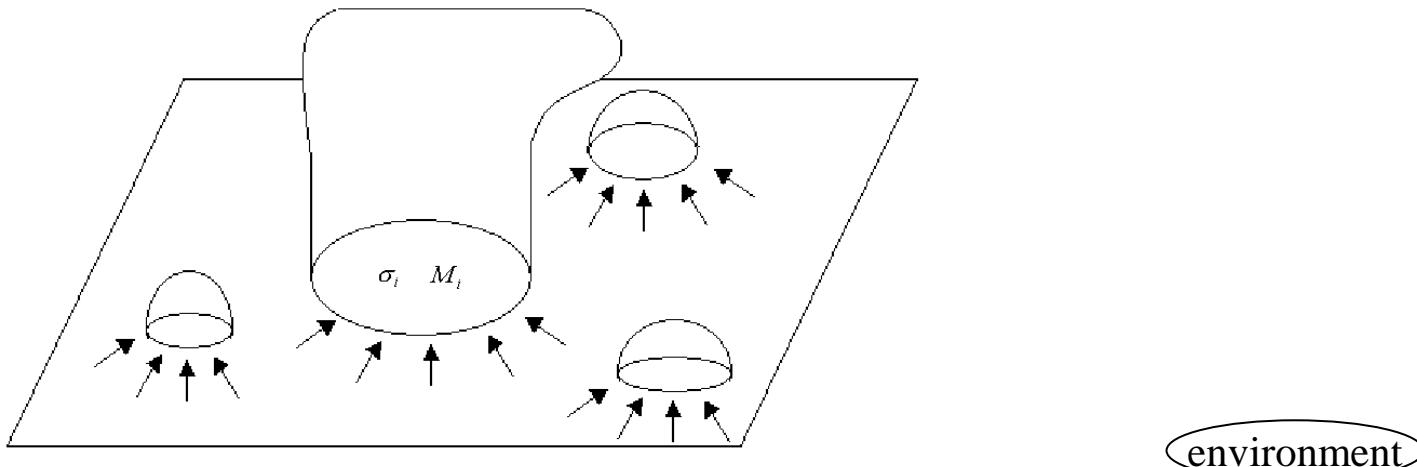
Energy Constraints :  $\int_{P_B}^{P_{T+1}} C_P (T_R - \bar{T}) dp = \int_{P_B}^{P_{T+1}} (q_R - \bar{q}) dp = 0$

## 5.4 Mass-flux schemes : Arakawa-Schubert (1974)

- mass flux approach, quasi-equilibrium

### Theoretical frame work for CPS :

- Area is large enough so that cloud ensemble can be a statistical entity
- Area is small enough so that cloud environment is approximately uniform horizontally



$M_i$  : vertical mass flux through ith cloud

$\sigma_i$  : fractional area covered by ith cloud

$M_c \equiv \sum_i M_i$  : total vertical mass flux

$$\rho \bar{\omega} = M_c + \tilde{M}$$

: net mass flux/unit large-scale horizontal area

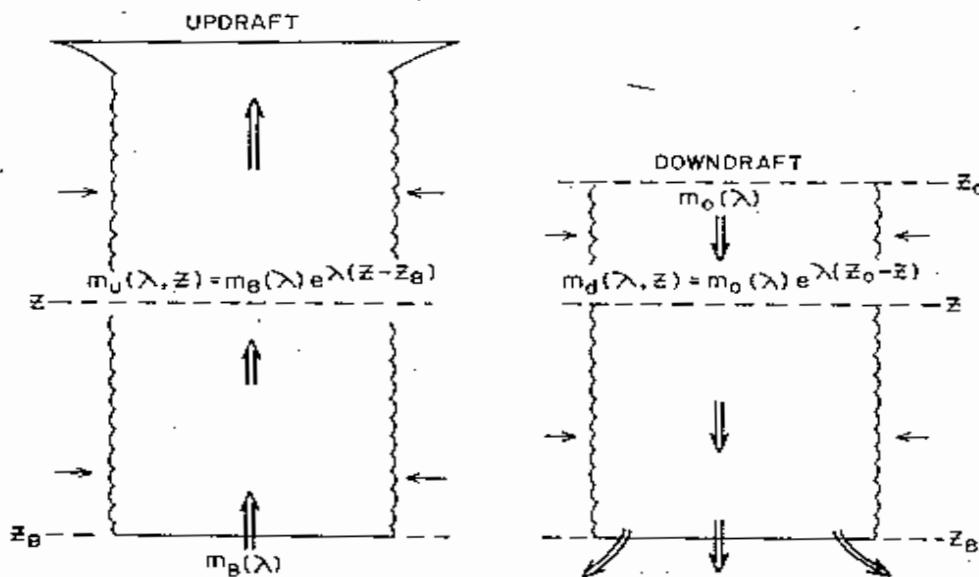
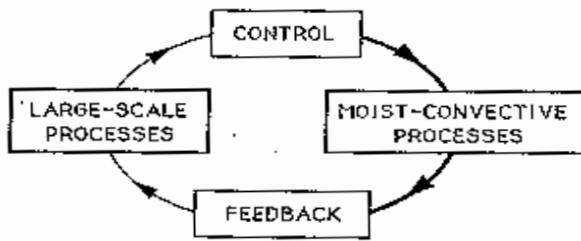


FIG. 4.10. Model for updraft and downdraft of cloud type  $\lambda$  (from Johnson 1976).

- CPS computes the warming (cooling) in the grid box due to adiabatic descent (ascent), rather than computing latent heat releaser in cloud models

Large-scale flux across grid box      Exchange of S between environment and clouds

$$\frac{\partial}{\partial t} \rho (1 - \sigma_c) \tilde{s} = -\bar{\nabla} \cdot (\rho \tilde{V} S) - \frac{\partial}{\partial Z} (\tilde{M} \tilde{S}) - \sum_i \left( \frac{\partial M_i}{\partial Z} + \rho \frac{\partial \sigma_i}{\partial t} \right) S_{ib} - LE + \tilde{Q}_R$$

$$\frac{\partial}{\partial t} \rho \sum_i \sigma_i s_i = -\frac{\partial}{\partial Z} \left( \sum_i M_i s_i \right) + \sum_i \left( \frac{\partial M_i}{\partial Z} + \rho \frac{\partial \sigma_i}{\partial t} \right) S_{ib} + \sum_x (LC_x + Q_{Ri})$$

$S_i : C_p T + gz$  of  $i^{\text{th}}$  cloud

$S_{ib} : C_p T + gz$  of the air entraining into or detrainning from the  $i^{\text{th}}$  cloud

$C_i$  : condensation in the  $i^{\text{th}}$  cloud

$E$  : evaporation of liquid water in the environment

$Q_r$  : Radiational heating

● Entrainment :  $\frac{\partial M_i}{\partial Z} + \rho \frac{\partial \sigma_i}{\partial t} > 0, \quad S_{ib} = \tilde{S}$

● Detrainment :  $\frac{\partial M_i}{\partial Z} + \rho \frac{\partial \sigma_i}{\partial t} < 0, \quad S_{ib} = S_i$

**Assume**  $\sigma_c \ll 1$  ,  $\bar{s} \approx \tilde{s}$

$$\begin{aligned}\frac{\partial}{\partial t} \rho \bar{s} = & -\nabla \cdot (\rho \bar{v} \bar{s}) - \frac{\partial}{\partial z} (\rho \bar{w} \bar{s}) - \overline{\nabla \cdot (\rho \bar{v} \bar{s} - \rho \bar{v} \bar{s})} \\ & + M_c \frac{\partial \bar{s}}{\partial z} - \sum_{dc} \left( \frac{\partial M_i}{\partial z} + \rho \frac{\partial \sigma_i}{\partial t} \right) (\bar{s}_i - \bar{s}) - LE + \widetilde{\theta}_R\end{aligned}$$

dc Detraining clouds      detrainment, entrainment

Adiabatic warming due to hypothetical  
subsidence between the clouds

$$\begin{aligned}\frac{\partial}{\partial t} \rho \bar{q} = & -\nabla \cdot (\rho \bar{v} \bar{q}) - \frac{\partial}{\partial z} (\rho \bar{w} \bar{q}) - \overline{\nabla \cdot (\rho \bar{v} \bar{q} - \rho \bar{v} \bar{q})} \\ & + M_c \frac{\partial \bar{q}}{\partial z} - \sum_{dc} \left( \frac{\partial M_i}{\partial z} + \rho \frac{\partial \sigma_i}{\partial t} \right) (q_i - \bar{q}) - E\end{aligned}$$

## Spectral cloud ensemble

$$M_c(z) = \int_0^{\lambda_{\max}} m(z, \lambda) d\lambda \quad \text{subensemble}$$

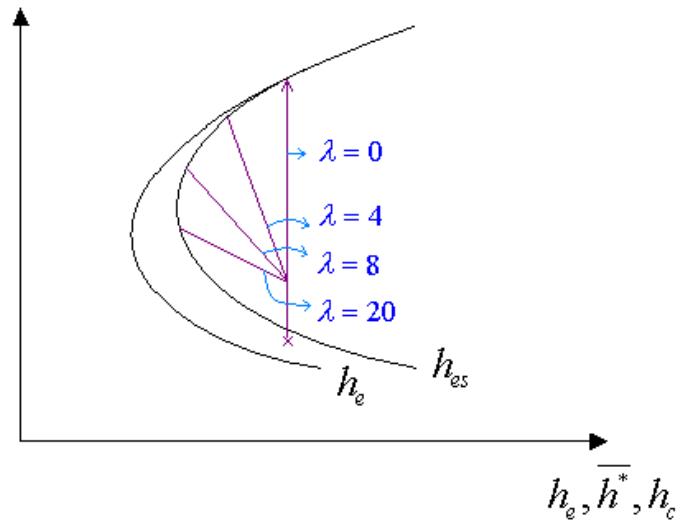
mass flux of between  $\lambda$  and  $d\lambda + \lambda$

$$= \int_0^{\lambda_{\max}} m_B(\lambda) \eta(z, \lambda) d\lambda \quad \text{Mass flux at cloud base}$$

$$\eta(z, \lambda) \equiv \frac{m(z, \lambda)}{m_B(\lambda)} \quad ; \quad \text{normalized subensemble mass flux}$$

$$\frac{\partial m(z, \lambda)}{\partial z} = \mu(z, \lambda) \eta(z, \lambda)$$

$\eta(z, \lambda) = e^{\lambda(z - z_B)}$  ; mass flux profile



## Cloud work function

$$A(\lambda) = \int_{z_B}^{z_D(\lambda)} \eta(z, \lambda) g \frac{T_c(z, \lambda) - \bar{T}(z)}{\bar{T}} dz$$

## Q-G equilibrium

$$\frac{dA(\lambda)}{dt} = \underbrace{\left. \frac{dA(\lambda)}{dt} \right|_{LS}}_{\substack{\text{Large-scale forcing} \\ >0 : \text{destabilized}}} + \underbrace{\left. \frac{dA(\lambda)}{dt} \right|_C}_{\substack{\text{Adjustment} \\ <0 : \text{stabilization}}} = 0$$

Large-scale forcing  
 $>0$  : destabilized      Adjustment  
 $<0$  : stabilization

Kernel : Cloud scheme kinetic energy

$$K_{ij} = \frac{A'_i - A_i}{(m_B \Delta t)}$$

$$\sum_j K_{ij} (m_B \Delta t)_j + F_i = 0$$

$$\Rightarrow m_B$$

→ compute  $\frac{\partial \bar{s}}{\partial t}, \frac{\partial \bar{q}}{\partial t}$  with  $\eta, m_B$

## \* AS type mass flux schemes

Grell scheme (1993) : removes lateral mixing to find the deepest cloud

Simplified AS (SAS, Han and Pan 2011): revised cloud physics from the Grell

Relaxed AS (RAS, Moorthi and Suarez 1992): linearized profile function

## \* Other mass flux schemes : Low-level control convective schemes (Stensrud 2007)

Kain and Fritsch (1993) : CAPE based sophisticated convective plume model

Emanuel (1991) : Stochastic mixing cloud model

Tiedtke (1989) : Large-scale moisture convergence (KUO) based mass flux

Gregory-Rowntree (1990): Parcel buoyancy based turbulence in cloud model

# 6. Shallow Convection

## 1.1 Purpose

more vigorous vertical mixing of  $q$  and  $T$  in the same way as the vertical diffusion with the enhanced turbulence diffusivity within clouds. With the enhanced vertical eddy transport between LCL and inversion level, this process does not allow the excess moisture trapped near the surface in synoptically inactive regions. (non-precipitating convection)

→ Cooling and moistening above LCL and heating and warming below.

## 1.2 Classification

- Moist adjustment type : Betts and Miller (1993), Lock et al. (2000), Tiedtke (1983)
- Mass flux type : Kain (2004), Park and Bretherton (2009), Han and Pan (2011)

### Tiedtke (1983)

$$\frac{\partial T}{\partial t} = \frac{1}{\rho} \frac{\partial}{\partial z} \left( \rho K \left[ \frac{\partial T}{\partial z} + \Gamma \right] \right)$$

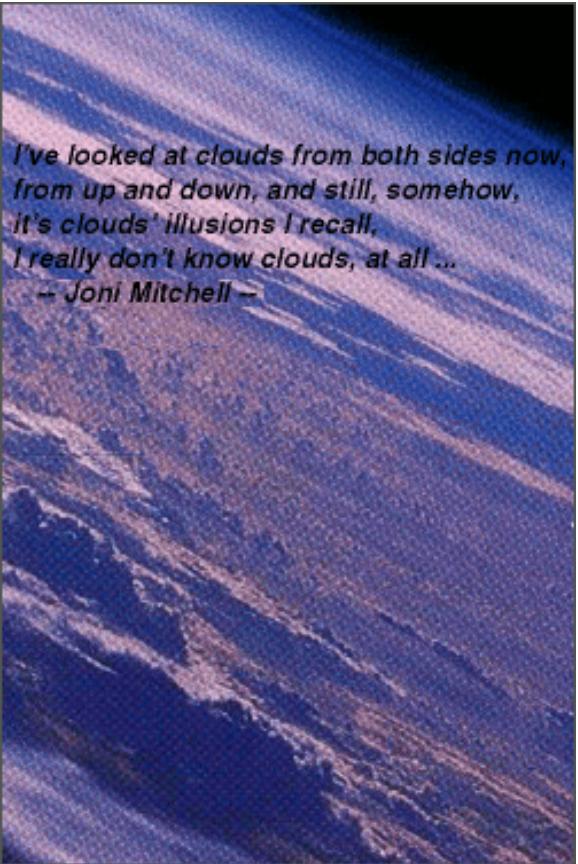
$$\frac{\partial q}{\partial t} = \frac{1}{\rho} \frac{\partial}{\partial z} \left( \rho K \frac{\partial q}{\partial z} \right)$$

### Han and Pan (2011)

$$\frac{1}{\eta} \frac{\partial \eta}{\partial z} = \varepsilon - \delta$$

$$\frac{\partial(\eta s)}{\partial z} = (\varepsilon \bar{s} - \delta s) \eta$$

$$\frac{\partial[\eta(q_v + q_l)]}{\partial z} = \eta[\varepsilon \bar{q}_v - \delta(q_v + q_l) - r]$$



*I've looked at clouds from both sides now,  
from up and down, and still, somehow,  
it's clouds' illusions I recall,  
I really don't know clouds, at all ...*

*-- Joni Mitchell --*

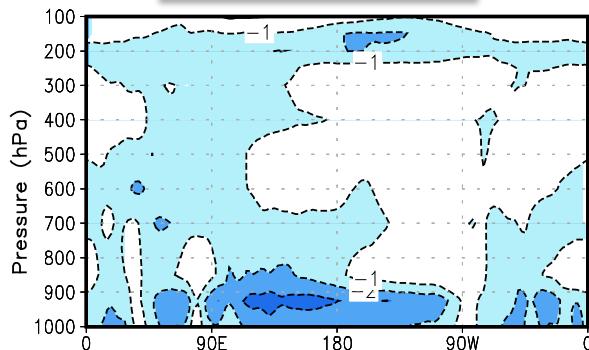


# 1.3 Impact of the shallow convection scheme

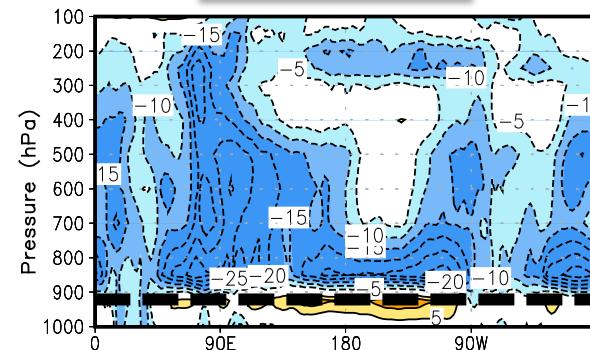
JJA 1996 simulation in a GCM

Temperature

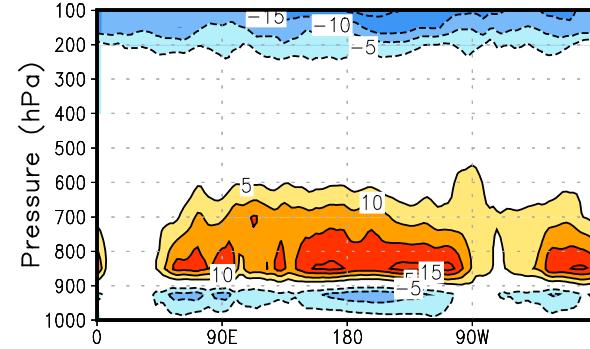
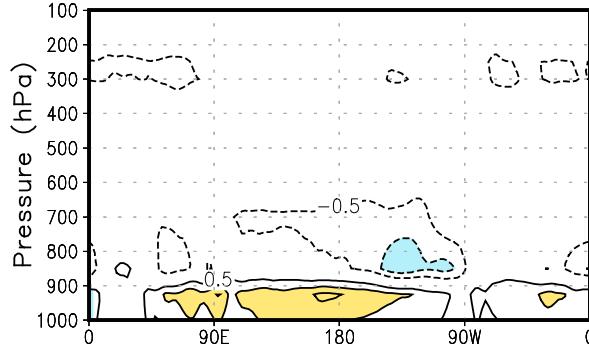
NO – RA2



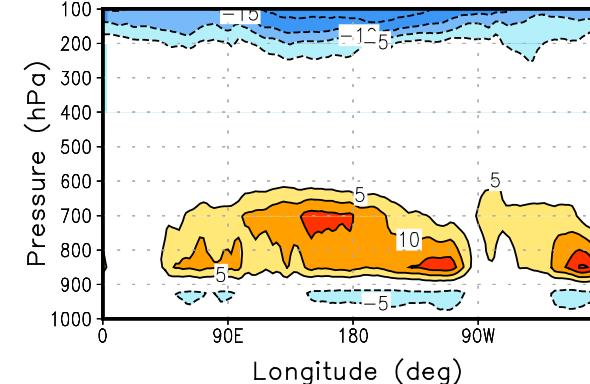
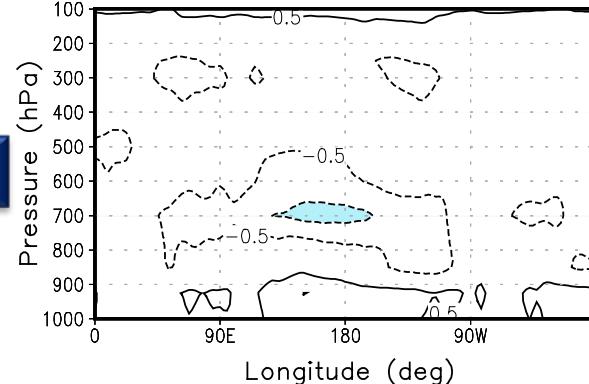
RH



Tiedtke – NO



Han and Pan– NO



# 7. Non-convective Precipitation

large-scale precipitation  
grid-resolvable scale precipitation  
explicit moisture scheme  
cloud scheme  
microphysics scheme

## 7.1 Purpose

Remove supersaturation after deep and shallow convection, and feedback to large-scale

## 7.2 Classification according to the complexity in microphysics

**1) Diagnostic** : condensation, evaporation of falling precipitation

**2) Bulk microphysics :**

hydrometeors with size distribution in inverse-exponential function

- Single moment : predict mixing ratios of hydrometeors
- Double moment : + number concentrations
- Triple moment : + reflectivity

**3) Bin microphysics** : divides the particle distribution into a number of finite size or mass categories.

## 7.3 Precipitate size distributions

Marshall and Palmer(1948) : exponential law  
 Heymsfield and Platt (1984) : Power law

$$N_R(D_R) = a D_R^b$$

The rain and snow particles are assumed to follow the size distribution derived by Marshall and Palmer(1948), and Gunn and Marshall(1958), respectively. The size distributions for both rain and snow are formulated according to an inverse-exponential distribution and its formula for rain can be expressed by

$$N_R(D_R) = N_{0R} \exp(-\lambda_R D_R) \quad A1$$

for rain, where  $N_{0R}$  is the intercept parameter of the rain distributions.

- The slope parameter of the size distributions for rain ( $\lambda_R$ ) is determined by multiplying (A1) by drop mass (A4) and integrating over all diameters and equating the resulting quantities to the appropriate water contents ( $= \rho q_R$ ). This may be written as,

$$\lambda_R = \left( \frac{\pi \rho_w N_{0R}}{\rho q_R} \right)^{1/4} \quad A2$$

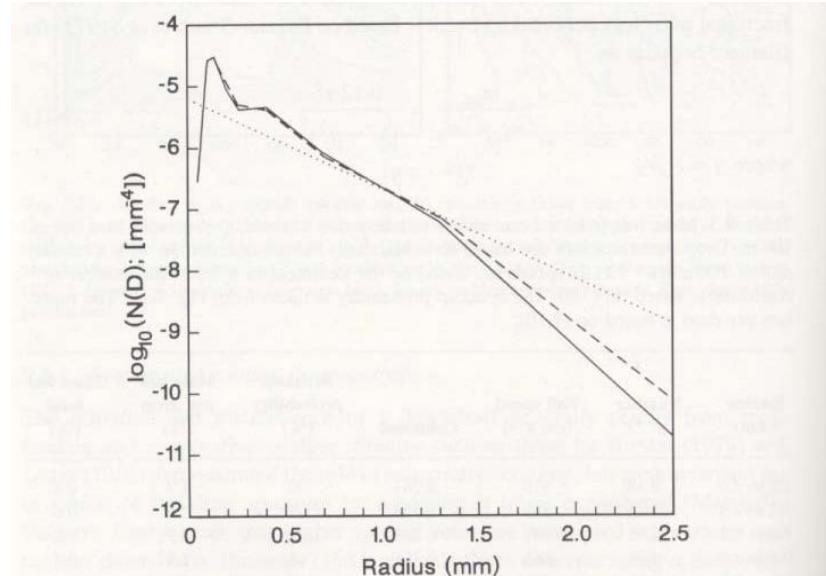


FIG. 9.21. Evolution of a drop spectrum in a subsaturated rainshaft including the effects of coalescence and breakup. The spectrum at the top of the rainshaft is Marshall-Palmer with a rainfall rate of  $110 \text{ mm h}^{-1}$ . (.....), 0 km; (- - -), 1 km; (-), 2 km;  $R = 110 \text{ mm h}^{-1}$ ;  $t = 24 \text{ min}$ . From Tzivion et al. (1989). *Journal of Atmospheric Sciences*, 46, 21. American Meteorological Society. Reproduced with permission

$$\Gamma(x) = \int_0^\infty t^{x-1} \exp(-t) dt$$

$$\begin{aligned} & \int_0^\infty D_R^{4-1} \exp(-\lambda_R D_R) dD_R \\ &= \Gamma(4) / \lambda_R^4 \end{aligned}$$

## 7.4 Bulk Method : 1-Moment versus 2-Moment

Mixing Ratio

(1-moment/ 2-moment scheme)

$$\left( \int \frac{dM(D_R)}{dt} dN_{DR} \right) / \rho = \frac{dq}{dt} (kg kg^{-1} s^{-1})$$

Number concentration  
(2-moment scheme)

$$\left( \int \frac{d \text{Prob}(D_R)}{dt} dN_{DR} \right) = \frac{dN}{dt} (m^{-3} s^{-1})$$

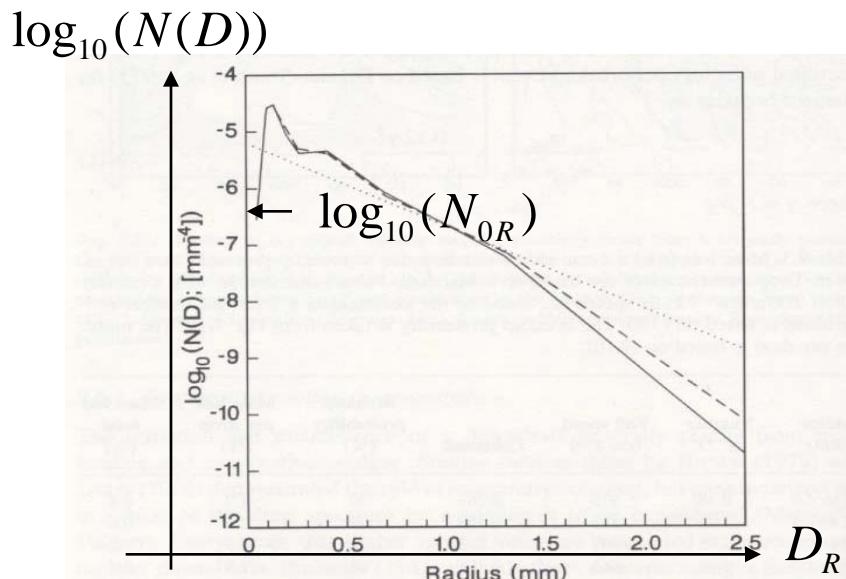


FIG. 9.21. Evolution of a drop spectrum in a subsaturated rainshaft including the effects of coalescence and breakup. The spectrum at the top of the rainshaft is Marshall-Palmer with a rainfall rate of  $110 \text{ mm h}^{-1}$ . (.....), 0 km; (- - -), 1 km; (-), 2 km;  $R = 110 \text{ mm h}^{-1}$ ;  $t = 24 \text{ min}$ . From Tzivivon et al. (1989). *Journal of Atmospheric Sciences*, 46, 21. American Meteorological Society. Reproduced with permission.

**Single moment scheme**

$$dN_{DR} = N_{0R} \exp(-\lambda_R D_R) dD_R$$

**Double moment scheme**

$$dN_{DR} = N_R \lambda_R^2 (N_R) D_R \exp(-\lambda_R D_R) dD_R$$

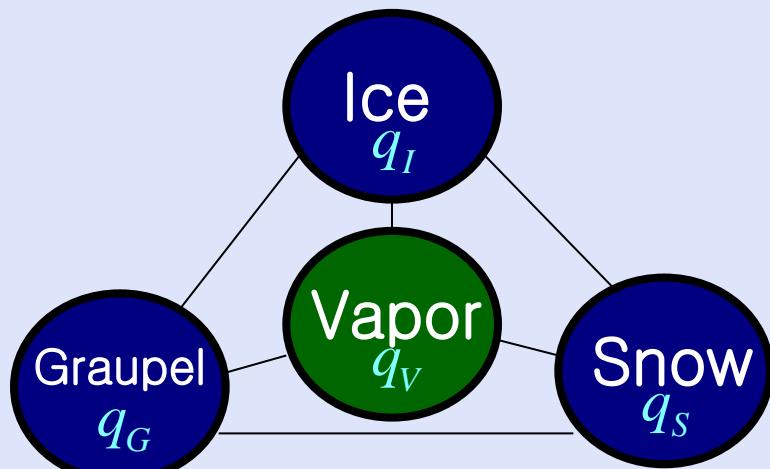
# WSM

# versus

# WDM

Cold rain processes :

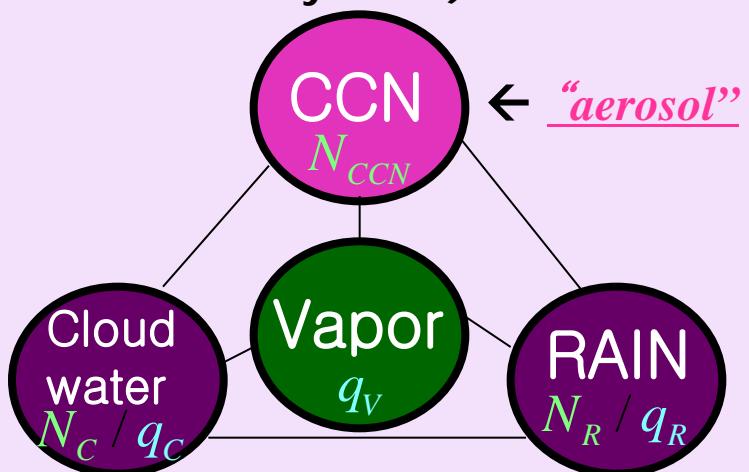
(Hong et al. 2004; Hong and Lim 2006)



$q$  for 4 hydrometeors will be predicted  
(Single Moment)

Warm rain processes :

(Khairoutdinov and Kogan 2000;  
Cohardt and Pinty 2000)



$N, q$  for 2 hydrometeors will be  
predicted (Double Moment)

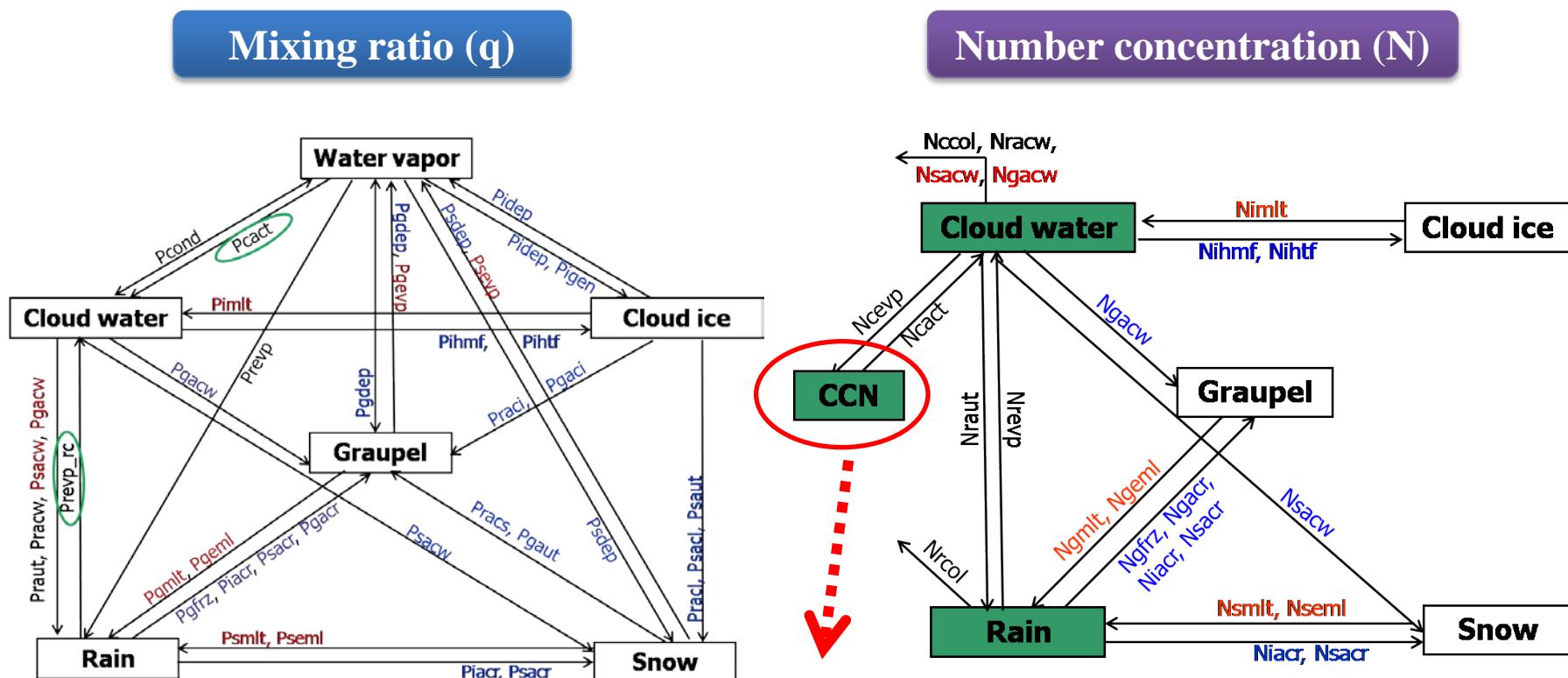
**N**: Cloud water, Rain, CCN

**Q**: Cloud water, Rain, Ice,  
Snow, Graupel, Vapor

**WDM6**

(Lim and Hong, 2010)

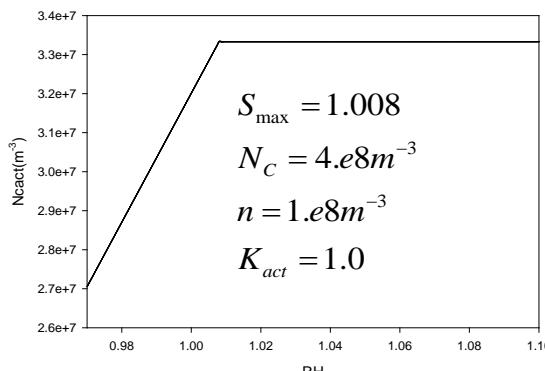
## Flowchart of the source/sink terms ( $S_x$ ) in the WDM6



## [Source/Sink terms for CCN number concentration ]

$$S_{CCN} = -N_{cact} + N_{cevp}$$

$$N_{cact} = \frac{\max \left\{ 0, (n + N_C) \min \left[ 1, (S / S_{\max})^{k_{act}} \right] - N_C \right\}}{\Delta t}$$



# Resolution Dependency

## Cut-off horizontal grid length for parameterizations

- PBL : ~50 m (Mirocha, 2008 WRF workshop )
- GWDO : ~ 3 km (hydrostatic approximation)
- GWDC: ~ 3 km (go with CP)
- Cumulus parameterization : ~ 3 km (Shin and Hong 2009)

- However, recall the past 20 years

### Cut-off horizontal grid length for Cumulus parameterization :

- KMA regional prediction model has been operational without CP even at 80 km until late 1990
- With advances in CP and other physics and initial condition, the cut-off length becomes smaller and smaller
- CP is beneficial even at 4 km (JMA operational model)

**Subgrid-scale parameterization for physics may be necessary even at 1 km or smaller since the finite model grid cannot resolve all the nature explicitly**

## warm rain processes

- follows the double-moment processes in Lim and Hong

```

do k = kts, kte
do i = its, ite
  supsat = max(q(i,k),qmin)-qs(i,k,1)
  satdt = supsat/dtcld

praut: auto conversion rate from cloud to rain [LH 9] [CP 17]
  (QC->QR)

    lencon = 2.7e-2*den(i,k)*qci(i,k,1)*(1.e20/16.*rslope2(i,k)
      *rslope2(i,k)-0.4)
    lenconcr = max(1.2*lencon, qcrmin)
    if(avedia(i,k,1).gt.di15) then
      taucon = 3.7/den(i,k)/qci(i,k,1)/(0.5e6*rslope2(i,k)-7.5)
      praut(i,k) = lencon/taucon
      praut(i,k) = min(max(praut(i,k),0.),qci(i,k,1)/dtcld)

nraut: auto conversion rate from rain to cloud [LH A6] [CP 18 & 19]
  (NC->NR)

  nraut(i,k) = 3.5e9*den(i,k)*praut(i,k)
  if(qrs(i,k,1).gt.lenconcr)
    nraut(i,k) = ncr(i,k,3)/qrs(i,k,1)*praut(i,k)
    nraut(i,k) = min(nraut(i,k),ncr(i,k,2)/dtcld)
  endif

pracw: accretion of cloud water by rain [LH 10] [CP 22 & 23]
  (QC->QR)
nracw: accretion of cloud water by rain [LH A9]
  (NC->)

  if(qrs(i,k,1).ge.lenconcr) then
    if(avedia(i,k,2).ge.di100) then
      nrauw(i,k) = min(ncrk1*ncr(i,k,2)*ncr(i,k,3)*(rslope3(i,k)
        + 24.*rslope3(i,k,1)),ncr(i,k,2)/dtcld)
      pracw(i,k) = min(pi/6.*((denr/den(i,k))*ncrk1*ncr(i,k,2)
        *ncr(i,k,3)*rslope3(i,k)*(2.*rslope3(i,k)
        + 24.*rslope3(i,k,1)),qci(i,k,1)/dtcld)
    else
      nrauw(i,k) = min(ncrk2*ncr(i,k,2)*ncr(i,k,3)*(2.*rslope3(i,k)
        *rslope3(i,k)+5040.*rslope3(i,k,1)
        *rslope3(i,k,1)),ncr(i,k,2)/dtcld)
      pracw(i,k) = min(pi/6.*((denr/den(i,k))*ncrk2*ncr(i,k,2)
        *ncr(i,k,3)*rslope3(i,k)*(6.*rslope3(i,k)
        *rslope3(i,k)+5040.*rslope3(i,k,1)*rslope3(i,k,1))
        ,qci(i,k,1)/dtcld)
    endif
  endif

```

## \*\* Warm rain processes (Hong and Lim 2010)

### \*Auto conversion from cloud to rain [C → R]

$$\text{Praut} [\text{kg kg}^{-1} \text{s}^{-1}] = L / \tau \quad L = 2.7 \times 10^{-2} \rho_a q_c \left( \frac{10^{20}}{16 \lambda_c^4} - 0.4 \right)$$

$$\tau = 3.7 \frac{1}{\rho_a q_c} \left( \frac{0.5 \times 10^6}{\lambda_c} - 7.5 \right)^{-1}$$

$$N_{\text{raut}} [\text{m}^{-3} \text{s}^{-1}] = 3.5 \times 10^9 \frac{\rho_a L}{\tau}$$

### \*Accretion of cloud water by rain [C → R]

$$D_R \geq 100 \mu\text{m}$$

$$\text{Pracw} [\text{kg kg}^{-1} \text{s}^{-1}] = \frac{\pi}{6} \frac{\rho_w}{\rho_a} K_1 \frac{N_C N_R}{\lambda_C^3} \left\{ \frac{2}{\lambda_C^3} + \frac{24}{\lambda_R^3} \right\}$$

$$N_{\text{racw}} [\text{m}^{-3} \text{s}^{-1}] = -K_1 N_C N_R \left\{ \frac{1}{\lambda_C^3} + \frac{24}{\lambda_R^3} \right\}$$

$$D_R < 100 \mu\text{m}$$

$$\text{Pracw} [\text{kg kg}^{-1} \text{s}^{-1}] = \frac{\pi}{6} \frac{\rho_w}{\rho_a} K_2 \frac{N_C N_R}{\lambda_C^3} \left\{ \frac{6}{\lambda_C^6} + \frac{5040}{\lambda_R^6} \right\}$$

$$N_{\text{racw}} [\text{m}^{-3} \text{s}^{-1}] = -K_2 N_C N_R \left\{ \frac{2}{\lambda_C^6} + \frac{5040}{\lambda_R^6} \right\}$$

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# Thank you !

