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Mesoscale &  
Microscale Meteorology @ NCAR

# WRF Variational Data Assimilation System (WRF-Var) Overview

WRF Tutorial Presentation

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## Acknowledge:

NCAR/MMM Division Staff

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US Air Force Weather Agency, Korean Meteorological Administration,  
Taiwanese Central Weather Bureau, Civil Aeronautics Administration,

# Outline of Talk

1. What is WRF-Var?
2. Practical Variational Data Assimilation.
3. The WRF-Var Algorithm.
4. Background Error Modeling.
5. Observational Issues.
6. Current Status and Future Plans.

# 1. What is WRF-Var?

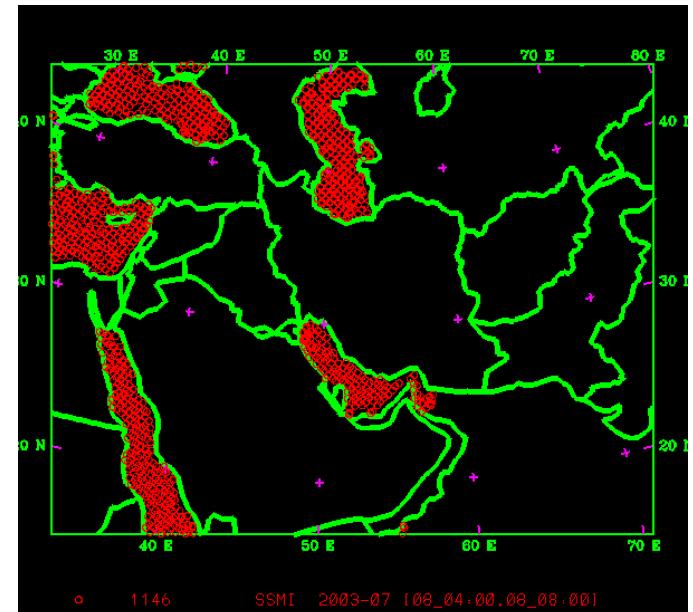
...WRF-Var is a **unified** variational data assimilation system built within the software framework of the Weather Research and Forecasting (WRF) model, used for application in both research and operational environments....



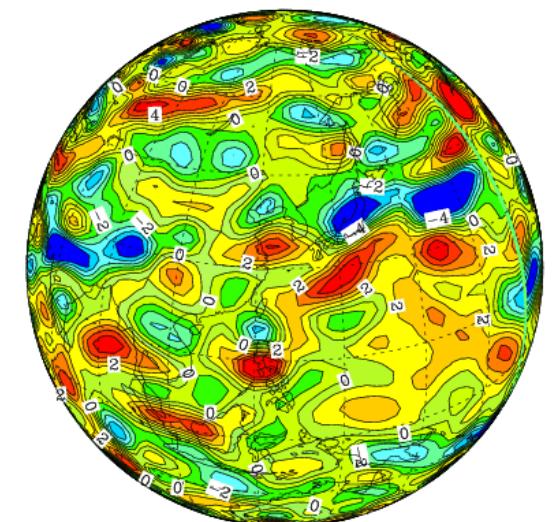
# What Do We Mean By “Unified”

- Regional (worldwide applicability) / global.
- Run-time configurable 3/4D-Var.
- Single code (WRF-Var) for development, release. Supported by NCAR/MMM.
- Embedded within WRF framework.
- Multi-model: WRF/MM5/KMA/NFS/...

AFWA 15km S-W Asia:

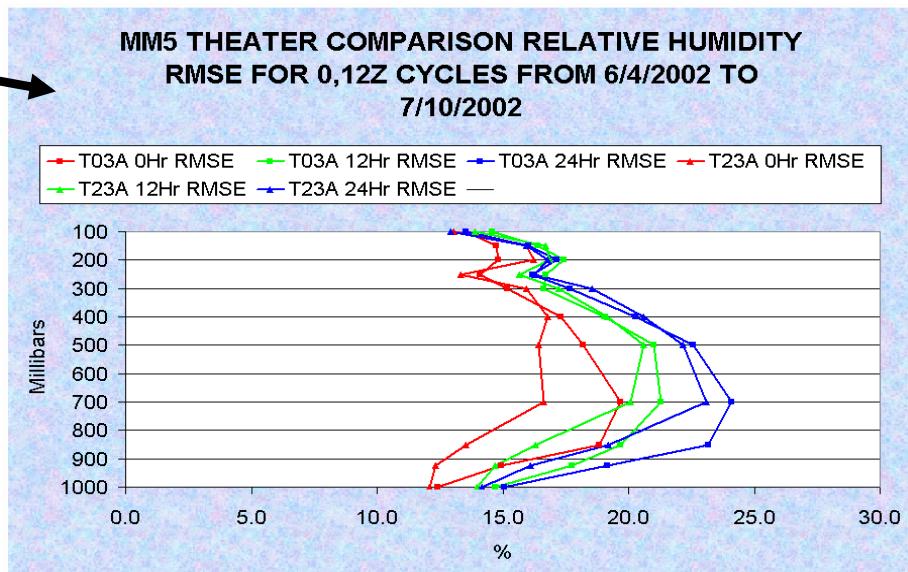
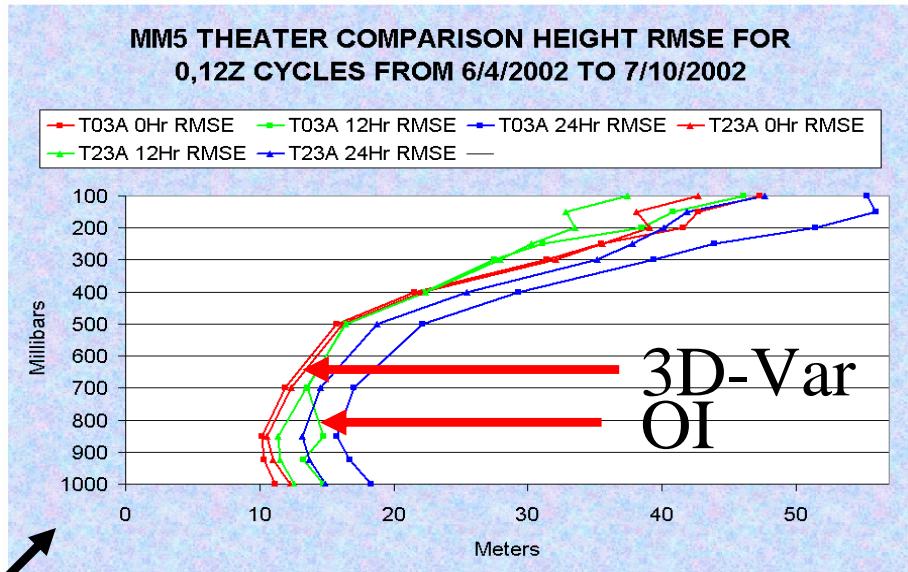


KMA T213 Global:



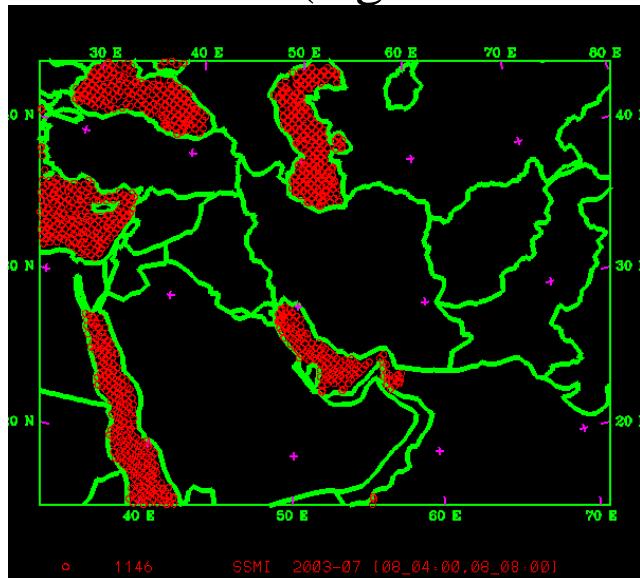
# WRF Variational Data Assimilation (WRF-Var) History

- **Late 1999:** Begin development of MM5 3D-Var.
  - **June 2001:** MM5-3DVar adopted as starting point for WRF 3D-Var.
  - **May 2002:** MM5/WRF 3D-Var operational at Taiwanese CAA.
  - **September 2002:** MM5/WRF 3D-Var operational in 45km domains at AFWA.
  - **June 2003:** WRF 3D-Var V1.0 release.
  - **May 2004:** WRF 3D-Var V2.0 release.
  - **July 2005:** WRF-Var V2.1 release.

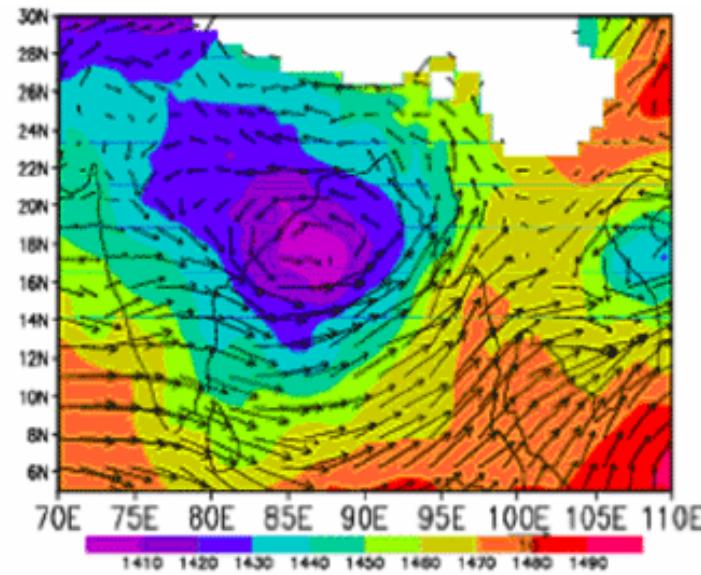


# WRF-Var Operational Applications: June 2005

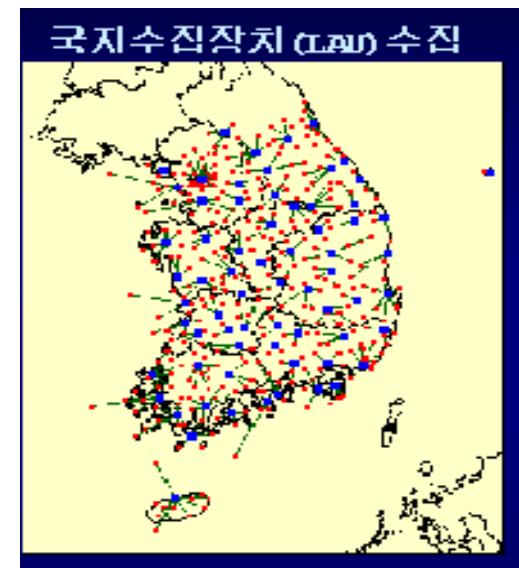
AFWA 15km (e.g. S-W Asia):



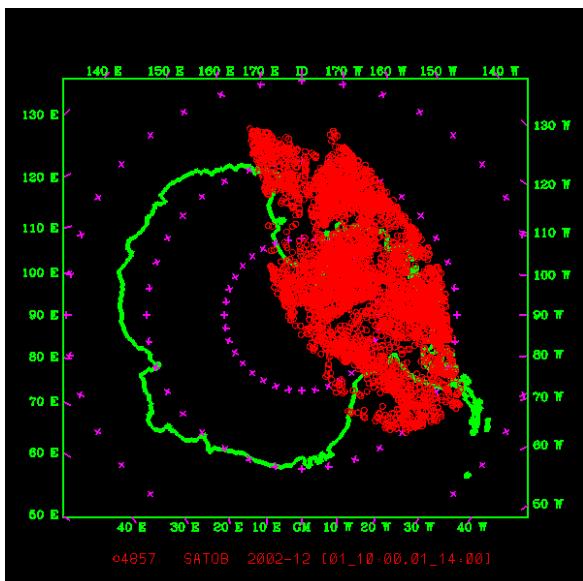
Indian NCMRWF 30km:



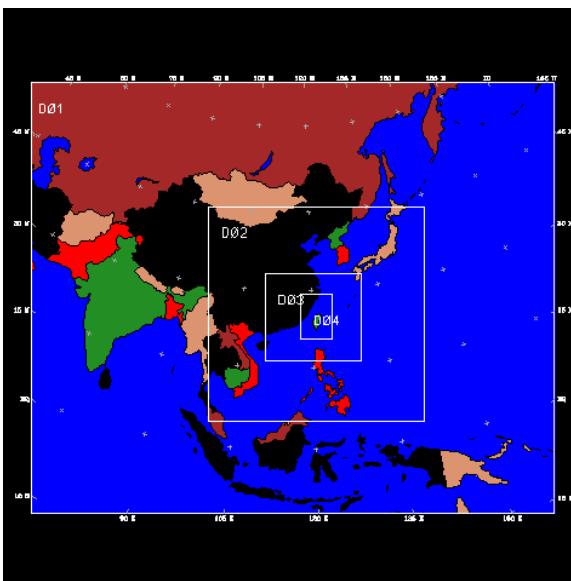
Korean 10km:



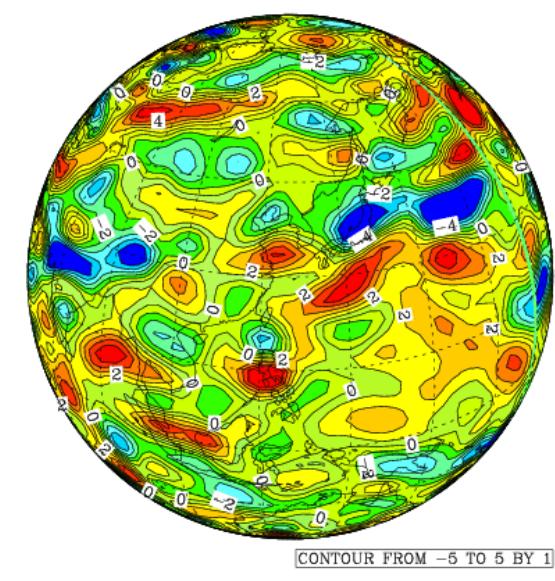
AMPS 30km:



Taiwanese CAA 135/45/15km:



Korean T213/T426:



## 2. Practical Variational Data Assimilation

# Data Assimilation Overview 1

- Assimilation system combines all sources of information:
  - Observations -  $y^o$
  - Background field -  $x^b$
  - Estimate of observation/background errors.
  - Laws of physics.
- Output of the assimilation system is the “analysis”.
- Analysis used in a number of ways:
  - Initial conditions for numerical forecasts.
  - Climatology - reanalyses.
  - Observing system justification (e.g. OSEs, OSSEs).



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# Data Assimilation Overview 2

There are never enough good observations!!

- Consider NWP model:
  - Typical global model –  $425 * 325 * 50 = 6.9$  million gridpoints.
  - Minimum number of prognostic variables =  $6 (u, v, w, T, p, q)$ .
  - Number of degrees of freedom = 41.4 million.
- Typical number of observations = few  $\times 10^6$  but:
  - Inhomogeneous distribution of data.
  - Observations not always in sensitive areas.
  - Observations have errors.
- Solutions:
  - Use sophisticated (variational/ensemble) techniques (can use “exotic” obs).
  - Use previous forecast to propagate obs. info from previous times.
  - Use approximate physical balance relationships.
  - More/better observations!



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# Alternative Formulations of Advanced DA

$$J(\mathbf{x}) = \frac{1}{2} [\mathbf{x} - \mathbf{x}^b]^T \mathbf{P}_b^{-1} [\mathbf{x} - \mathbf{x}^b] + \frac{1}{2} [\mathbf{y} - H(\mathbf{x})]^T \mathbf{R}^{-1} [\mathbf{y} - H(\mathbf{x})]$$

- Minimization implies gradient of cost function is zero. Leads to **information** or **analysis space** formulation (applied in ECMWF, Met. Office, HIRLAM, etc...):

$$\mathbf{x}^a - \mathbf{x}^b = [\mathbf{H}^T \mathbf{R}^{-1} \mathbf{H} + \mathbf{P}_b^{-1}]^{-1} \mathbf{H}^T \mathbf{R}^{-1} [\mathbf{y} - H(\mathbf{x}^b)]$$

- Alternatively, application of the “Sherman-Morrison-Woodbury” formula leads to the **error** or **observation** space formulation (NAVDAS, PSAS):

$$\mathbf{x}^a - \mathbf{x}^b = \mathbf{P}_b \mathbf{H}^T [\mathbf{H} \mathbf{P}_b \mathbf{H}^T + \mathbf{R}^{-1}]^{-1} [\mathbf{y} - H(\mathbf{x}^b)]$$

- Both can be written in terms of a “Kalman Gain”  $\mathbf{K}$

$$\mathbf{x}^a - \mathbf{x}^b = \mathbf{K} [\mathbf{y} - H(\mathbf{x}^b)]$$

Good reference: NAVDAS Source Book (Daley and Barker, 2001, NRL)



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# Variational Data Assimilation

- **Variational** analysis  $x^a$  is minimum  $x$  of cost-function  $J = -\ln (P(x))$
- Assume error probability  $P(x)$  is Gaussian then

$$J(x) = J_b + J_o = \frac{1}{2} [x - x^b]^T P_b^{-1} [x - x^b] + \frac{1}{2} [y - H(x)]^T R^{-1} [y - H(x)]$$

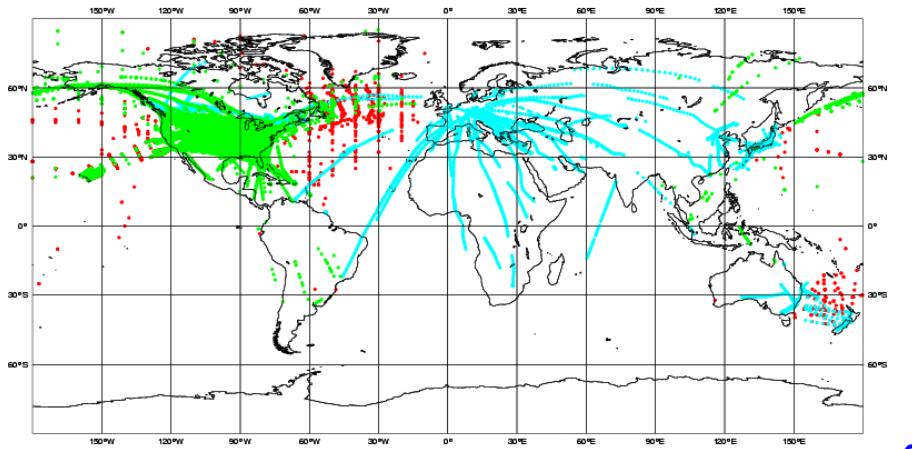
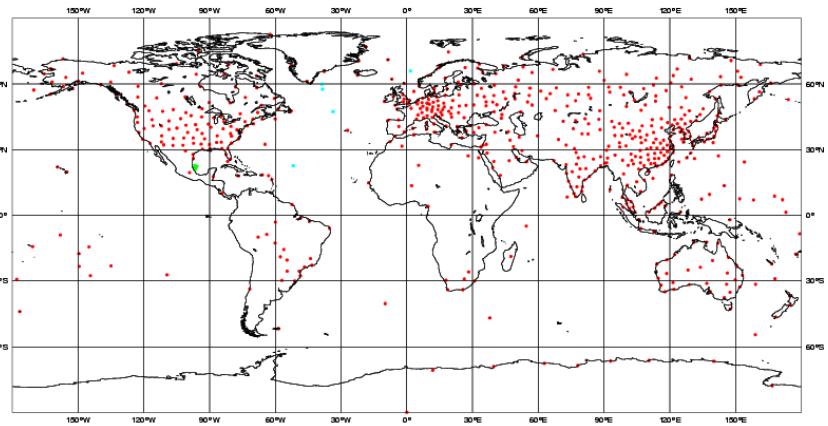
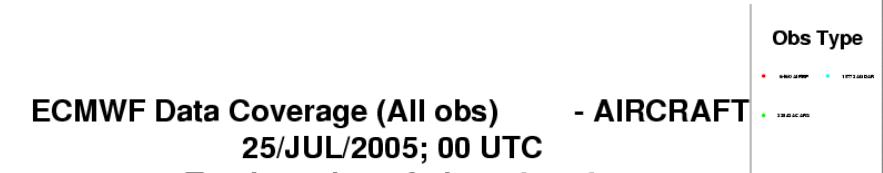
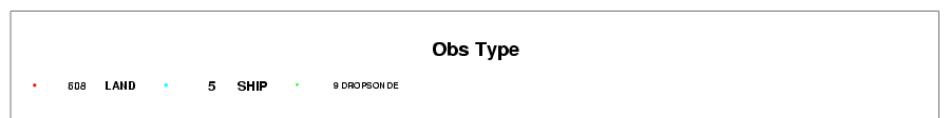
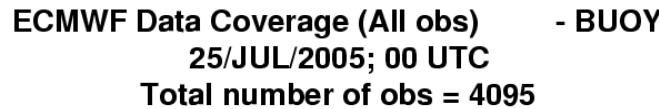
- $x^b$  is the *background*.  $H$  is the (possibly nonlinear) *observation operator*.
- **Error covariances:**

$P_b$  = Background (previous forecast) error covariance matrix.

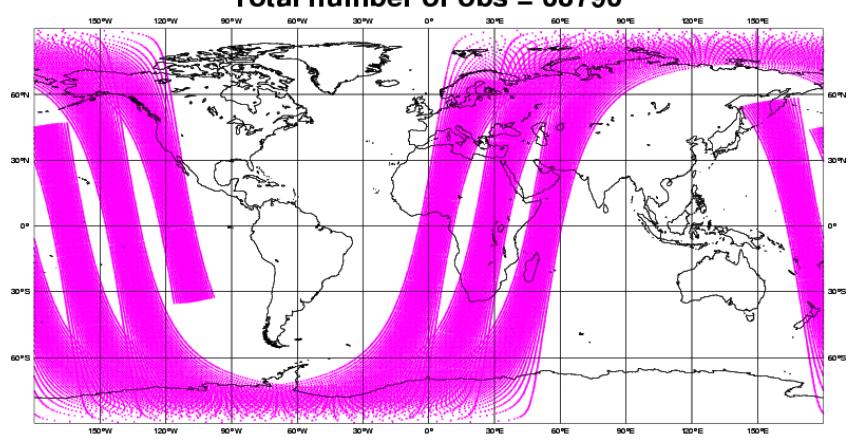
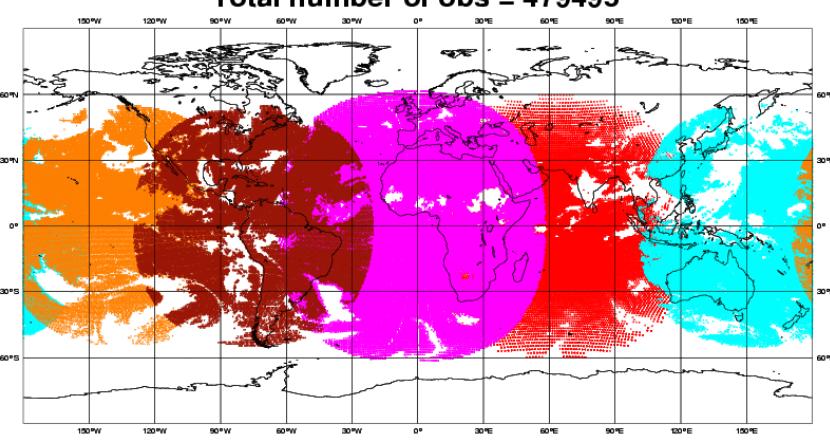
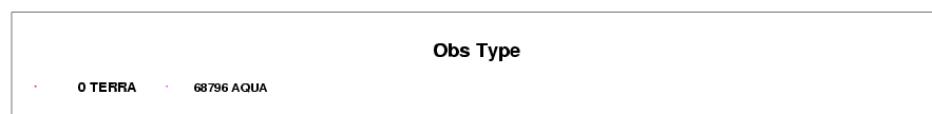
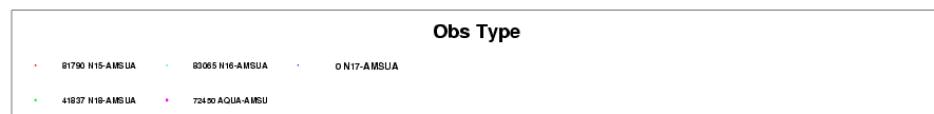
$R$  = Observation error covariance matrix (includes instrumental and representativeness error).

- Practical implementation requires numerous assumptions and approximations.....consider first the observations.....

# ECMWF Global Observations 1



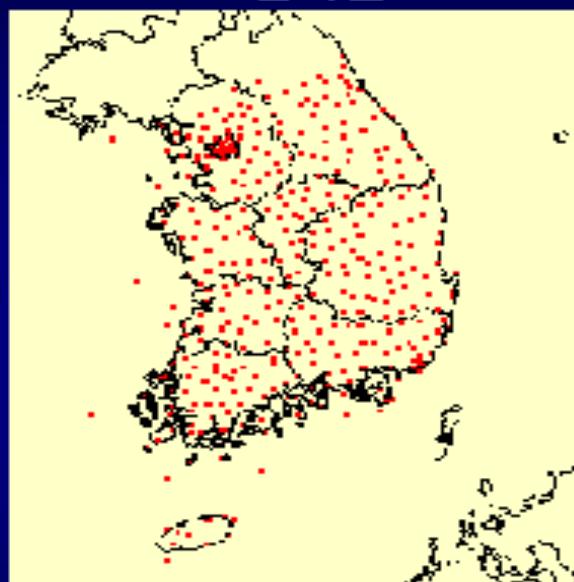
# ECMWF Global Observations 2



# Korean AWS/Radar Observations

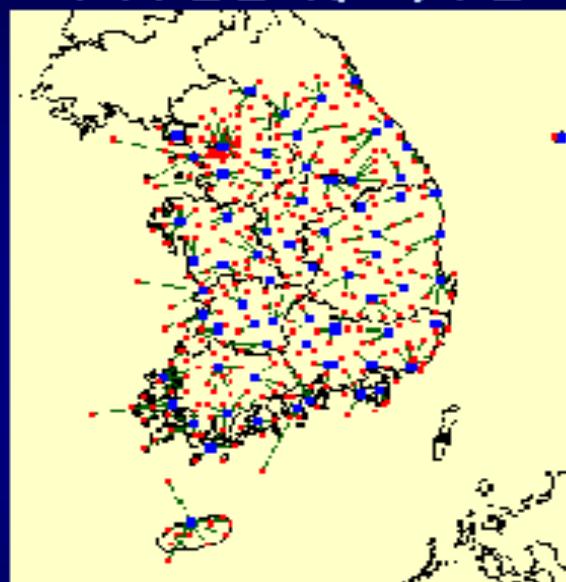
## 국지기상 연속감시 시스템

AWS 관측분포

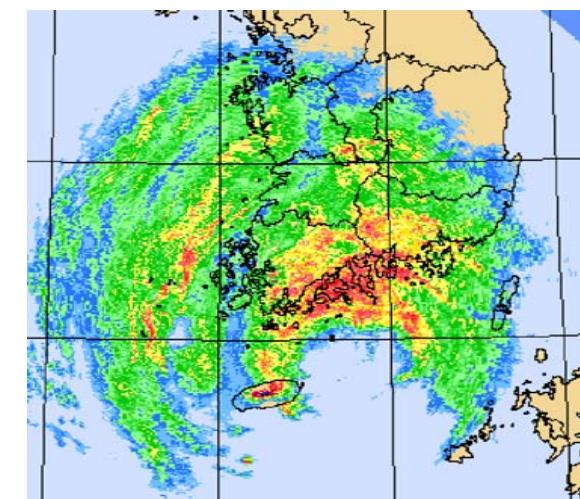


- 전국 400개소
- 관측간격 20km 미하

국지수집장치 (LAU) 수집



- 전국 68개소
- 매분 5초마다
- AWS → LAU로 자료전송  
(2400bps, 전용선)





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# Observation Cost Function ( $J_o$ ) Implementation

$$J(x) = J_b + J_o = \frac{1}{2} [x - x^b]^T P_b^{-1} [x - x^b] + \frac{1}{2} [y - H(x)]^T R^{-1} [y - H(x)]$$

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- Observation error correlations increase computational cost of second term (also hard to determine), so...
- Assume observation errors uncorrelated (specified by std. dev.  $\sigma_o^2$ ):

$$J(x) = \frac{1}{2} [x - x^b]^T P_b^{-1} [x - x^b] + \frac{1}{2} \sum_n [y - H(x)]_n^2 / \sigma_{on}^2$$

---

- Assumption motivates move towards assimilation of “raw” observations e.g. radiances, rather than retrievals.
- Use of “super observations” makes assumption better (and reduces cost still further).



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# Background Cost Function ( $J_b$ ) Implementation

$$J(x) = \frac{1}{2} [x - x^b]^T P_b^{-1} [x - x^b] + \frac{1}{2} \sum_n [y - H(x)]_n^2 / \sigma_{on}^2$$

*The Incremental formulation:*

- Define **analysis increments**:  $x^a = x^b + I x'$
- Solve **incremental** cost function:

$$J(x) = \frac{1}{2} x'^T P_b^{-1} x' + \frac{1}{2} \sum_n [d - y']_n^2 / \sigma_{on}^2$$

where  $y' = Hx'$ ,  $d = y - H(x^b)$



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# Incremental WRF-Var Preconditioning

$$J(x) = \frac{1}{2} x'^T P_b^{-1} x' + \frac{1}{2} \sum_n [d - y']_n^2 / \sigma_{on}^2$$

- Define **preconditioned control variable**  $v$  space transform  $x' = Uv$  where  $U$  transform **CAREFULLY** chosen to satisfy  $P_b = UU^T$ .
- Choose (at least assume) control variable components with uncorrelated errors:

$$J(x) = \frac{1}{2} \sum_i v_i^2 + \frac{1}{2} \sum_n [d - y']_n^2 / \sigma_{on}^2$$

- where

i~number pieces of independent information.

n~number of thinned, quality controlled observations.



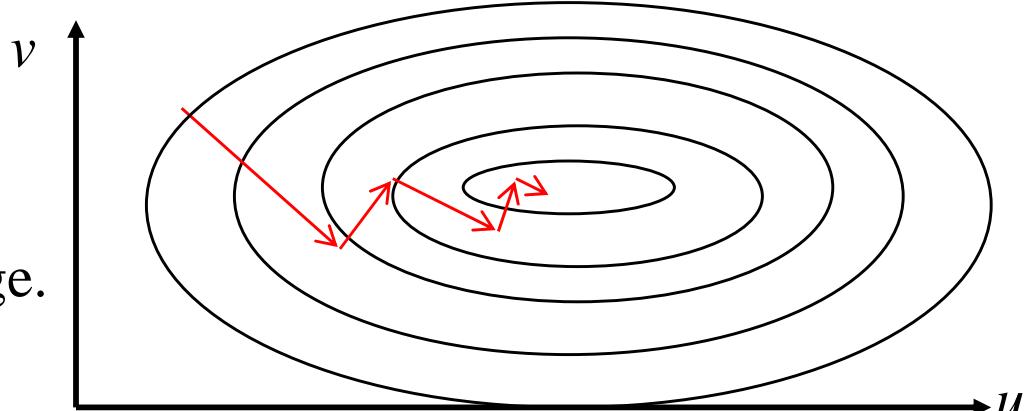
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# Minimization Basics

$$J = u^2/a^2 + v^2/b^2$$

- Suppose want to minimize J by iteration:

Steepest descent: many iterations to converge.

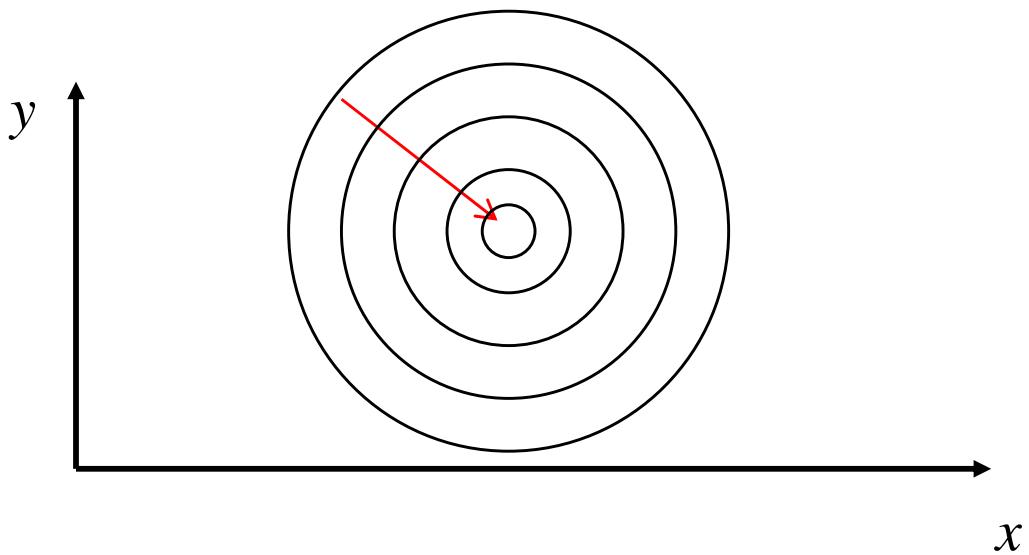


- Write transformation

$$(x, y) = (u/a, v/b), \quad J = x^2 + y^2$$

Steepest descent: one iteration to convergence.

In VAR, precondition and use e.g.  
Quasi-Newton, Conjugate Gradient methods.





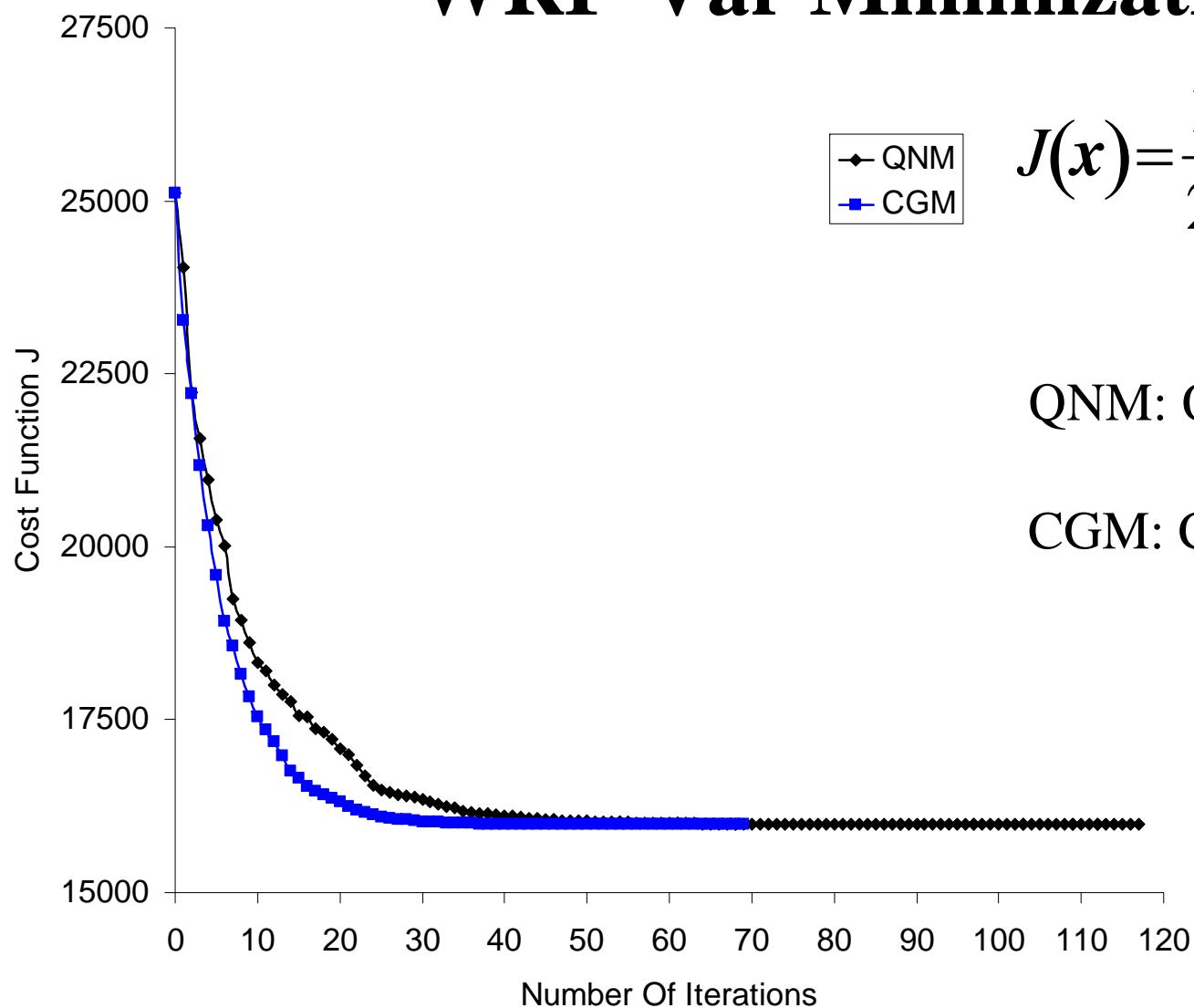
# WRF-Var Minimization Example

QNM  
CGM

$$J(x) = \frac{1}{2} \sum_i v_i^2 + \frac{1}{2} \sum_n [d - y']_n^2 / \sigma_{on}^2$$

QNM: Quasi-Newton Method.

CGM: Conjugate Gradient Method.

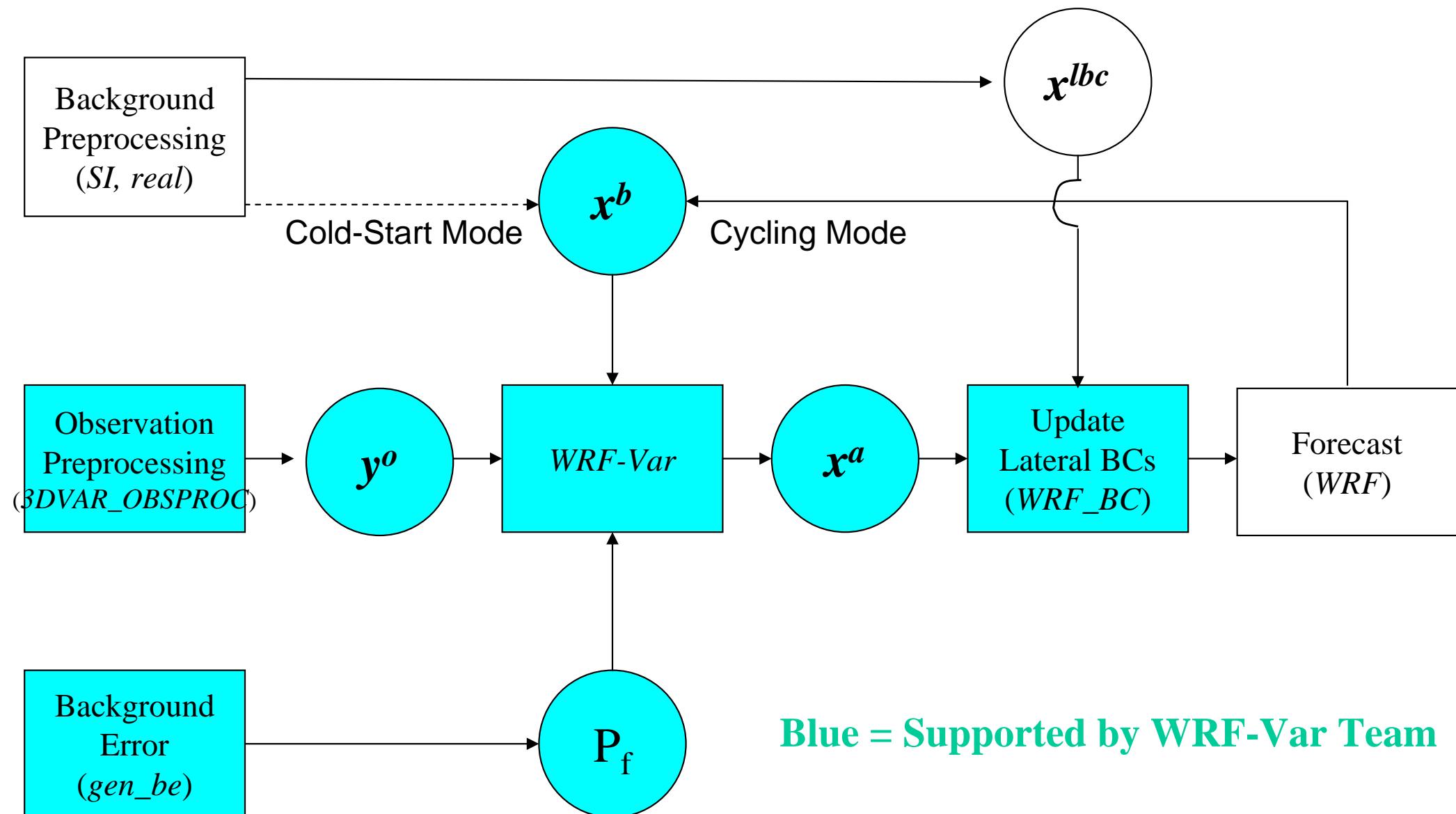


Convergence obtained when gradient < 0.001 starting gradient.

Here, CGM -> ~40% reduction in 3DVAR run-time.

# 3. The WRF-Var Algorithm

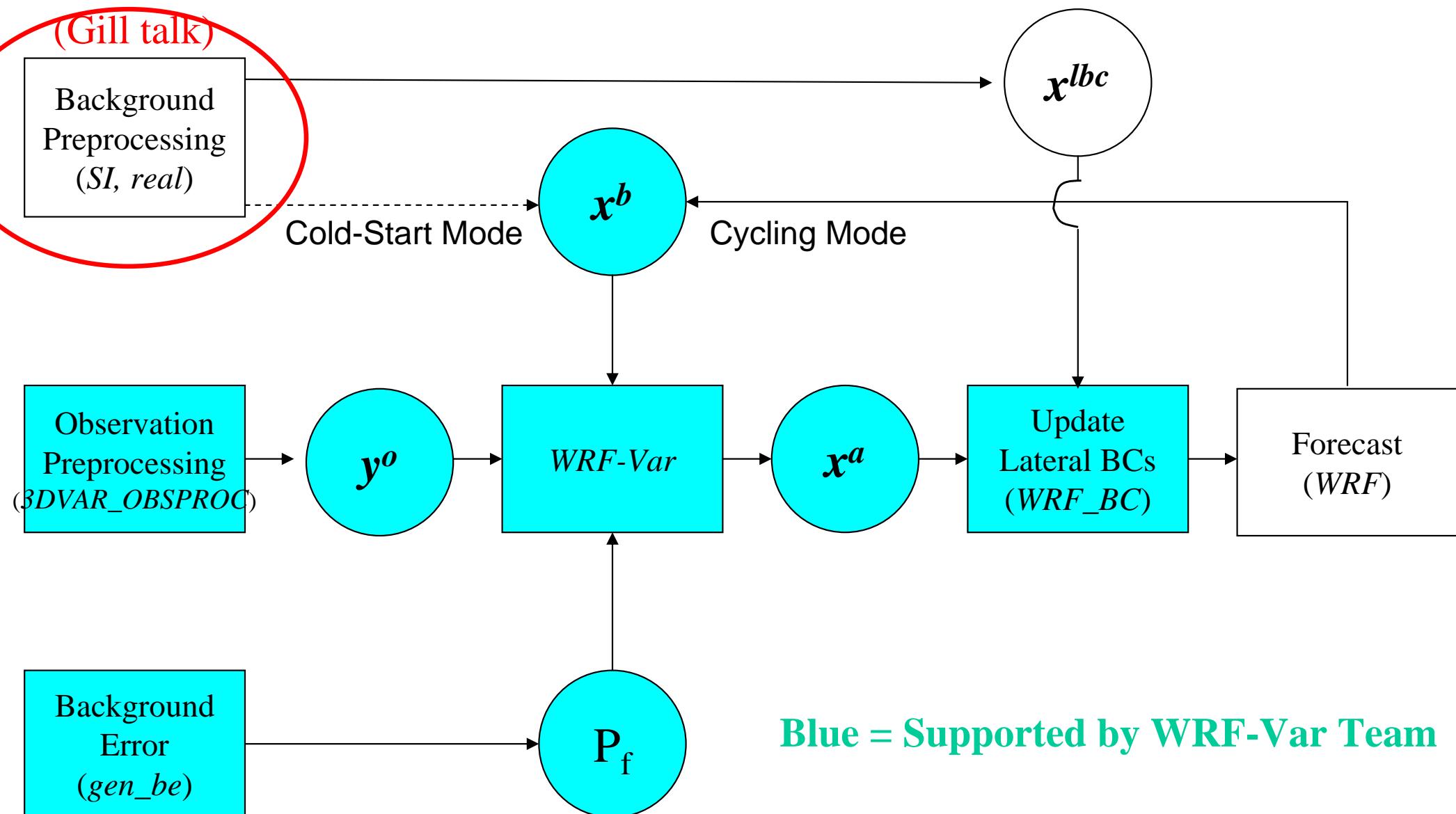
# WRF-Var in the WRF Modeling System





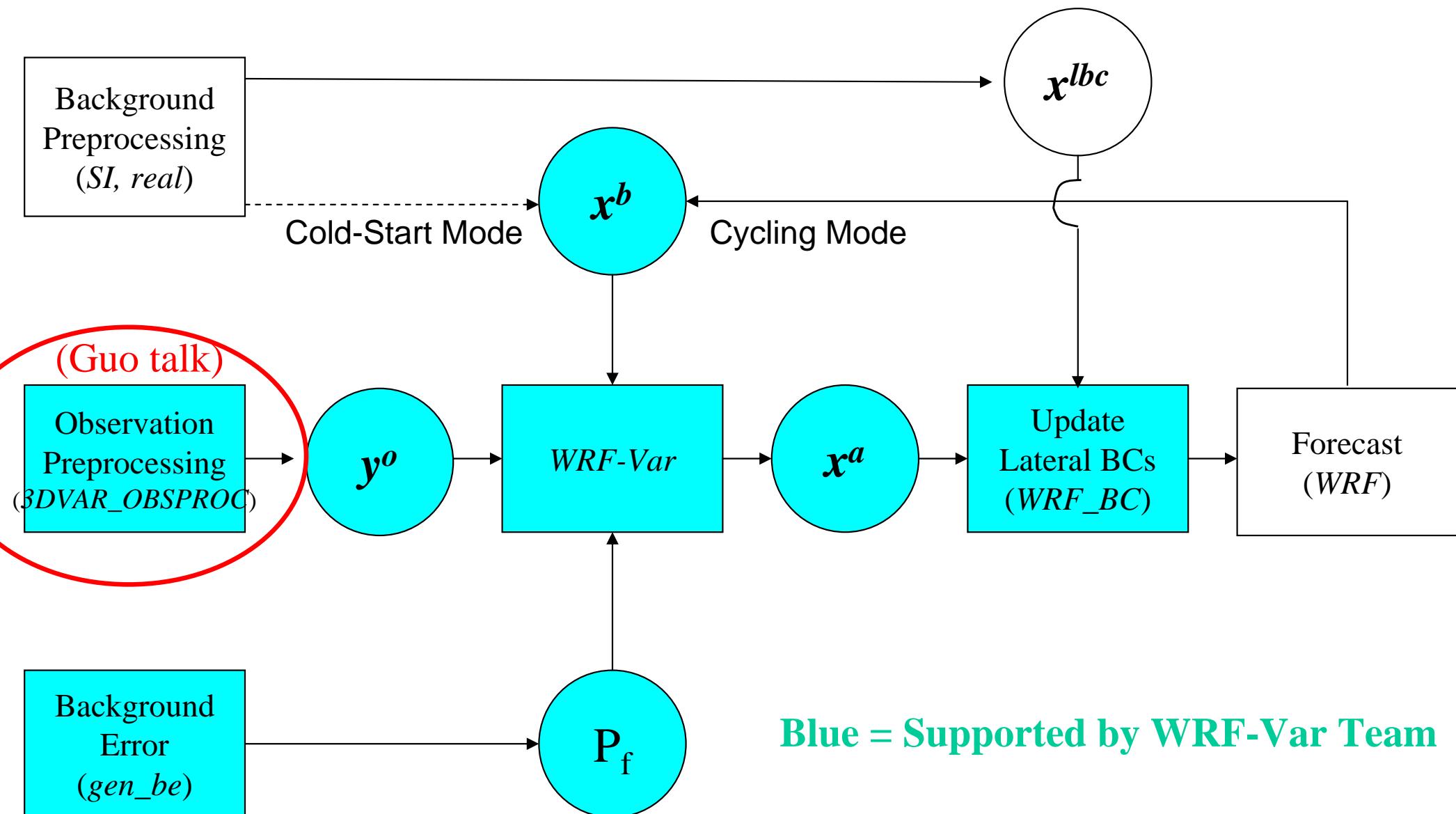
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# WRF-Var in the WRF Modeling System





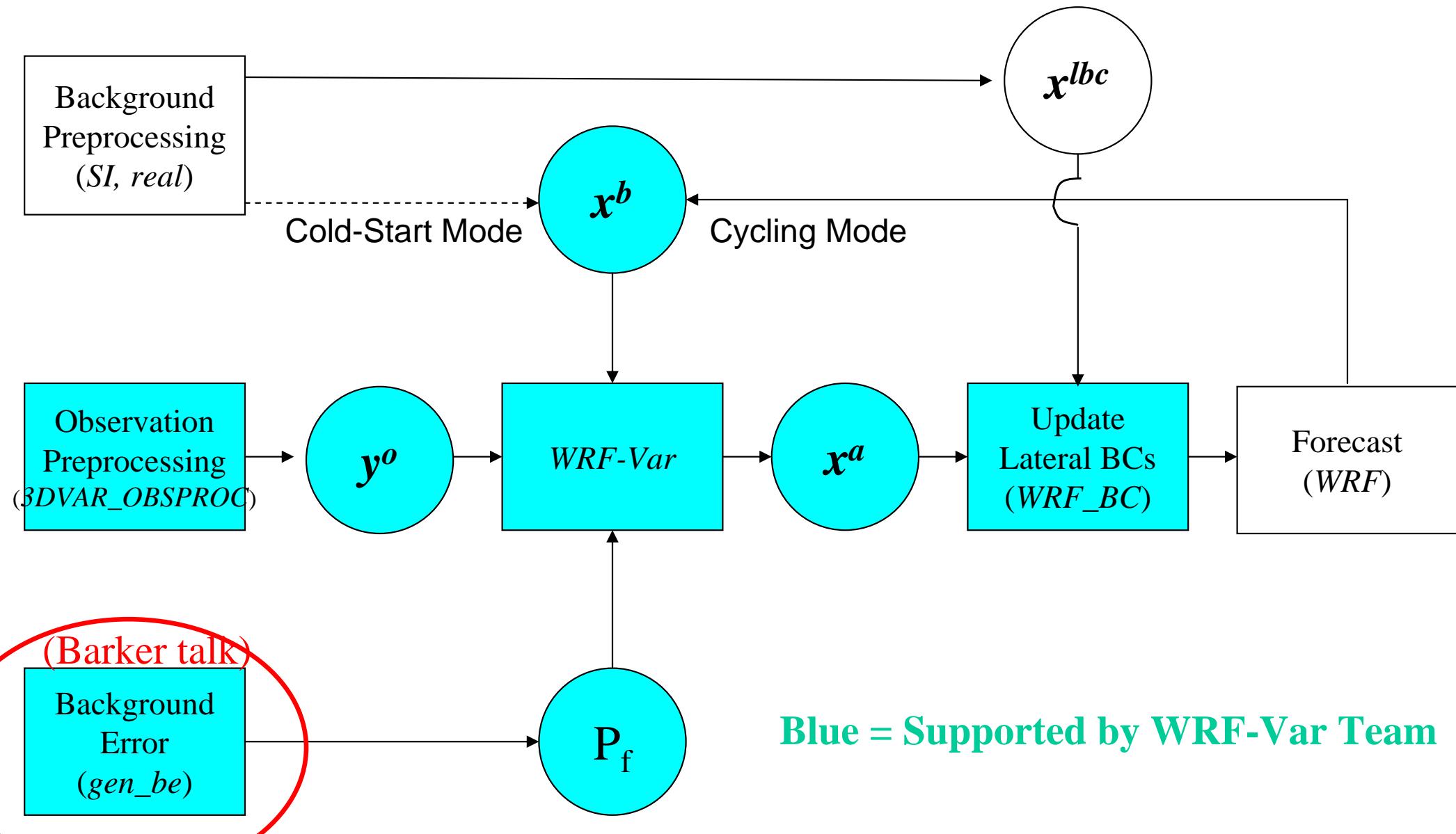
# WRF-Var in the WRF Modeling System





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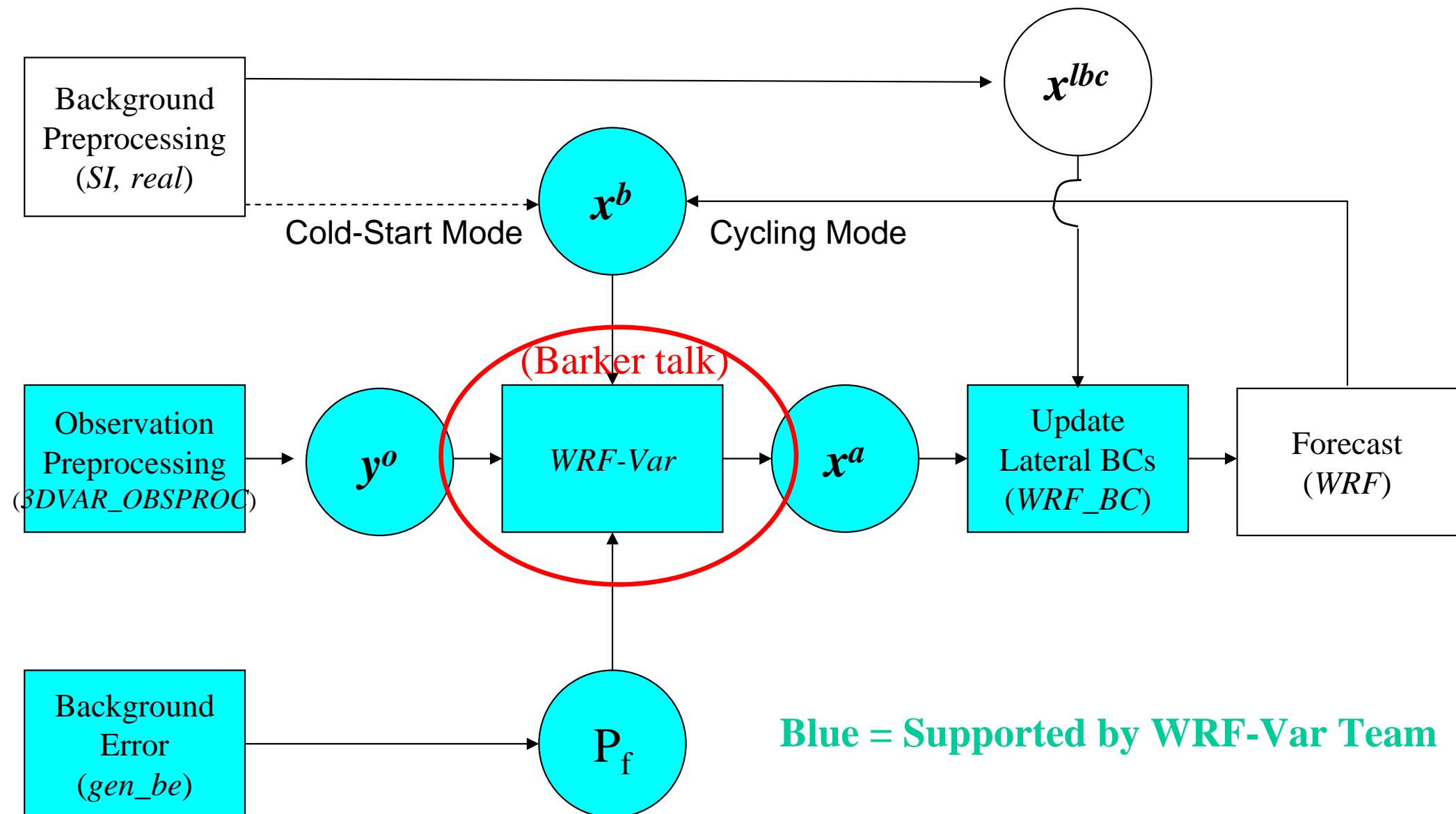
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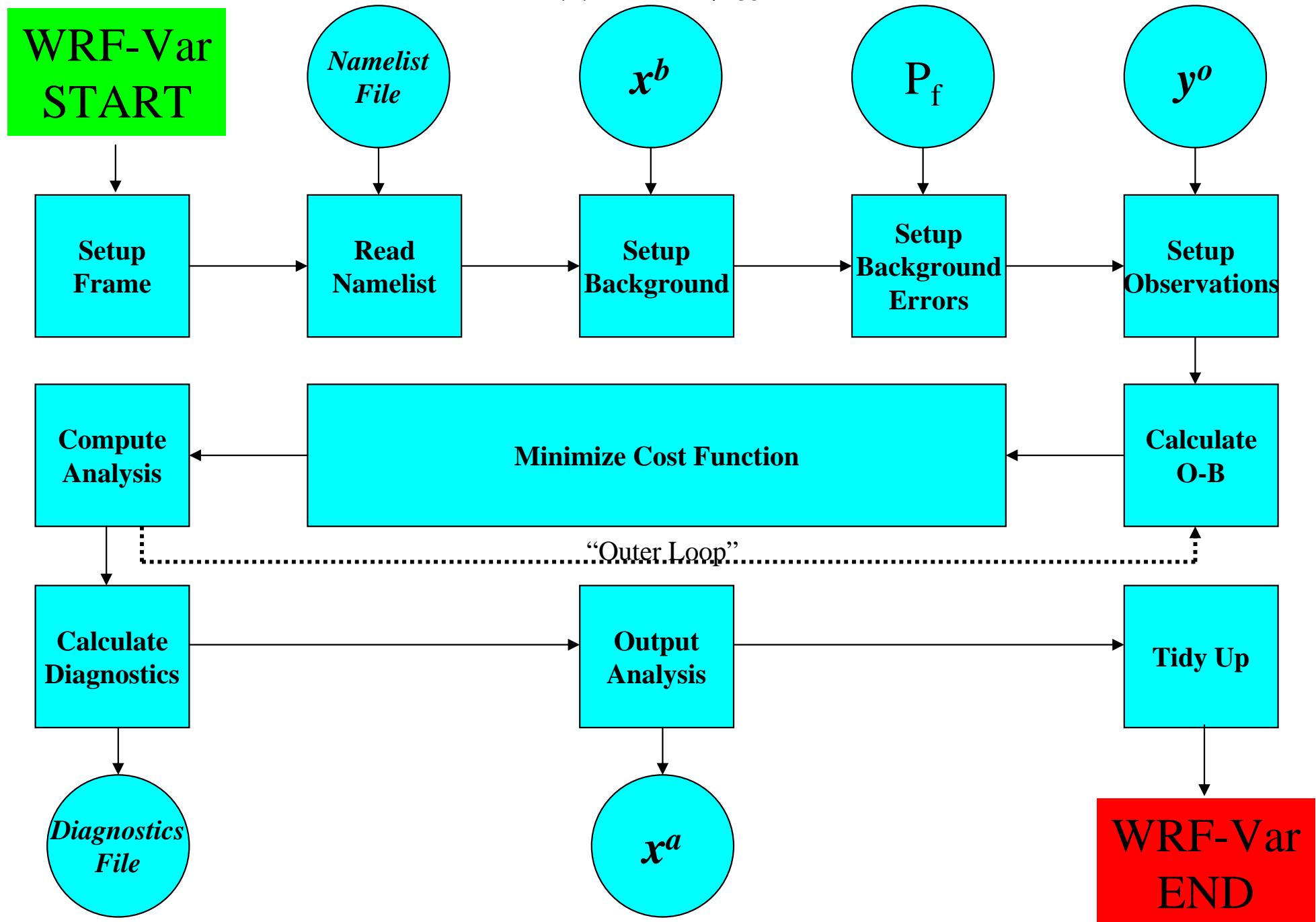
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# WRF-Var in the WRF Modeling System



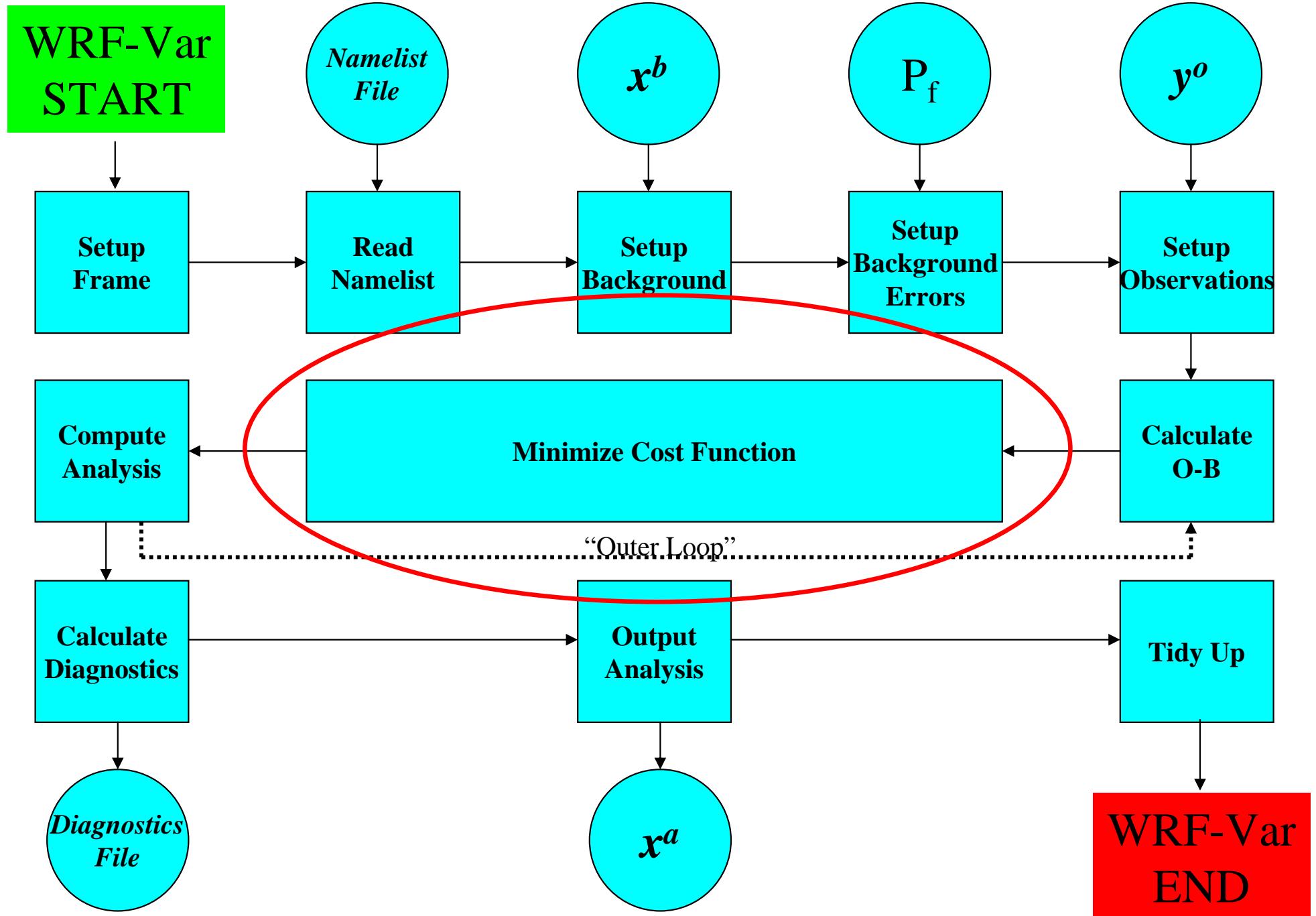


# WRF-Var





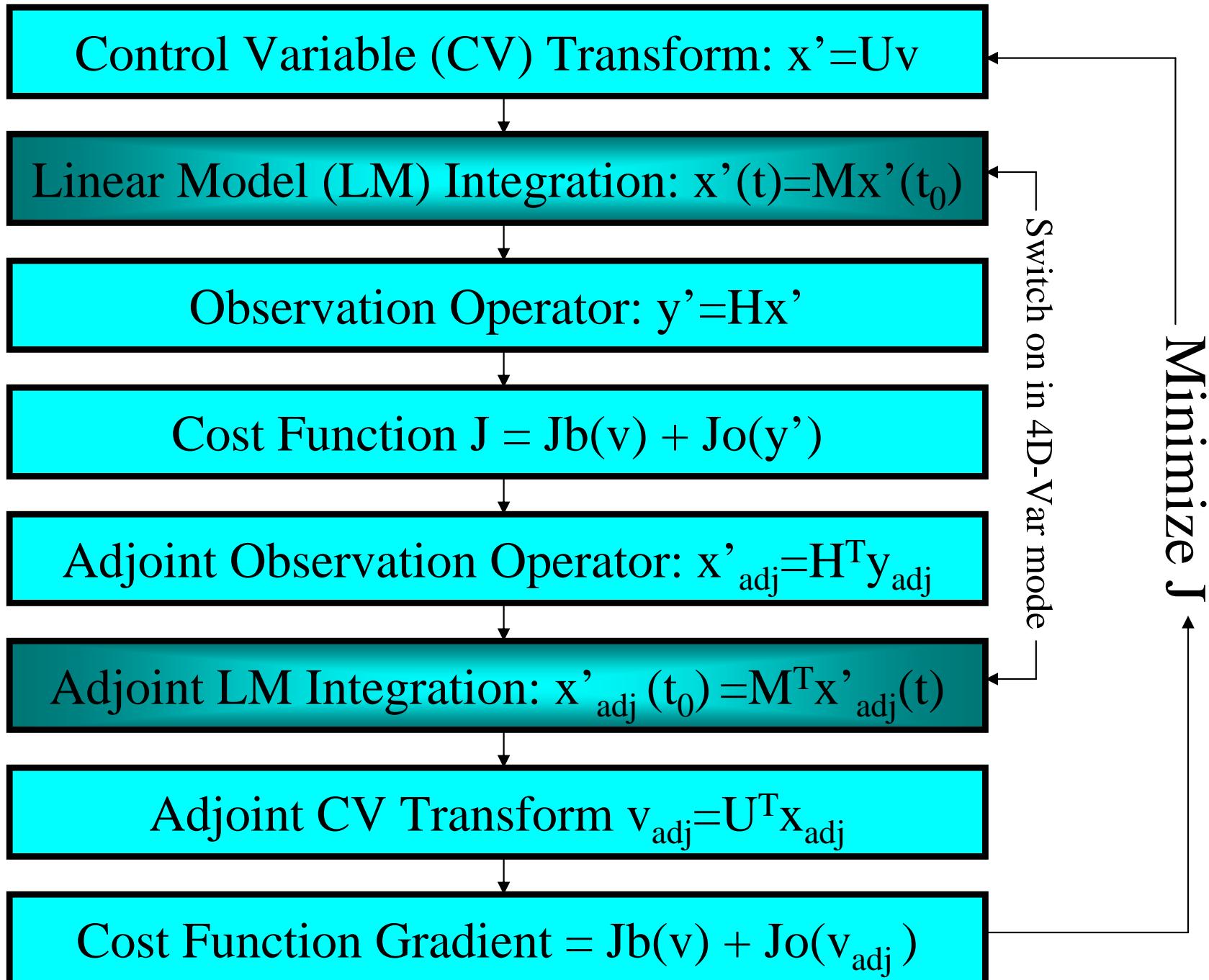
# WRF-Var





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# WRF-Var “Inner Loop”



# 4. Background Error Modelling

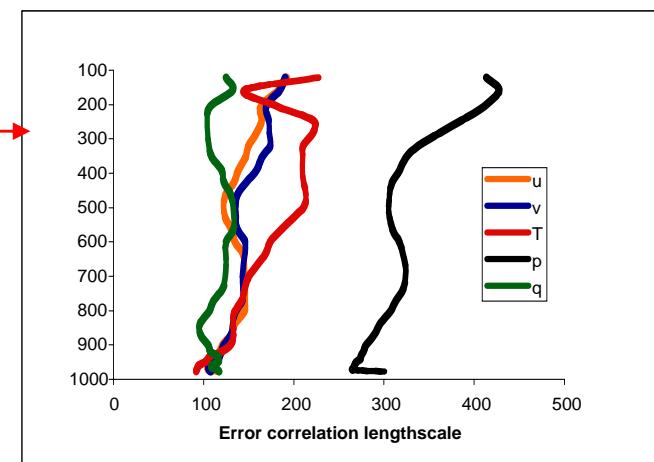
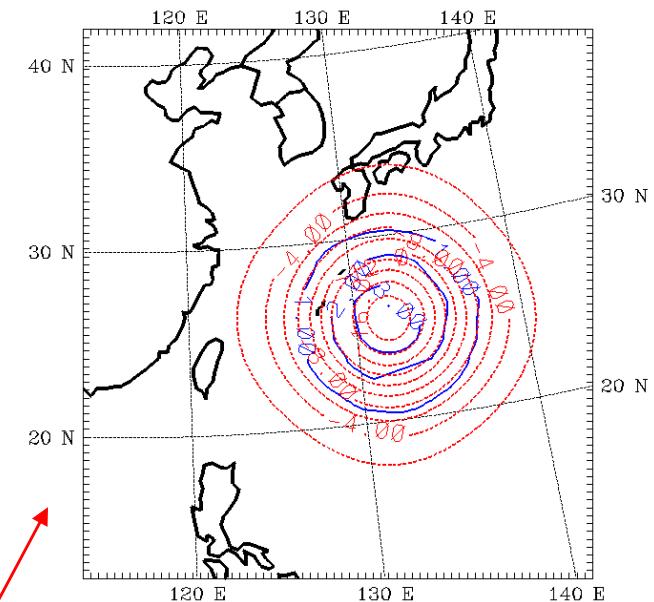


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# WRF-Var Control Variable Transform

cv_options		2 (original MM5)	3(GSI)	4 (Global)	5(regional)
Analysis increments	$\mathbf{x}'$	$u', v', T', q', p_s'(i, j, k)$			
Change of Variable	$U_p$	$\psi', \chi', p_u', q'(i, j, k)$	$\psi', \chi_u', T_u', \tilde{r}', p_{uu}'(i, j, k)$		
Vertical Covariances	$U_v$	$\mathbf{B} = \mathbf{E} \Lambda \mathbf{E}^T$	RF	$\mathbf{B} = \mathbf{E} \Lambda \mathbf{E}^T$	
Horizontal Correlations	$U_h$	RF	Spectral	RF	
Control Variables	$\mathbf{v}$	$\mathbf{v}(i, j, m)$	$\mathbf{v}(l, n, m)$	$\mathbf{v}(i, j, m)$	

$$\mathbf{x}' = U\mathbf{v} = U_p U_v U_h \mathbf{v}$$



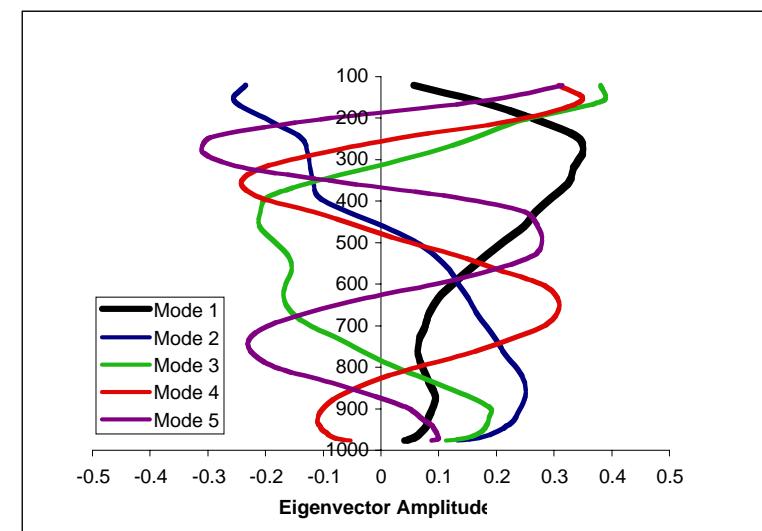
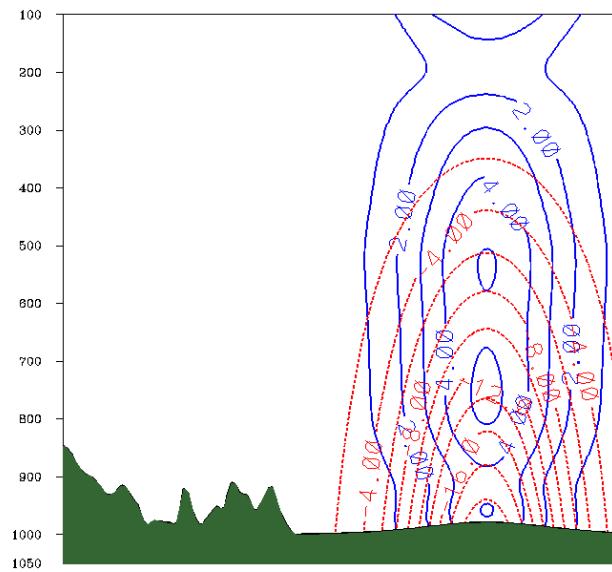


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Vertical Covariances	$U_v$	$\mathbf{B} = \mathbf{E} \Lambda \mathbf{E}^T$	RF	$\mathbf{B} = \mathbf{E} \Lambda \mathbf{E}^T$	
Horizontal Correlations	$U_h$	RF	Spectral	RF	
Control Variables	$\mathbf{v}$	$\mathbf{v}(i, j, m)$	$\mathbf{v}(l, n, m)$	$\mathbf{v}(i, j, m)$	

$$\mathbf{x}' = U\mathbf{v} = U_p U_v U_h \mathbf{v}$$





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# WRF-Var Control Variable Transform

cv_options		2 (original MM5)	3(GSI)	4 (Global)	5(regional)
Analysis increments	$\mathbf{x}'$	$u', v', T', q', p_s'(i, j, k)$			
Change of Variable	$U_p$	$\psi', \chi', p_u', q'(i, j, k)$	$\psi', \chi_u', T_u', \bar{r}', p_{su}'(i, j, k)$		
Vertical Covariances	$U_v$	$\mathbf{B} = \mathbf{E} \Lambda \mathbf{E}^T$	RF	$\mathbf{B} = \mathbf{E} \Lambda \mathbf{E}^T$	
Horizontal Correlations	$U_h$	RF	Spectral	RF	
Control Variables	$\mathbf{v}$	$\mathbf{v}(i, j, m)$	$\mathbf{v}(l, n, m)$	$\mathbf{v}(i, j, m)$	

$$\mathbf{x}' = U\mathbf{v} = U_p U_v U_h \mathbf{v}$$

Define control variables:

$$\psi'$$

$$r' = q'/q_s(T_b, q_b, p_b)$$

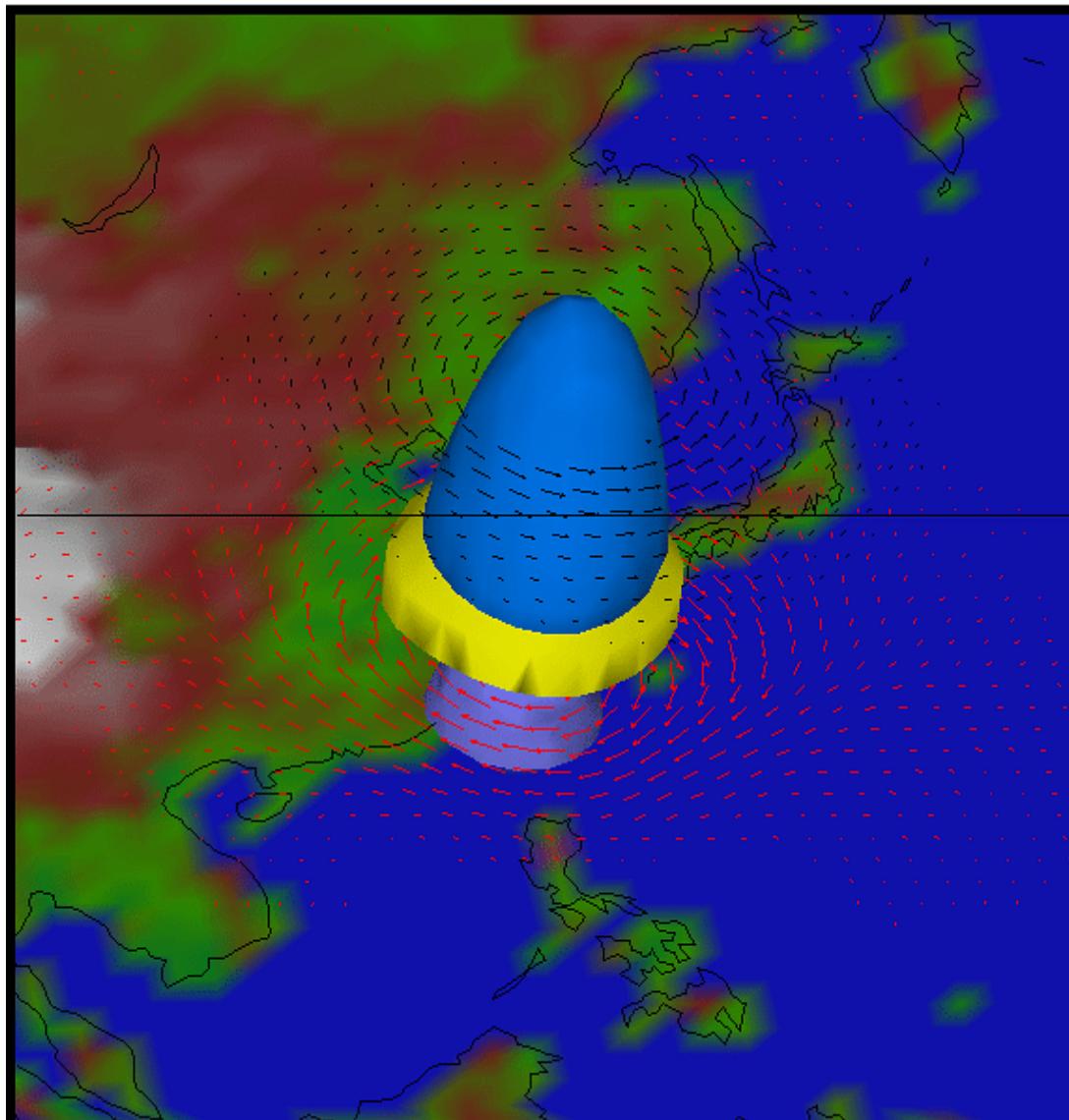
$$\chi' = \chi_u' + \chi_b'(\psi')$$

$$T' = T_u' + T_b'(\psi')$$

$$p_s' = p_{su}' + p_{sb}'(\psi')$$



# WRF-Var: Analysis Increment of Single GPS TPW Observation



The plot at left shows the combined response of WRF-Var to a single TPW observation O-B=1mm located at Taipei.

**Analysis Increment Isosurfaces:**

Blue =  $q$  (1g/kg).

Yellow =  $T$  (1K).

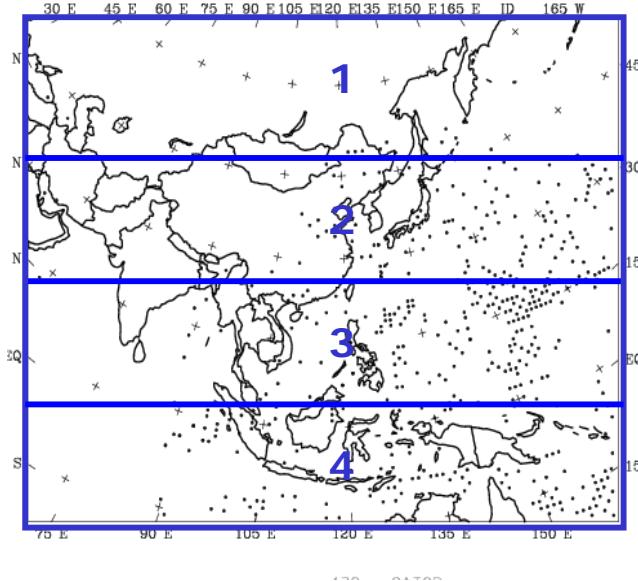
Purple=Pressure(1hPa).

Red = Wind Circulation at  $k=5$ .

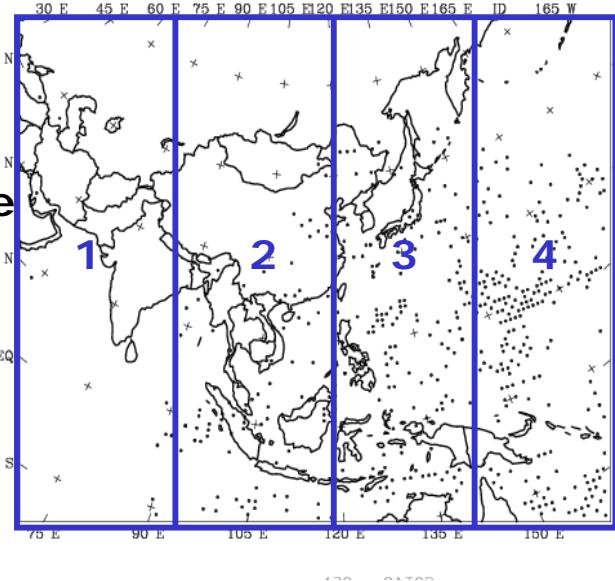
Black = Wind Circulation at  $k=25$ .



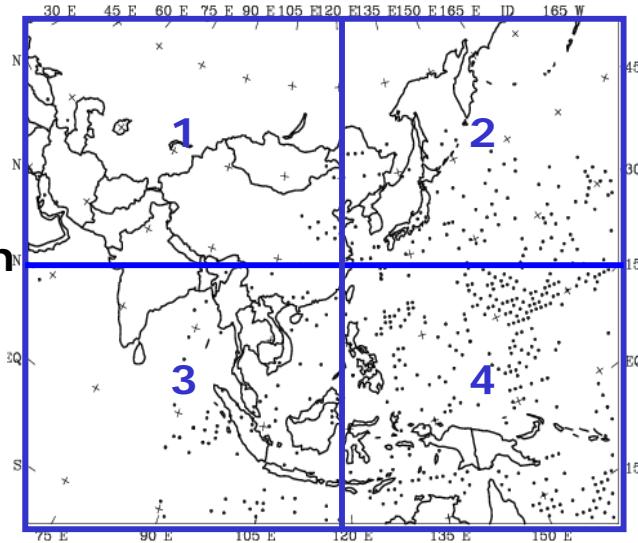
# WRF-Var Multi-Processor Decomposition (e.g. np=4)



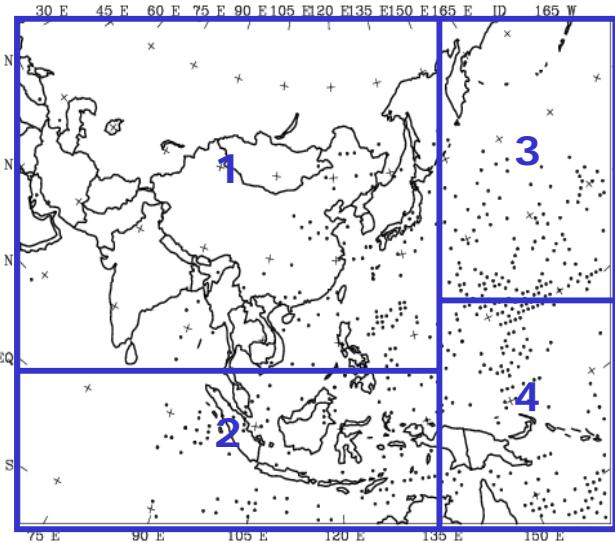
Recursive  
Filter  
and  
FFTs



Minimization  
and  
Forecast  
Model

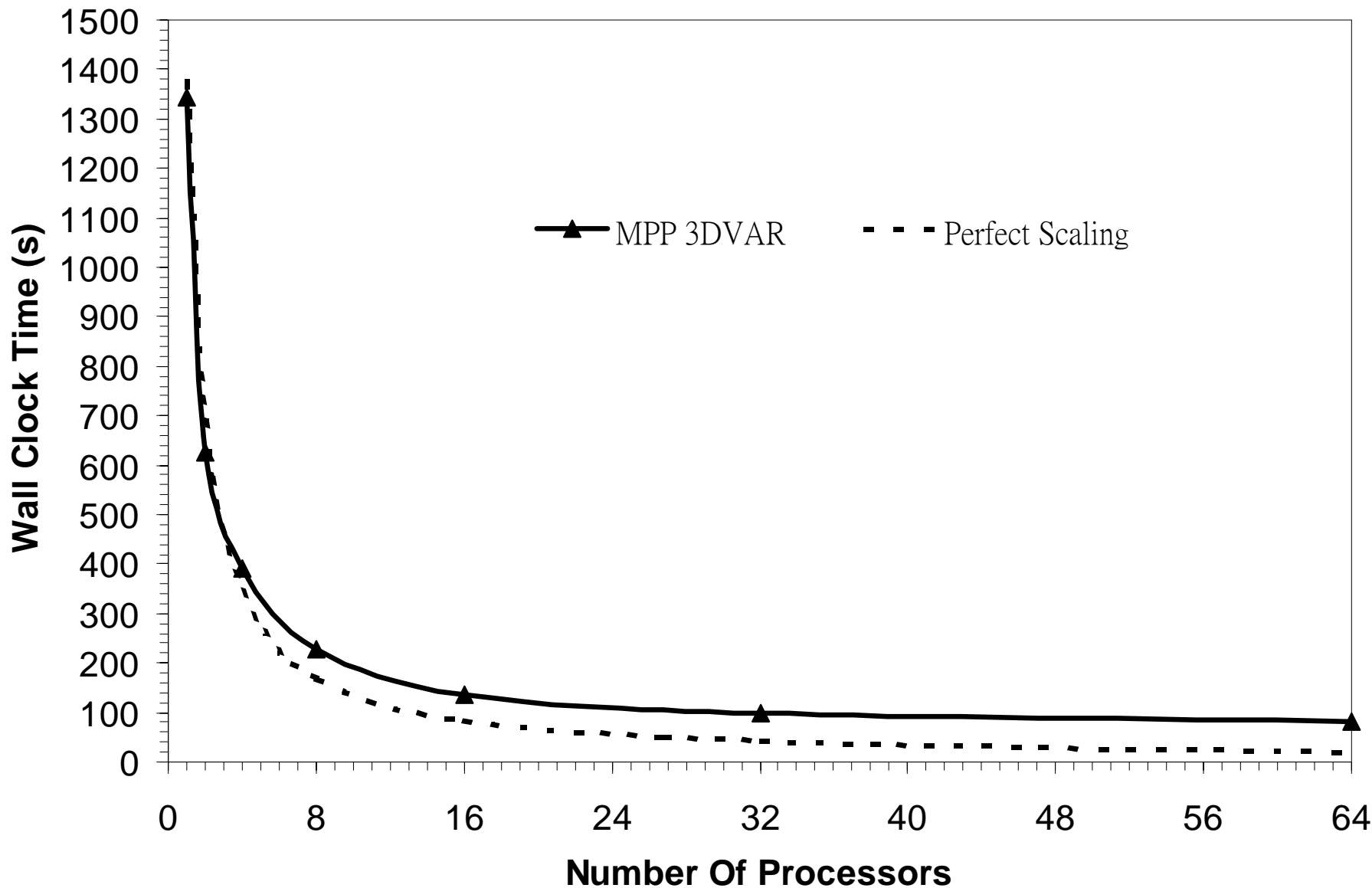


Observation  
Operators





# MPP Scalability – NCAR IBM-SP



- Test Case: 140x150x41 AFWA 45km “T4 theater” – 25<sup>th</sup> Jan 2002.
- Background error tuning – Old Its = 98, New = 49 (64PE = 58s).

# 5. Observational Issues



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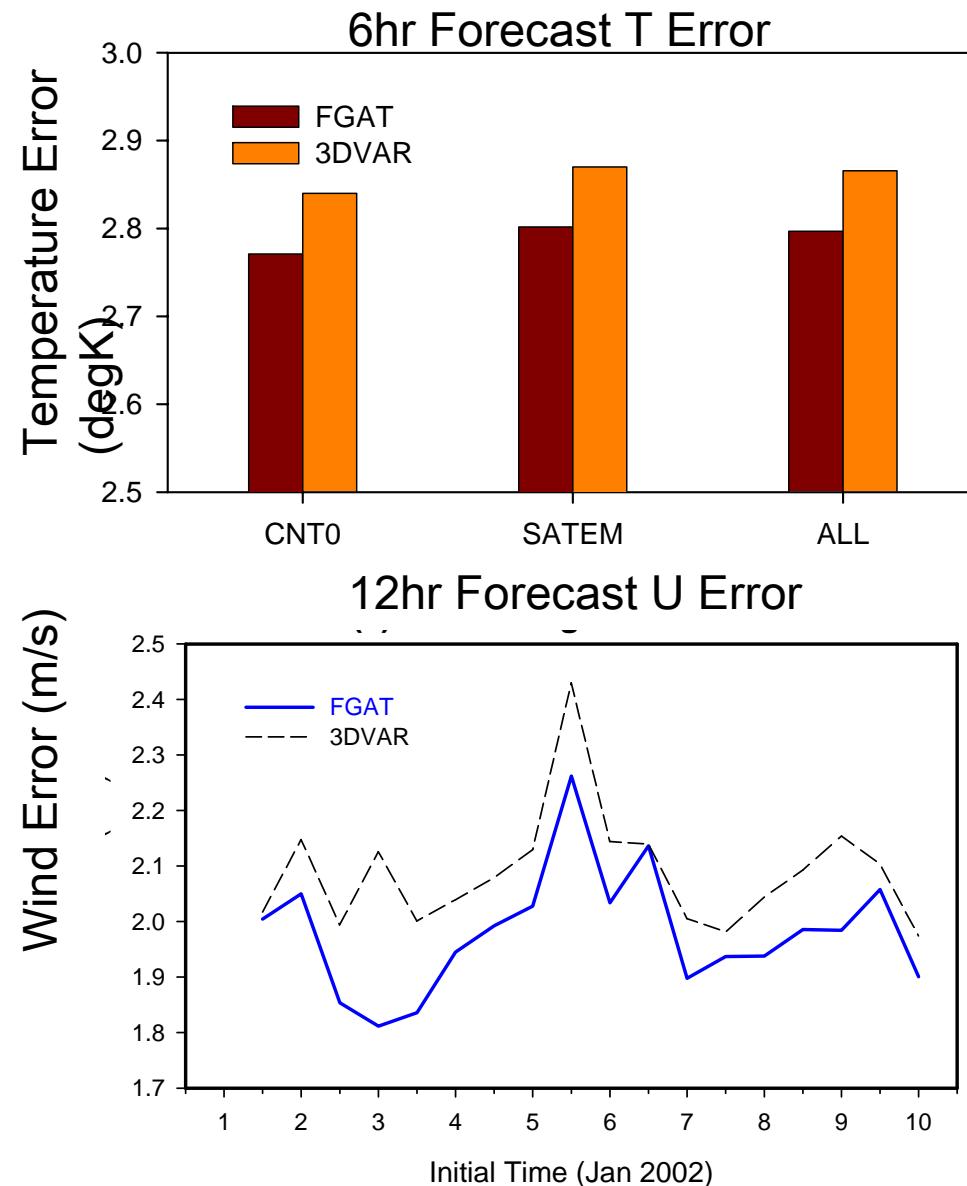
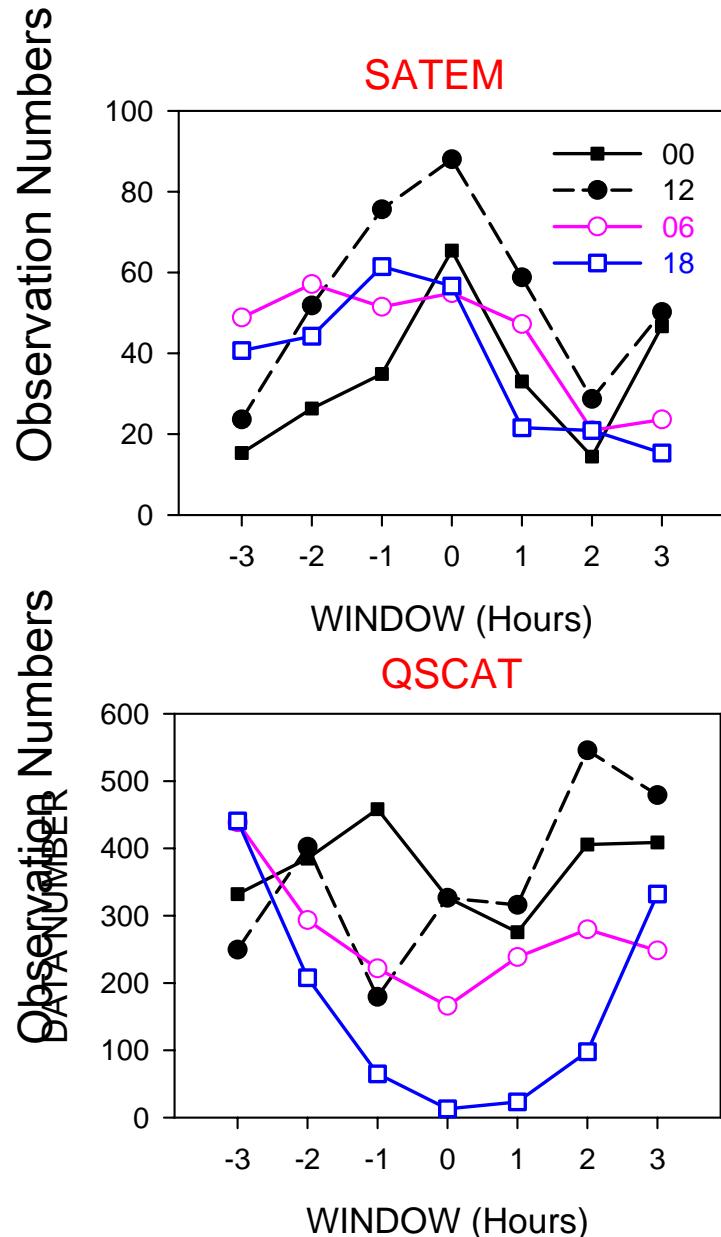
# WRF-Var Observations Used (July 2005)

- Conventional:
  - Surface (SYNOP, METAR, SHIP, BUOY).
  - Upper air (TEMP, PIBAL, AIREP, ACARS).
- Remotely sensed retrievals:
  - Atmospheric Motion Vectors (SATOBS, MODIS).
  - Ground-based GPS Total Precipitable Water.
  - SSM/I oceanic surface wind speed and TPW.
  - Scatterometer (Quikscat) oceanic surface winds.
  - Wind Profiler.
  - Radar radial velocity and reflectivity.
  - ATOVS/AIRS/MODIS temperature/humidities.
  - GPS “local” refractivity.
- Radiances:
  - SSM/I brightness temperatures (Shu-Hua Chen).
  - AMSU GOES/AIRS (under development).



# First Guess at Appropriate Time (FGAT)

- Principle: Compare observations with first guess forecast valid at time of observation





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# Radar Radial Velocity Observation Operator

- Observation operator (Sun and Crook 1998):

$$V_r = u \frac{x - x_i}{r_i} + v \frac{y - y_i}{r_i} + (w - v_T) \frac{z - z_i}{r_i}$$

- Terminal velocity a function of rain concentration:

$$v_T = 5.40a \cdot q_r^{0.125}$$

$$a = (p_0 / \bar{p})^{0.4}$$

- Require addition of hydrometeor variables to WRF-Var.

# Radar Data Assimilation

- Purpose: Can we assimilate radar radial velocity (and reflectivity) in 3D-Var to produce superior forecasts?
- Quality control/preprocessing crucial.
- Diagnose/analyze vertical velocity via “Richardson equation”

$$\gamma p \frac{\partial w}{\partial z} = \gamma p \left[ \frac{Q}{T c_p} - \nabla_z \bullet v \right] - v \bullet \nabla_z p + g \int_z^{\infty} \nabla_z \bullet (\rho v) dz$$

Combines thermodynamic, continuity and hydrostatic equations....

- Linearize continuous eqn., then discretize (assume Q=0 for now):

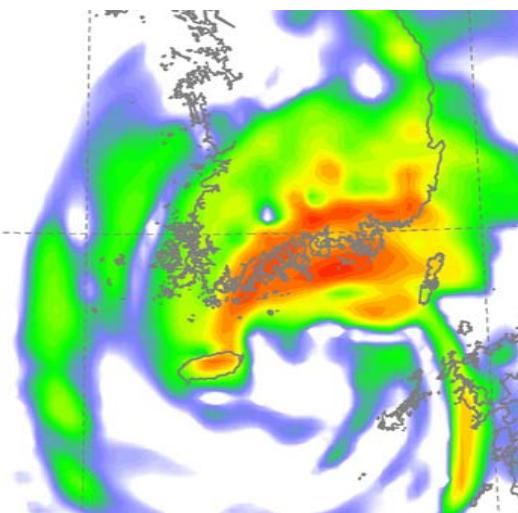
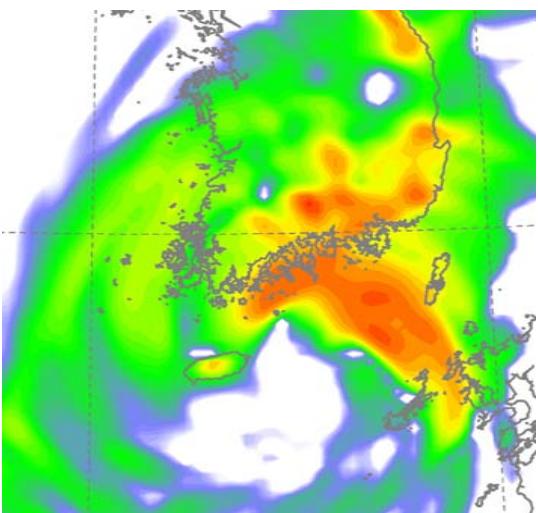
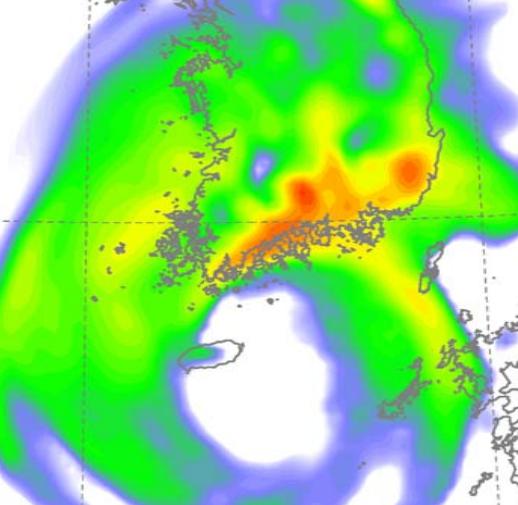
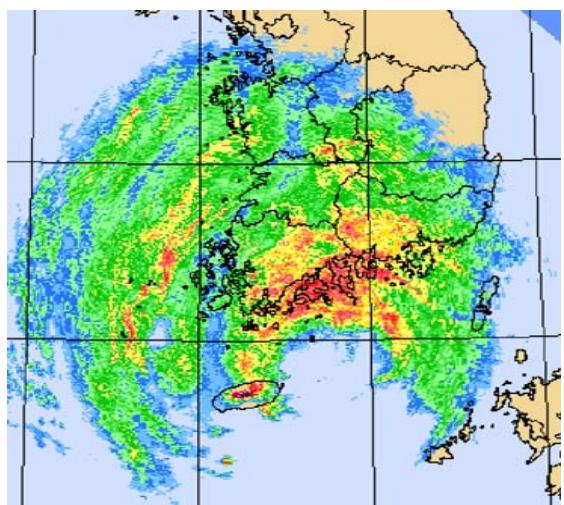
$$\begin{aligned} \gamma \bar{p} \frac{\partial w'}{\partial z} = & -\gamma p' \frac{\partial \bar{w}}{\partial z} - \gamma \bar{p} \nabla \cdot \vec{v}'_h - \gamma p' \nabla \cdot \vec{\bar{v}}_h - \bar{\vec{v}}_h \nabla p' \\ & - \vec{v}' \nabla \bar{p} + g \int_z^{\infty} \nabla \cdot (\rho \vec{v}'_h) dz + g \int_z^{\infty} \nabla \cdot (\rho' \vec{\bar{v}}_h) dz \end{aligned}$$

# Korean Radar Data Assimilation in WRF 3D-Var

Typhoon Rusa Test Case 3hr Precip: Typhoon Rusa 3hr Precip. Verification:

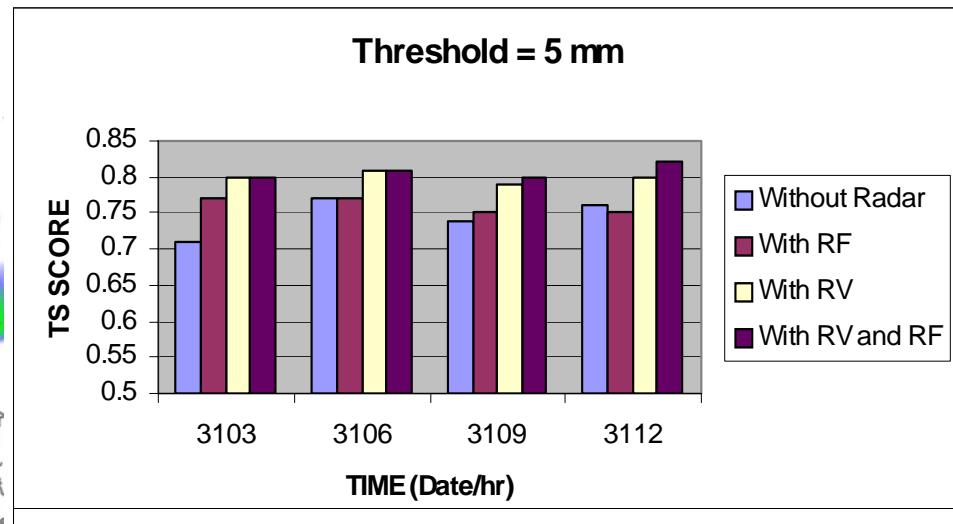
Obs (03Z, 31/08)

No Radar

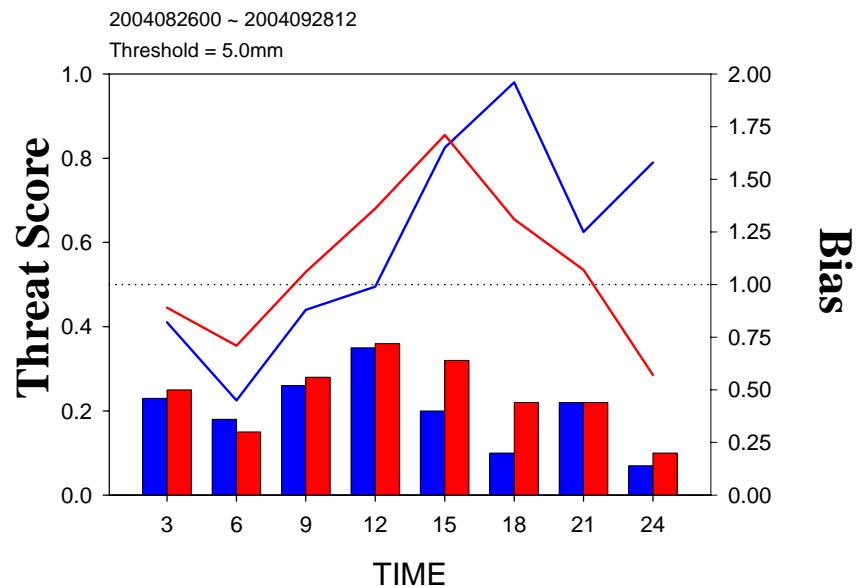


Radar RV

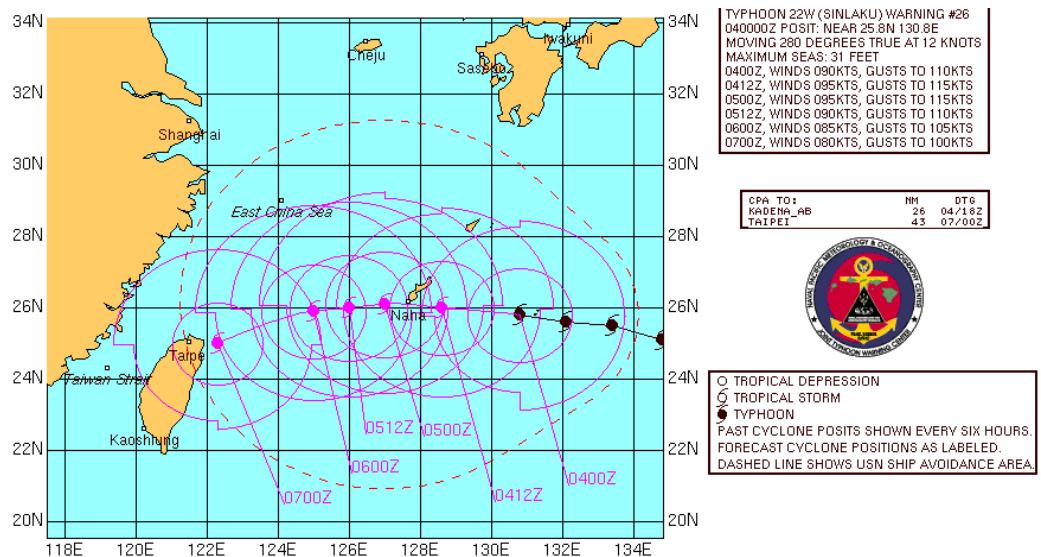
Radar RV+RF



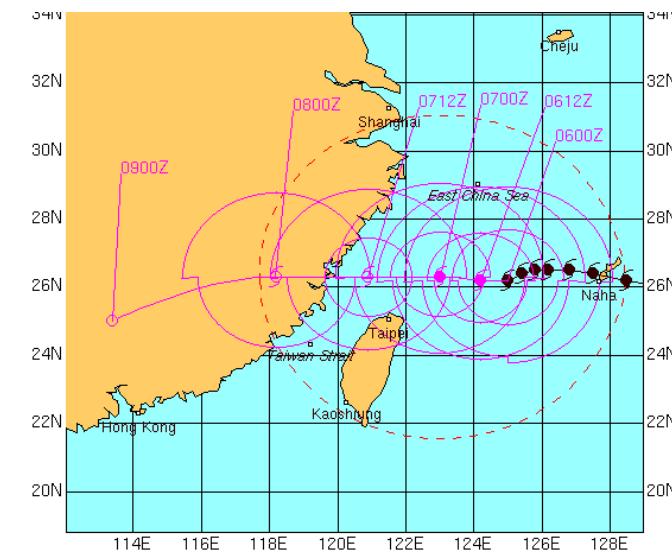
**KMA Pre-operational Verification:  
(no radar: blue, with radar: red)**



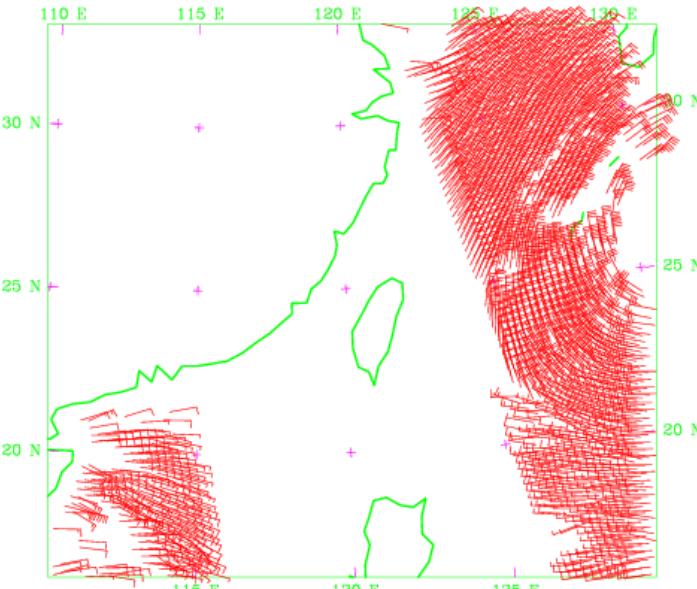
# Typhoon Sinlaku WRF-Var Bogussing



**00Z September 4<sup>th</sup> 2002**

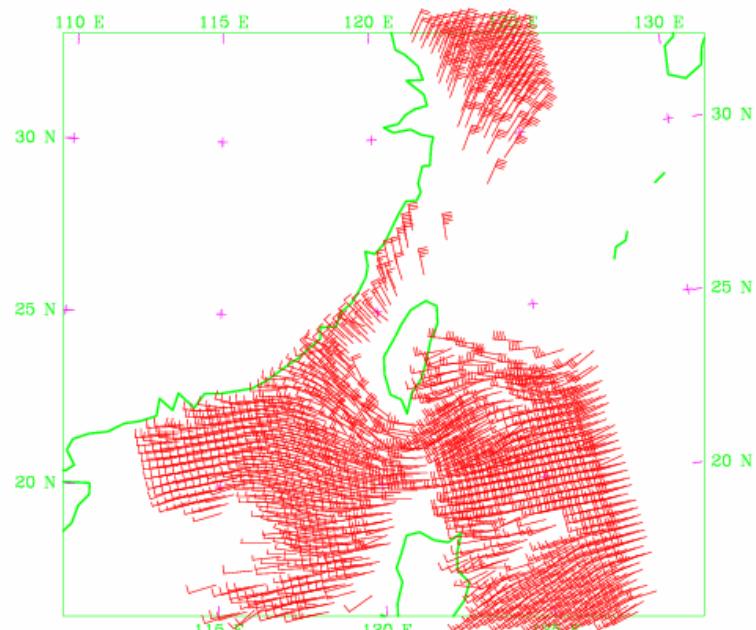


**00Z September 6<sup>th</sup> 2002**



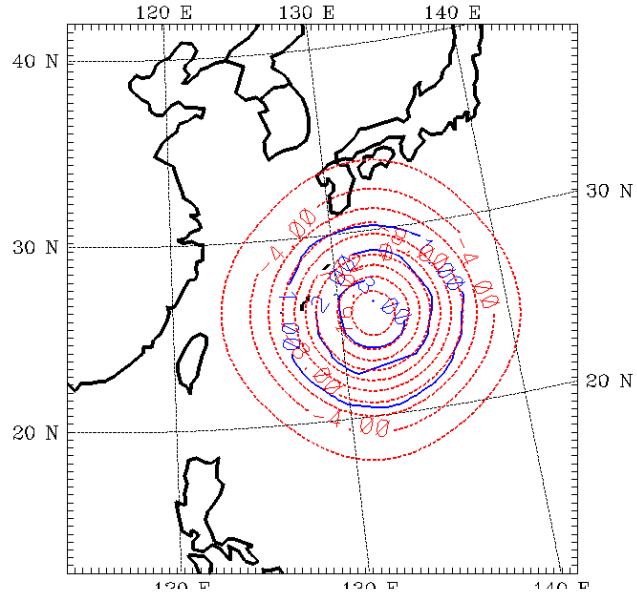
Quikscat Data

Barker et al  
(2004)

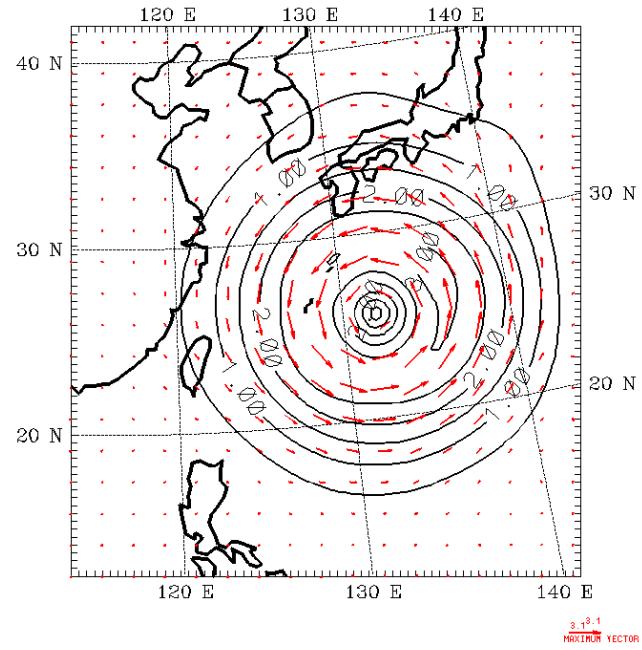
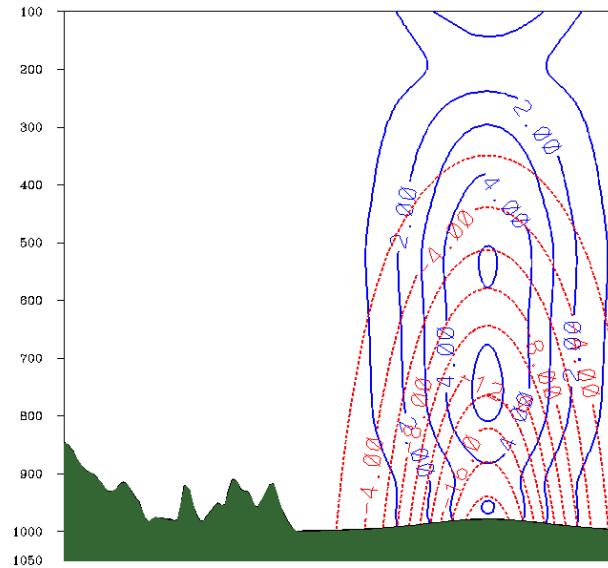




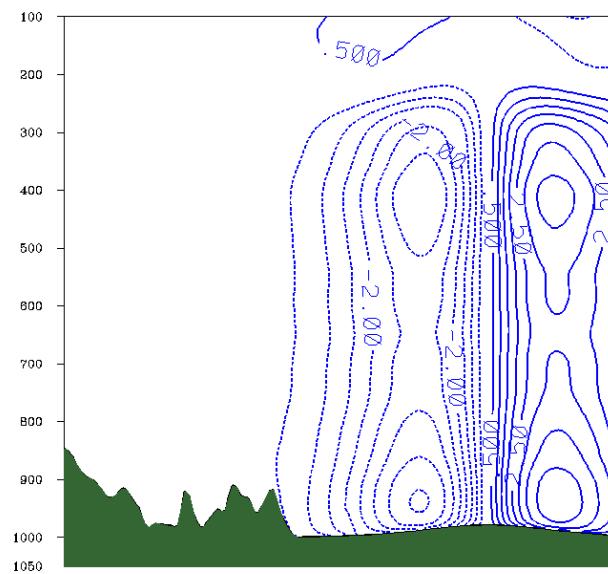
# WRF-Var bogus:Analysis Increments



Pressure,  
Temperature



Wind Speed,  
Vector,  
v-wind component.



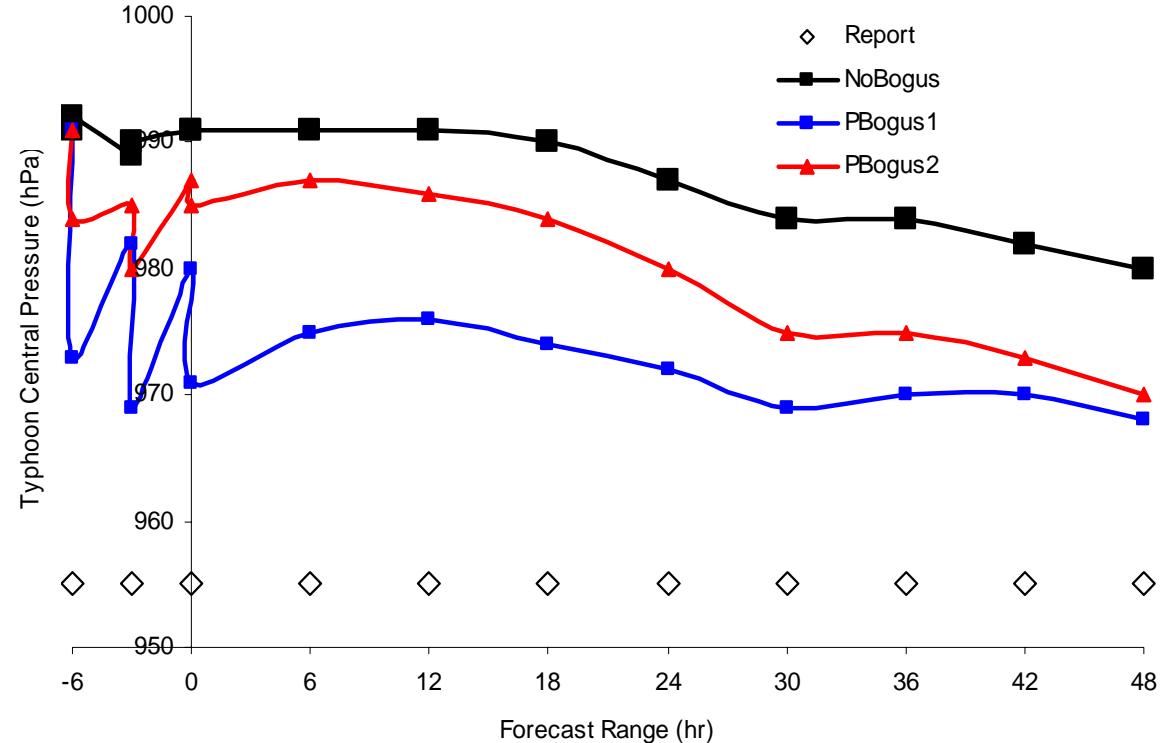


NCAR

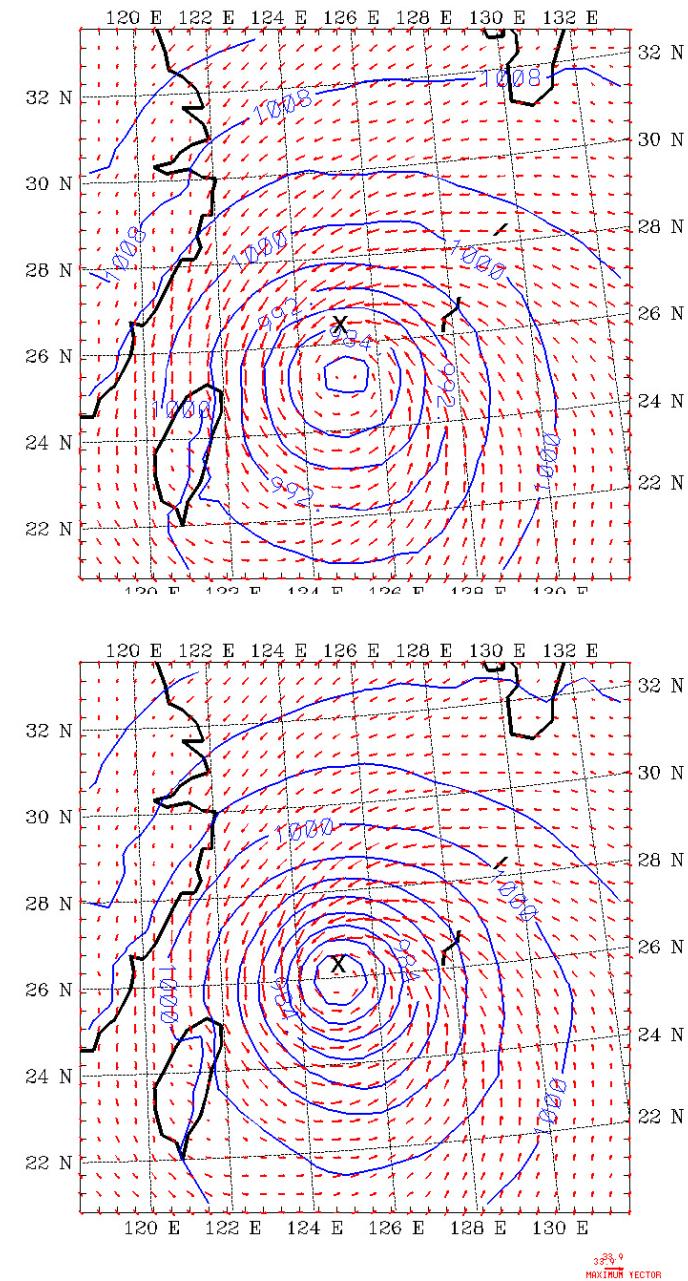
# WRF-Var bogus: Impact on forecast

48hr Forecast (NoBogus)->

## Typhoon Central Pressure



48hr Forecast (PBogus1)->



# 4. Current Status and Future Plans

# WRF-Var Version 2.1 (Release July 2005)

- First Guess at Appropriate Time (FGAT).
- Radar reflectivity.
- Other new obs: GPS refractivity, MODIS AMVs.
- Platforms: IBM-SP, DEC, Linux, SGI, Cray X1, Apple G4/G5.
- Initial 4D-Var modifications.
- New utility *gen\_be* to calculate local background error statistics.
- Global 3D-Var capability.

# WRF 4DVAR project

Supported by AFWA

The team: Dale, Hans, John, Qingnong, Wei Huang

## Schedule

- FY04: prepare. (wrf model, simplified model, testing TAF on wrf subroutines.)
- FY05: construct. (4DVAR framework, basic (dry) wrf TL and AD components, initial experiments.)
- FY06: refine. (more physics, parallel code, extensive testing.)

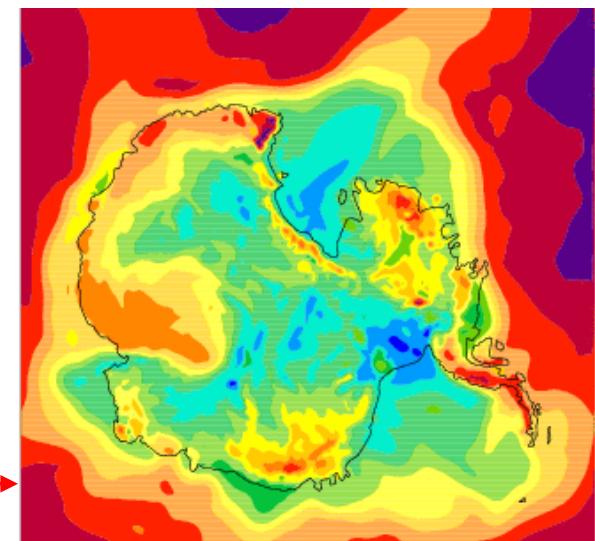


# NCAR/MMM WRF Advanced Data Assimilation (WG10) Plans

## WRF-Var:

- Further development of radar, GPS refractivity assimilation.
- Initial 4D-Var capability for AFWA (Oct. 2005).
- 4D-Var operational at AFWA (October 2007).
- Initial radiance capability (AMSU /RTTOVS) (Dec. 2005).
- Global 3D-Var operational at KMA (2006/2007).
- Applications (US, Korea, Taiwan, India, Antarctica).
- Flow-dependent covariances (Alpha CV, 4D-Var).

WRF 20km Antarctica:



## Unified WRF Data Assimilation System (WADAS?):

- Further comparison of EnKF and variational schemes.
- Combined variational and ensemble-based techniques.
- Leverages satellite radiance expertise of JCSDA, EUMETSAT, universities, etc.
- Suitable for MMM research, operations, and academic community use.

Alpha CV: T response to wind ob:

