

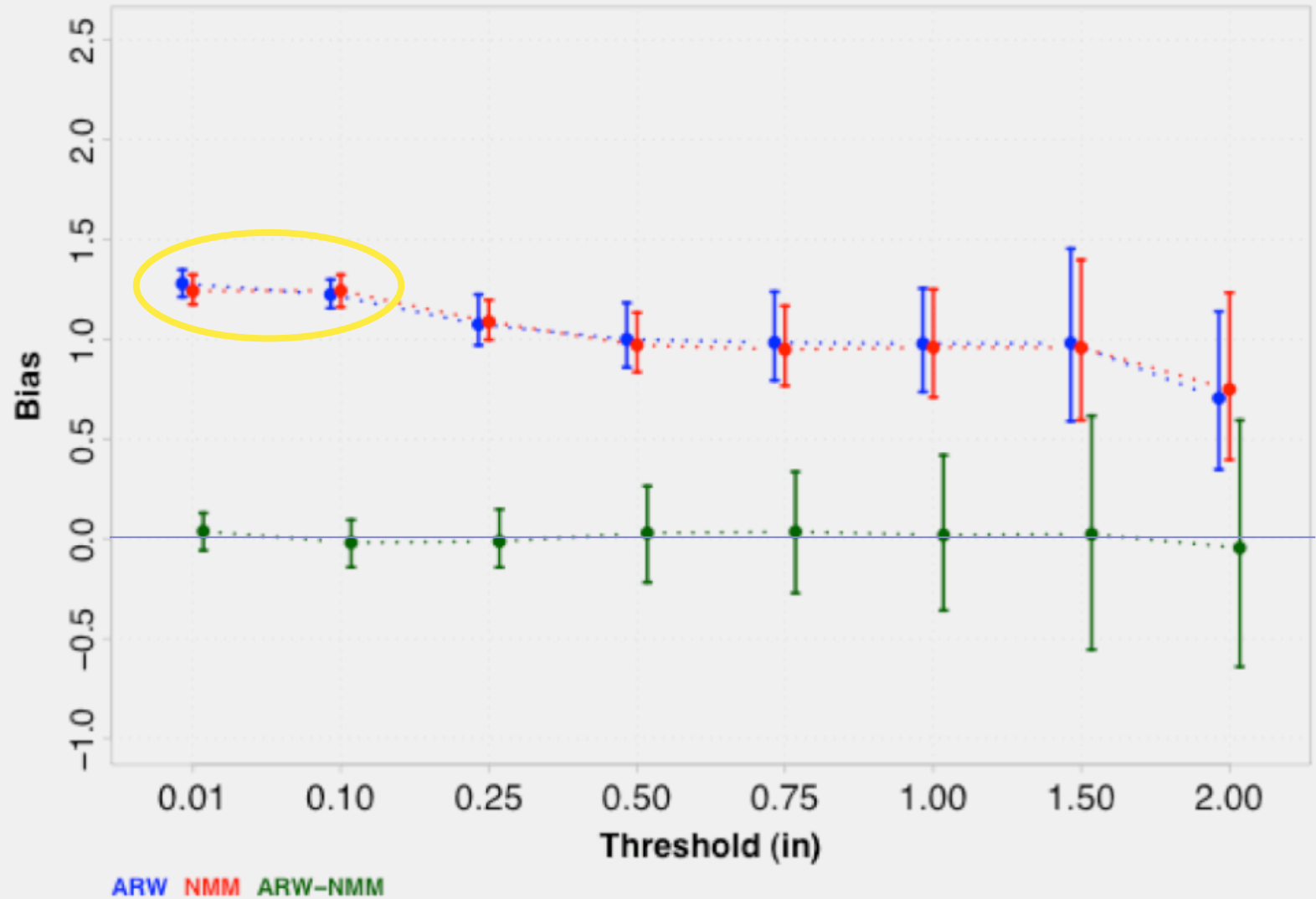
Giving meaning to your forecast verification results

Barbara Brown bgb@ucar.edu

- What does $\text{RMSE} = 25$ mean?
- Is 25 a good value? (What is “good”?)
- Is 25 better than 30?

Answer: It depends!!

24-h Accumulated Precipitation Bias (60-h forecast)



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Accounting for Uncertainty

- Observational
- Model
 - Model parameters
 - Physics
 - Verification scores
- Sampling
 - Verification statistic is a realization of a random process
 - What if the experiment were re-run under identical conditions?



Hypothesis Testing and Confidence Intervals

- Hypothesis testing
 - Given a null hypothesis (e.g., “*Model forecast is un-biased*”), is there enough evidence to reject it?
 - Can be *One-* or *two-sided*
 - Test is against a *single null hypothesis*.
- Confidence intervals
 - Related to hypothesis tests, but more useful.
 - How confident are we that the true value of the statistic (e.g., bias) is different from a particular value?

Hypothesis Testing and Confidence Intervals

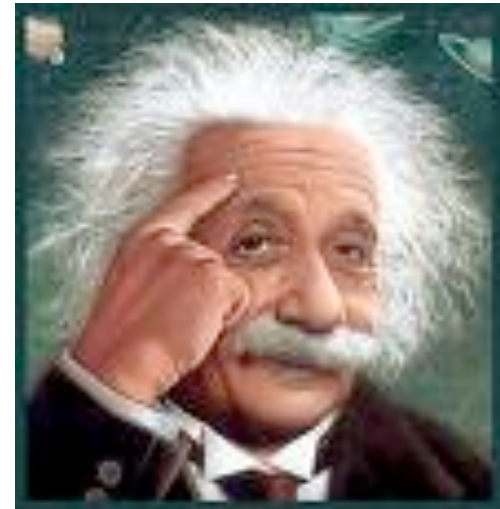
Example: The difference in bias between two models is 0.01.

Hypothesis test: Is this different from zero?

Confidence interval: Does zero fall within the interval? Does 0.5 fall within the interval?

Confidence Intervals (Cis)

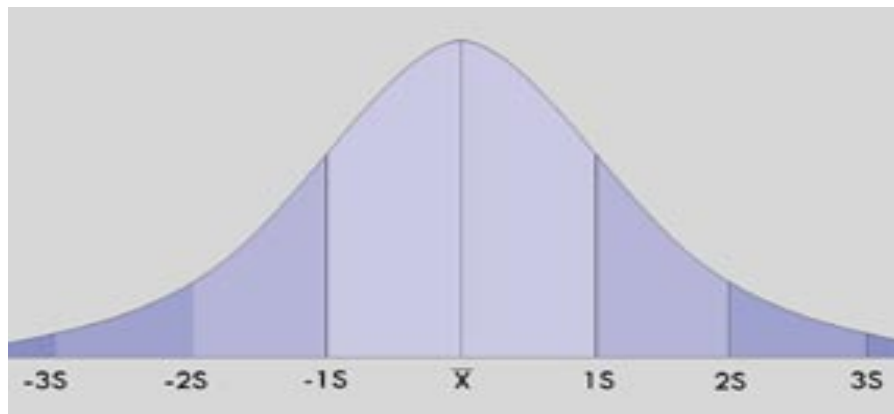
“If we re-run the experiment 100 times, and create 100 $(1-\alpha)100\%$ CI's, then *we expect the true value of the parameter to fall inside $(1-\alpha)100$ of the intervals.*”



Confidence intervals can be *parametric* or *non-parametric*...

Confidence Intervals (CI's)

- Parametric
 - Assume the observed sample is a realization from a known *population* distribution with possibly unknown parameters (e.g., normal).
 - Normal approximation CI's are most common.
 - Quick and easy.



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Confidence Intervals (CI's)

- Nonparametric
 - Assume the distribution of the observed sample is representative of the *population* distribution.
 - Bootstrap CI's are most common.
 - Can be computationally intensive, but easy enough.

Normal Approximation CI's

The diagram shows the formula for a Normal Approximation Confidence Interval: $\hat{\theta} \pm z_{\alpha/2} se(\theta)$. Red arrows point from descriptive text to parts of the formula: 'Estimate' points to $\hat{\theta}$, 'Standard normal variate' points to $z_{\alpha/2}$, and 'Population ("true") parameter' points to θ inside the $se()$ function.

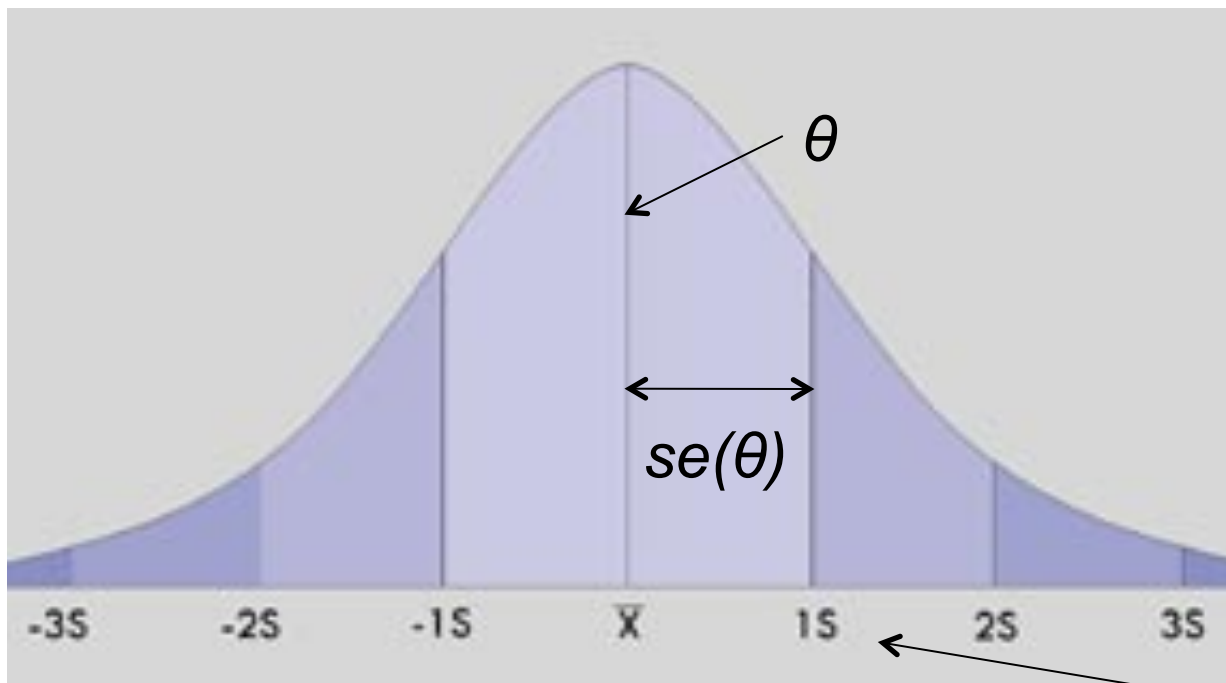
$$\hat{\theta} \pm z_{\alpha/2} se(\theta)$$

Is a $(1-\alpha)100\%$ Normal CI for Θ , where

- Θ is the statistic of interest (e.g., the forecast mean)
- $se(\Theta)$ is the standard error for the statistic
- z_v is the v -th quantile of the standard normal distribution.

Normal Approximation CI's

$$\hat{\theta} \pm z_{\alpha/2} se(\theta)$$



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(note: s = Standard error)

$z_{\alpha/2}$

Normal Approximation CI's

Example: Let X_1, \dots, X_n be an independent and identically distributed (iid) sample from a normal distribution with variance σ_X^2 .

Then, $\bar{X} = \frac{1}{n} \sum_{i=1}^n X_i$ is an estimate of the **mean**

of the sample. A $(1-\alpha)100\%$ CI for the mean is given by

$$\bar{X} \pm z_{\alpha/2} \frac{\sigma_X}{\sqrt{n}}$$

Note: You can find much more about these ideas in any basic statistics text book

Normal Approximation CI's

- Numerous verification statistics can take this approximation in some form or another
 - Alternative CIs are available for other types of variables
 - Examples: forecast/observation *variance*, linear *correlation*
 - Still rely on the underlying sample being iid normal.
- Contingency table verification scores also have normal approximation CI's (for large enough sample sizes)
 - Examples: *POD*, *FAR*

Application of Normal Approximation CI's

- Independence assumption (i.e., “iid”) – temporal and spatial
 - Should check the validity of the independence assumption
 - MET doesn't do this
 - Methods that can take into account dependencies will be added to MET in the future
- Normal distribution assumption
 - Should check validity of the normal distribution (e.g., qq-plots, other methods)
 - MET does not do this – should be done outside of MET
 - **However...** MET applies appropriate approaches for different verification statistics
- Multiple testing
 - When computing many confidence intervals, the true significance levels are affected (reduced) by the number of tests that are done

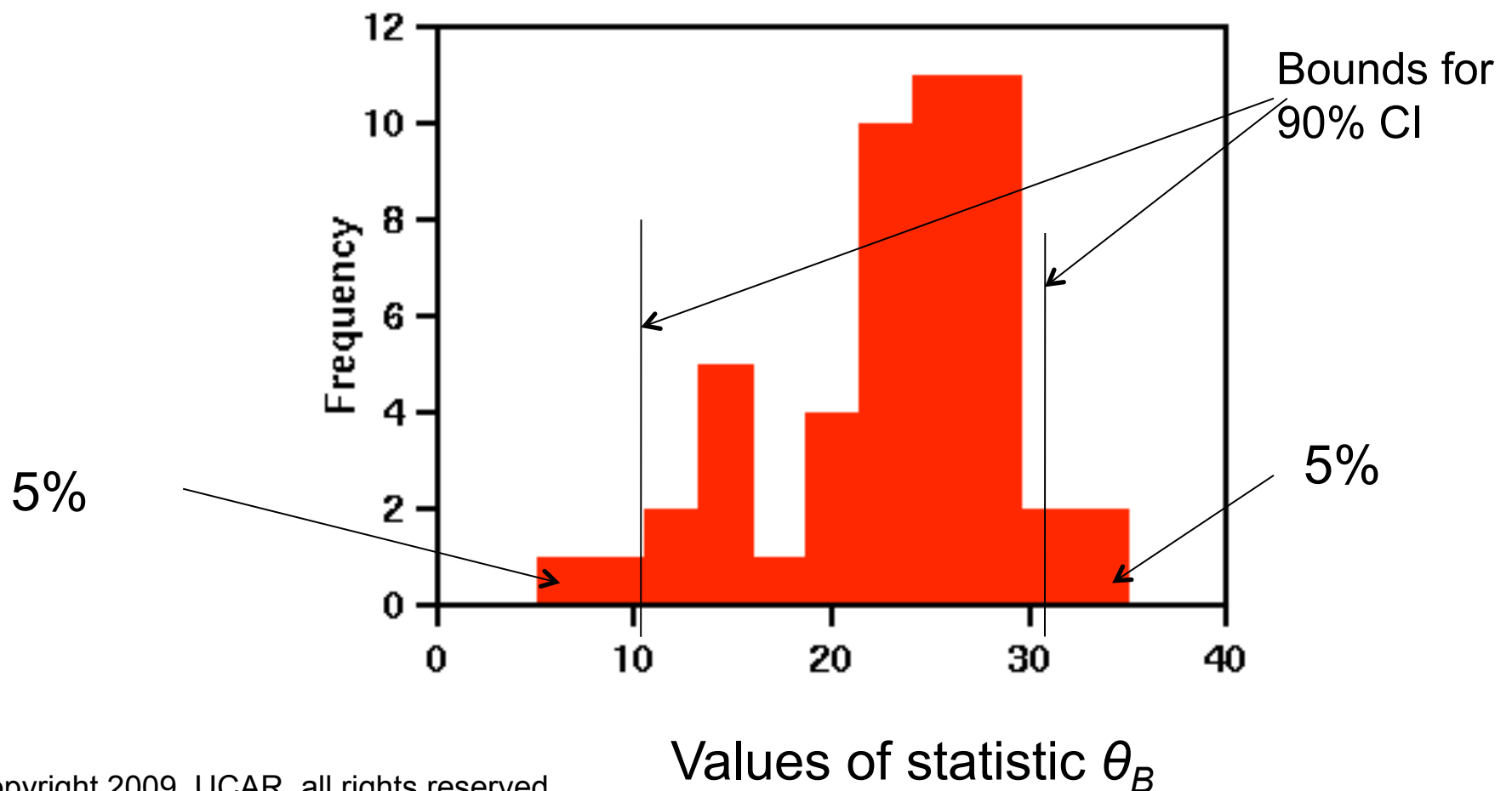


(Nonparametric) Bootstrap CI's

IID Bootstrap Algorithm

1. Resample *with replacement* from the sample,
 X_1, \dots, X_n .
2. Calculate the verification statistic(s) of interest from the resample in step 1.
3. Repeat steps 1 and 2 many times, say B times, to obtain a sample of the verification statistic(s) θ_B .
4. Estimate $(1-\alpha)100\%$ CI's from the sample in step 3.

Empirical Distribution (Histogram) of statistic calculated on repeated samples



Bootstrap CI's

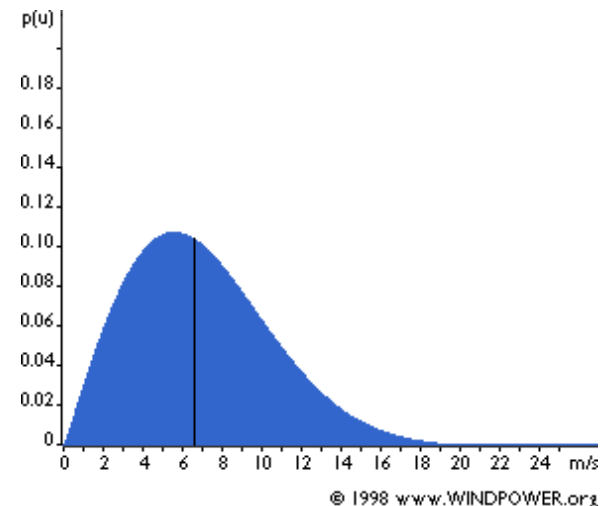
IID Bootstrap Algorithm: **Types of CI's**

1. Percentile Method CI's
2. Bias-corrected and adjusted (BCa)
3. ABC
4. Basic bootstrap CI's
5. Normal approximation
6. Bootstrap-t

} Available
in MET

Bootstrap CI's

- **Sample size** is a configurable parameter in MET
- **Typical approach:** Use same sample size as the original sample
 - Sometimes better to take smaller samples (e.g., heavy-tailed distributions; see Gilleland, 2008).



Practical Considerations

- Availability of CI methods
 - Normal CI is only available for appropriate statistics
 - Bootstrap is available for all/most statistical measures
- Bootstrap can be disabled in MET
- Number of points impacts speed of bootstrap
 - Grid-stat typically uses more points than Point-stat
 - THUS: Bootstrap is quicker with Point-stat.
- May be computationally inefficient to bootstrap over an entire field (e.g., several thousand points)
 - Alternative: Bootstrap the statistics for each field over time.
 - Measures (between-field) uncertainty of the estimates over time, rather than the within field uncertainty.

Practical Considerations

- Normal approximation intervals are quick, and generally accurate
 - Only valid for certain measures
- MET assumes that the samples are independent (probably not totally valid)

Thank you. Questions?

For more information, see:

Developmental Testbed Center, 2009. Model Evaluation Tools User's Guide. Available at:

<http://www.dtcenter.org/met/>

Gilleland E, 2008. Confidence intervals for forecast verification. *Submitted* as an NCAR Technical Note. Available at:

<http://www.ral.ucar.edu/~ericg/Gilleland2008.pdf>

Also look at basic statistical methods textbooks for information on confidence interval methods