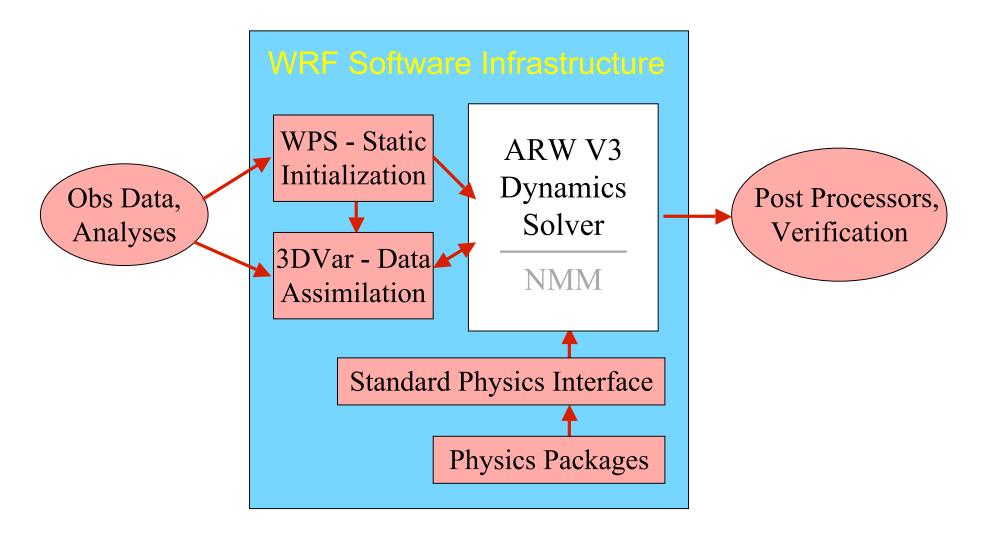
# The Advanced Research WRF (ARW) Dynamics Solver

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#### **WRF ARW Tech Note**

A Description of the Advanced Research WRF Version 3 http://www.mmm.ucar.edu/wrf/users/pub-doc.html

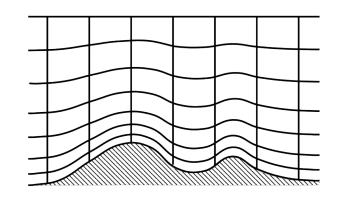
## **ARW Dynamical Solver**

- Terrain representation
- Vertical coordinate
- Equations / variables
- Time integration scheme
- Grid staggering
- Advection scheme
- Time step parameters
- Filters
- Boundary conditions
- Nesting
- Map projections

#### ARW, Terrain Representation

Lower boundary condition for the geopotential  $(\phi = gz)$  specifies the terrain elevation, and specifying the lowest coordinate surface to be the terrain results in a terrain-following coordinate.

$$\frac{\partial \phi}{\partial t} + u \frac{\partial \phi}{\partial x} + v \frac{\partial \phi}{\partial y} + \omega \frac{\partial \phi}{\partial \eta} = gw$$



Vertical coordinate:

hydrostatic pressure 
$$\pi$$
  $\eta = \frac{(\pi_d - \pi_{dt})}{\mu_d}, \quad \mu_d = \pi_{ds} - \pi_{dt}$ 

## Flux-Form Equations in ARW

Terrain-following hydrostatic pressure coordinate:

hydrostatic pressure  $\pi$ 

$$\eta = \frac{(\pi_d - \pi_{dt})}{\mu_d}, \quad \mu_d = \pi_{ds} - \pi_{dt}, \quad \mu_d(x, y)\Delta \eta = \Delta \pi_d = -g\rho_d \Delta z$$

Conserved state variables:

$$\mu_d$$
,  $U = \mu_d u$ ,  $V = \mu_d v$ ,  $W = \mu_d w$ ,  $\Theta = \mu_d \theta$ 

Non-conserved state variable:  $\phi = gz$ 

## 2D Flux-Form Moist Equations in ARW

Moist Equations:

$$\frac{\partial U}{\partial t} + \alpha \mu_d \frac{\partial p}{\partial x} + \frac{\alpha}{\alpha_d} \frac{\partial p}{\partial \eta} \frac{\partial \phi}{\partial x} = -\frac{\partial Uu}{\partial x} - \frac{\partial \Omega u}{\partial \eta}$$

$$\frac{\partial W}{\partial t} + g \left( \mu_d - \frac{\alpha}{\alpha_d} \frac{\partial p}{\partial \eta} \right) = -\frac{\partial Uw}{\partial x} - \frac{\partial \Omega w}{\partial \eta}$$

$$\frac{\partial \mu_d}{\partial t} + \frac{\partial U}{\partial x} + \frac{\partial \Omega}{\partial \eta} = 0$$

$$\frac{\partial \Theta}{\partial t} + \frac{\partial U\theta}{\partial x} + \frac{\partial \Omega\theta}{\partial \eta} = \mu Q$$

$$\frac{\partial \theta}{\partial t} = gw$$

$$\frac{\partial (\mu_d q_{v,l})}{\partial t} + \frac{\partial (U q_{v,l})}{\partial x} + \frac{\partial (\Omega q_{v,l})}{\partial \eta} = \mu Q_{v,l}$$

Diagnostic relations:

$$\frac{\partial \phi}{\partial \eta} = -\alpha_d \mu_d, \quad p = \left(\frac{R\Theta}{p_o \mu_d \alpha_v}\right)^{\gamma}$$

## Time Integration in ARW

## 3<sup>rd</sup> Order Runge-Kutta time integration

advance 
$$\phi^t \rightarrow \phi^{t+\Delta t}$$

$$\phi^* = \phi^t + \frac{\Delta t}{3} R(\phi^t)$$

$$\phi^{**} = \phi^t + \frac{\Delta t}{2} R(\phi^*)$$

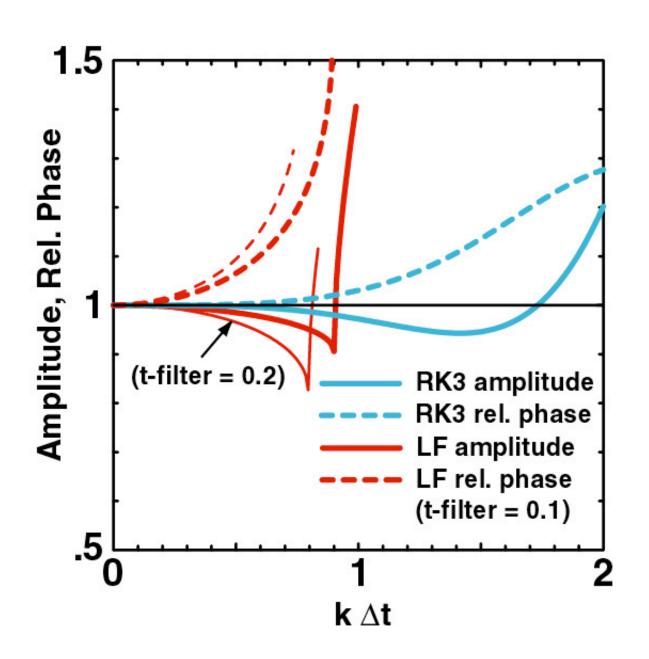
$$\phi^{t+\Delta t} = \phi^t + \Delta t R(\phi^{**})$$

Amplification factor 
$$\phi_t = ik\phi$$
;  $\phi^{n+1} = A\phi^n$ ;  $|A| = 1 - \frac{(k\Delta t)^4}{24}$ 

#### Phase and amplitude errors for LF, RK3

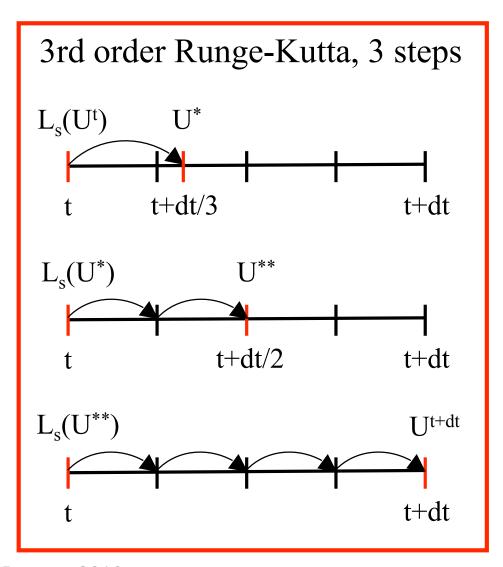
Oscillation equation analysis

$$\phi_t = ik\phi$$



## Time-Split Runge-Kutta Integration Scheme

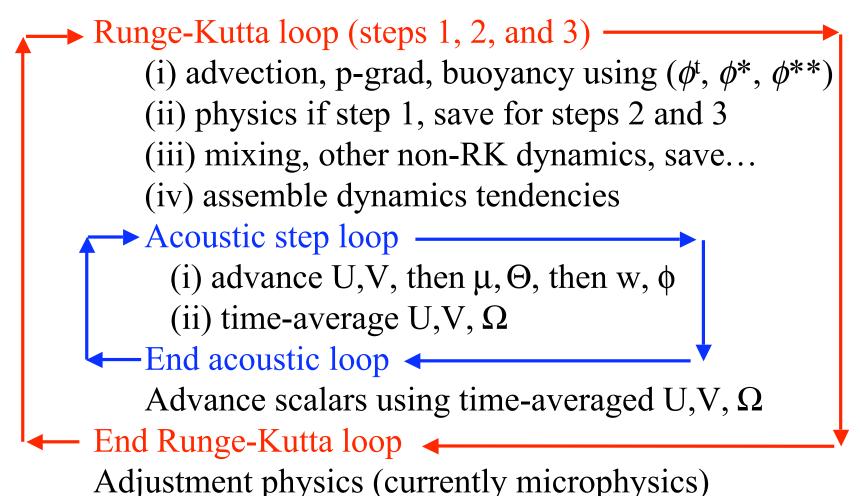
$$U_{t} = L_{fast}(U) + L_{slow}(U)$$



- RK3 is 3rd order accurate for linear eqns, 2nd order accurate for nonlinear eqns.
- Stable for centered and upwind advection schemes.
- Stable for Courant number Udt/dx < 1.73
- Three  $L_{slow}(U)$  evaluations per timestep.

## WRF ARW Model Integration Procedure

#### Begin time step



End time step

#### Flux-Form Perturbation Equations

Introduce the 
$$\phi = \overline{\phi}(\overline{z}) + \phi', \ \mu = \overline{\mu}(\overline{z}) + \mu';$$
 perturbation variables:  $p = \overline{p}(\overline{z}) + p', \ \alpha = \overline{\alpha}(\overline{z}) + \alpha'$ 

Note – 
$$\phi = \overline{\phi}(\overline{z}) = \overline{\phi}(x, y, \eta),$$
  
likewise  $\overline{p}(x, y, \eta), \overline{\alpha}(x, y, \eta)$ 

Reduces horizontal pressure-gradient errors.

For small time steps, recast variables as perturbations from time t

$$U' = U'^{t} + U'', \ V' = V'^{t} + V'', \ W' = W'^{t} + W'',$$

$$\Theta' = \Theta'^{t} + \Theta'', \ \mu' = \mu'^{t} + \mu'', \ \phi' = \phi'^{t} + \phi'';$$

$$p' = p'^{t} + p'', \ \alpha' = \alpha'^{t} + \alpha''$$

Allows vertical pressure gradient to be expressed in terms of  $\phi$ ".

#### Small Time Step Integration of Acoustic/Gravity Wave Terms

(Without expanding variables into perturbation form)

$$U^{\tau+\Delta\tau} \qquad \frac{\partial U}{\partial t} + \left(\mu_{d}\alpha \frac{\partial p}{\partial x} + \frac{\alpha}{\alpha_{d}} \frac{\partial p}{\partial \eta} \frac{\partial \phi}{\partial x}\right)^{\tau} = R_{U}^{t}$$

$$\mu_{d}^{\tau+\Delta\tau} \qquad \Omega^{\tau} \qquad \frac{\partial \mu_{d}}{\partial t} + \frac{\partial U}{\partial x}^{\tau+\Delta\tau} + \frac{\partial \Omega}{\partial \eta}^{\tau+\Delta\tau} = 0$$

$$\Theta^{\tau+\Delta\tau} \qquad \frac{\partial \Theta}{\partial t} + \left(\frac{\partial U\theta^{t}}{\partial x} + \frac{\partial \Omega\theta^{t}}{\partial \eta}\right)^{\tau+\Delta\tau} = R_{\Theta}^{t}$$

$$W^{\tau+\Delta\tau} \qquad \frac{\partial W}{\partial t} + g\left(\mu_{d} - \frac{\alpha}{\alpha_{d}} \frac{\partial p}{\partial \eta}\right)^{\tau} = R_{W}^{t}$$

$$\phi^{\tau+\Delta\tau} \qquad \mu_{d}^{t} \frac{\partial \phi}{\partial t} + U^{\tau+\Delta\tau} \frac{\partial \phi^{t}}{\partial x} + \Omega^{\tau+\Delta\tau} \frac{\partial \phi^{t}}{\partial \eta} - g\overline{W}^{\tau} = R_{\phi}^{t}$$

- Forward-backward differencing on U,  $\Theta$ , and  $\mu$  equations
- Vertically implicit differencing on W and  $\phi$  equations

## **Hydrostatic Option**

Instead of solving vertically implicit equations for W and  $\phi$ 

Integrate the hydrostatic equation to obtain  $p(\pi)$ :

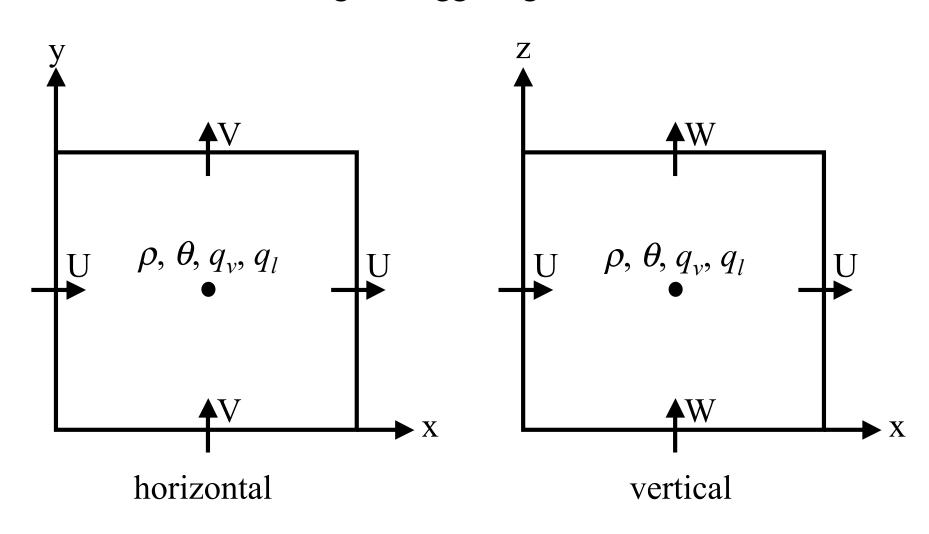
$$\frac{\partial p}{\partial \eta} = \left(\frac{\alpha_d}{\alpha}\right)^t \mu$$

Recover 
$$\alpha$$
 and  $\phi$  from:  $p = p_0 \left(\frac{R\theta}{p_0 \alpha_v}\right)^{\gamma}$ , and  $\frac{\partial \phi}{\partial \eta} = -\mu_d \alpha_d$ 

W is no longer required during the integration.

## ARW model, grid staggering

#### C-grid staggering



#### Advection in the ARW Model

2<sup>nd</sup>, 3<sup>rd</sup>, 4<sup>th</sup>, 5<sup>th</sup> and 6<sup>th</sup> order centered and upwind-biased schemes are available in the ARW model.

Example: 5<sup>th</sup> order scheme

$$\frac{\partial (U\phi)}{\partial x} = \frac{1}{\Delta x} \left( F_{i+\frac{1}{2}}(U\phi) - F_{i-\frac{1}{2}}(U\phi) \right)$$

where

$$F_{i-\frac{1}{2}}(U\phi) = U_{i-\frac{1}{2}} \left\{ \frac{37}{60} (\phi_i + \phi_{i-1}) - \frac{2}{15} (\phi_{i+1} + \phi_{i-2}) + \frac{1}{60} (\phi_{i+2} + \phi_{i-3}) \right\}$$

$$-sign(1,U) \frac{1}{60} \left\{ (\phi_{i+2} - \phi_{i-3}) - 5 (\phi_{i+1} - \phi_{i-2}) + 10 (\phi_i - \phi_{i-1}) \right\}$$

#### Advection in the ARW Model

For constant U, the 5<sup>th</sup> order flux divergence tendency becomes

$$\Delta t \frac{\delta \left(U\phi\right)}{\Delta x} \bigg|_{5th} = \Delta t \frac{\delta \left(U\phi\right)}{\Delta x} \bigg|_{6th}$$

$$- \left| \frac{U\Delta t}{\Delta x} \right| \frac{1}{60} \left(-\phi_{i-3} + 6\phi_{i-2} - 15\phi_{i-1} + 20\phi_{i} - 15\phi_{i+1} + 6\phi_{i+2} - \phi_{i+3}\right)$$

$$\frac{Cr}{60} \frac{\partial^{6}\phi}{\partial x^{6}} + H.O.T$$

The odd-ordered flux divergence schemes are equivalent to the next higher ordered (even) flux-divergence scheme plus a dissipation term of the higher even order with a coefficient proportional to the Courant number.

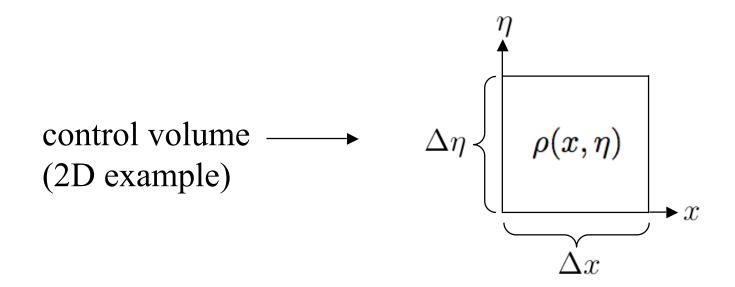
#### Maximum Courant Number for Advection

$$C_a = U\Delta t / \Delta x$$

Time Integration Scheme	Advection Scheme				
	$2^{nd}$	$3^{rd}$	$\mathcal{4}^{th}$	$5^{th}$	$6^{th}$
Leapfrog (α=0.1)	0.91	U	0.66	U	0.57
RK2	U	0.90	U	0.39	U
RK3	1.73	1.63	1.26	1.43	1.09

U = unstable

(Wicker & Skamarock, 2002)



Mass in a control volume is proportional to

$$(\Delta x \Delta \eta)(\mu)^t$$

since 
$$\mu(x)\Delta\eta = \Delta\pi = -g\rho\Delta z$$

Mass in a control volume  $(\Delta x \Delta \eta)(\mu)^t$ 2D example

Mass conservation equation

$$\Delta t^{-1}(\Delta x \Delta \eta) \cdot \left[ (\mu)^{t+\Delta t} - (\mu)^t \right] = \left[ (\mu u \Delta \eta)_{x-\Delta x/2,\eta} - (\mu u \Delta \eta)_{x+\Delta x/2,\eta} \right] + \left[ (\mu \omega \Delta x)_{x,\eta-\Delta \eta/2} - (\mu \omega \Delta x)_{x,\eta+\Delta \eta/2} \right]$$

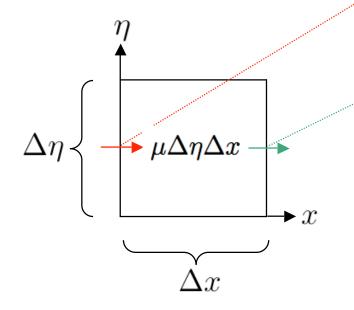
Change in mass over a time step

mass fluxes through control volume faces

Mass in a control volume  $(\Delta x \Delta \eta)(\mu)^t$ 

Mass conservation equation

$$\Delta t^{-1}(\Delta x \Delta \eta) \cdot \left[ (\mu)^{t+\Delta t} - (\mu)^t \right] = \left[ (\mu u \Delta \eta)_{x-\Delta x/2,\eta} - (\mu u \Delta \eta)_{x+\Delta x/2,\eta} \right] + \left[ (\mu \omega \Delta x)_{x,\eta-\Delta \eta/2} - (\mu \omega \Delta x)_{x,\eta+\Delta \eta/2} \right]$$



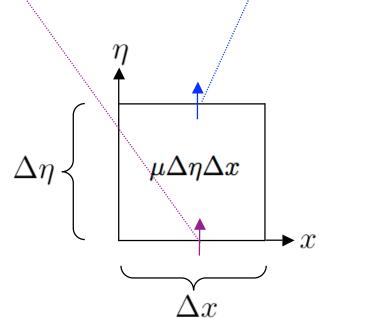
Horizontal fluxes through the vertical control-volume faces

Mass in a control volume  $(\Delta x \Delta \eta)(\mu)^t$ 

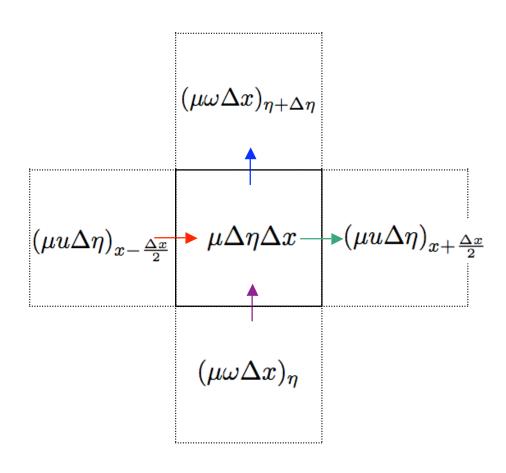
Mass conservation equation

$$\Delta t^{-1}(\Delta x \Delta \eta) \cdot \left[ (\mu)^{t+\Delta t} - (\mu)^t \right] = \left[ (\mu u \Delta \eta)_{x-\Delta x/2,\eta} - (\mu u \Delta \eta)_{x+\Delta x/2,\eta} \right] + \left[ (\mu \omega \Delta x)_{x,\eta-\Delta \eta/2} - (\mu \omega \Delta x)_{x,\eta+\Delta \eta/2} \right]$$

Vertical fluxes through the horizontal control-volume faces



The same mass fluxes are used for neighboring grid cells - hence mass is conserved locally and globally.



Mass in a control volume  $(\Delta x \Delta \eta)(\mu)^t$ 

Scalar mass  $(\Delta x \Delta \eta)(\mu \phi)^t$ 

Mass conservation equation:

$$\frac{\Delta t^{-1}(\Delta x \Delta \eta) \cdot \left[ (\mu)^{t+\Delta t} - (\mu)^t \right]}{ \left[ (\mu u \Delta \eta)_{x-\Delta x/2,\eta} - (\mu u \Delta \eta)_{x+\Delta x/2,\eta} \right] + \left[ (\mu u \Delta x)_{x,\eta-\Delta \eta/2} - (\mu u \Delta x)_{x,\eta+\Delta \eta/2} \right] }$$

change in mass over a time step

mass fluxes through control volume faces

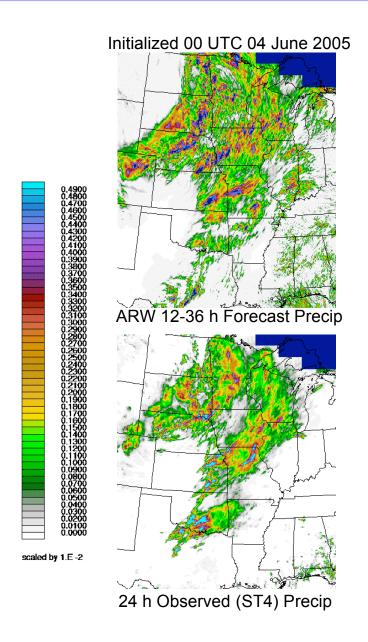
Scalar mass conservation equation:

$$\Delta t^{-1}(\Delta x \Delta \eta) \cdot \left[ (\mu \phi)^{t+\Delta t} - (\mu \phi)^t \right] = \left[ (\mu u \phi \Delta \eta)_{x-\Delta x/2,\eta} - (\mu u \phi \Delta \eta)_{x+\Delta x/2,\eta}) \right] + \left[ (\mu \omega \phi \Delta x)_{x,\eta-\Delta \eta/2} - (\mu \omega \phi \Delta x)_{x,\eta+\Delta \eta/2}) \right]$$

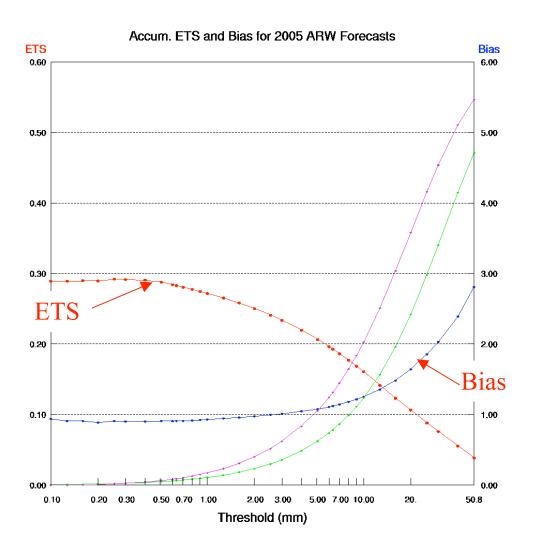
change in tracer mass over a time step

tracer mass fluxes through control volume faces

## Moisture Transport in ARW: High Precipitation Bias

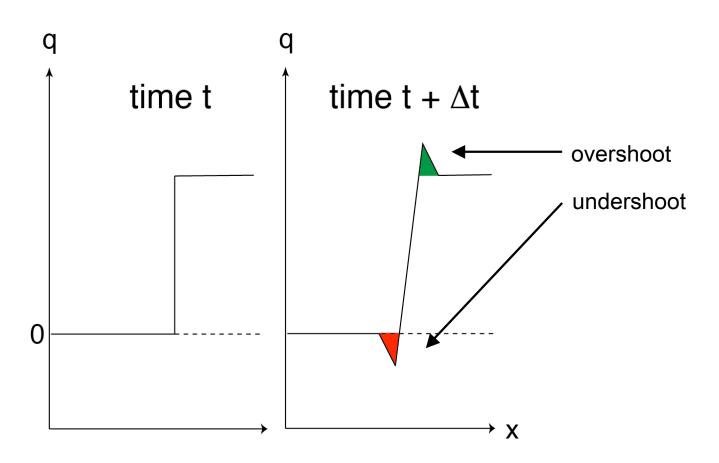


#### 2005 ARW 4 km Forecasts:



#### Moisture Transport in ARW

1D advection



ARW scheme is conservative, but not positive definite nor monotonic. Removal of negative q results in spurious source of q .

#### Positive-Definite/Monotonic Flux Renormalization

Scalar update, last RK3 step

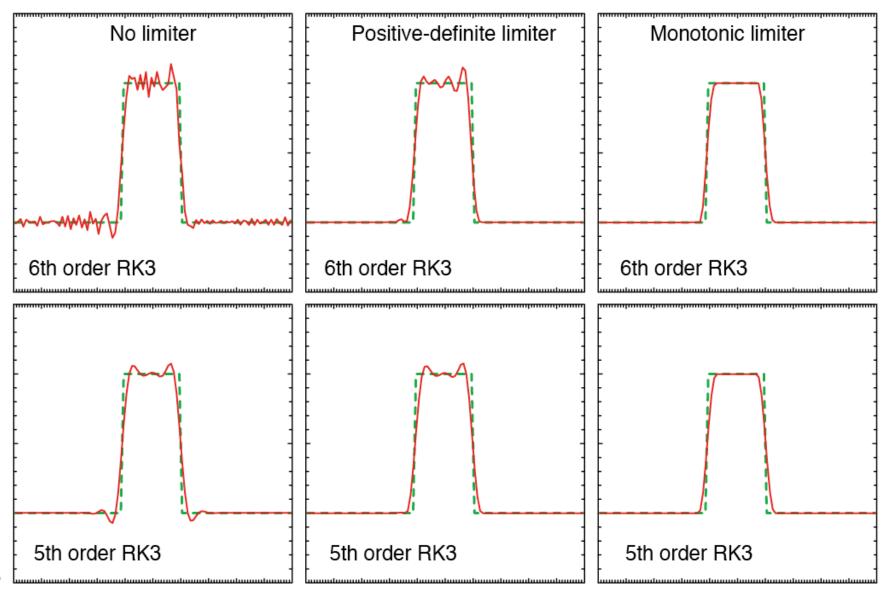
$$(\mu\phi)^{t+\Delta t} = (\mu\phi)^t - \Delta t \sum_{i=1}^n \delta_{x_i}[f_i]$$
 (1)

- (1) Decompose flux:  $f_i = f_i^{upwind} + f_i^c$
- (2) Renormalize high-order correction fluxes  $f_i^c$  such that solution is positive definite or monotonic:  $f_i^c = R(f_i^c)$
- (3) Update scalar eqn. (1) using  $f_i = f_i^{upwind} + R(f_i^c)$

Skamarock, MWR 2006, 2241-2250

## PD/Monotonic Limiters in ARW - 1D Example Top-Hat Advection

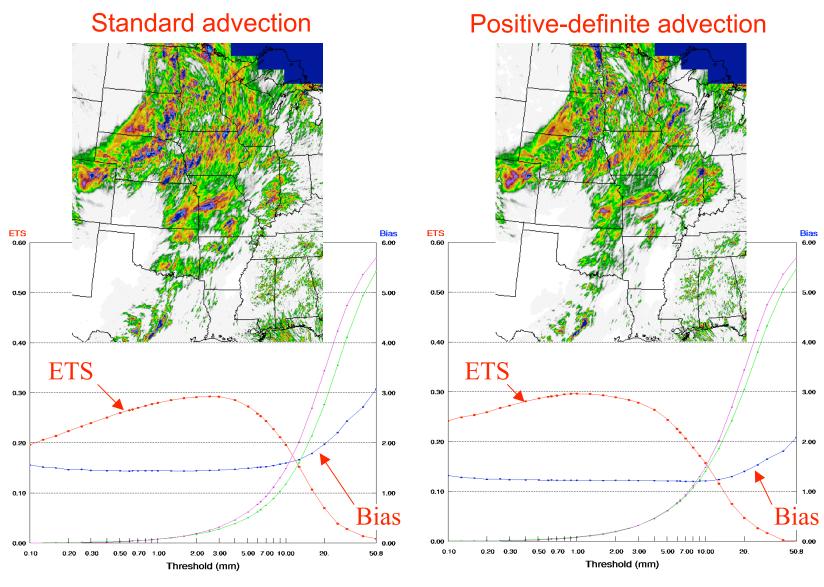
1D Top-hat transport Cr = 0.5, 1 revolution, 200 steps



January

## Moisture Transport in ARW: 24 h ETS and BIAS





## **ARW Model: Dynamics Parameters**

#### 3<sup>rd</sup> order Runge-Kutta time step

Courant number limited, 1D: 
$$C_r = \frac{U\Delta t}{\Delta x} < 1.43$$

Generally stable using a timestep approximately twice as large as used in a leapfrog model.

#### Acoustic time step

2D horizontal Courant number limited: 
$$C_r = \frac{C_s \Delta \tau}{\Delta h} < \frac{1}{\sqrt{2}}$$
  
 $\Delta \tau_{sound} = \Delta t_{RK} / \text{(number of acoustic steps)}$ 

#### Guidelines for time step

 $\Delta t$  in seconds should be about  $6*\Delta x$  (grid size in kilometers). Larger  $\Delta t$  can be used in smaller-scale dry situations, but  $time\_step\_sound$  (default = 4) should increase proportionately if larger  $\Delta t$  is used.

## **ARW Filters: Divergence Damping**

Purpose: filter acoustic modes (3-D divergence,  $D = \nabla \cdot \rho \mathbf{V}$ )

$$\left\{ \frac{\partial \rho \mathbf{V}}{\partial t} + \nabla p + \ldots = \gamma_d' \nabla D \right\}$$

$$\nabla \cdot \left\{ \quad \right\} \quad \rightarrow \quad \frac{\partial D}{\partial t} + \nabla^2 p + \ldots = \gamma_d' \nabla^2 D$$

From the pressure equation:  $p_t \simeq c^2 D$ 

$$\frac{\partial \rho \mathbf{V}}{\partial t} + \nabla [p_{\tau} + \gamma_d (p^{\tau} - p^{\tau - \Delta \tau})] + \dots = 0$$

 $\gamma_d = 0.1$  recommended (default)

(Illustrated in height coordinates for simplicity)

## ARW Filters: Vertically Implicit Off-Centered Acoustic Step

Purpose: damp vertically-propagating acoustic modes

$$\frac{\partial W}{\partial t} + g \overline{\left(\mu_d - \frac{\alpha}{\alpha_d} \frac{\partial p}{\partial \eta}\right)^{\tau}} = \dots$$

$$\frac{\partial \phi}{\partial t} - \frac{g}{\mu_d^t} \overline{W}^{\tau} = \dots$$

$$\overline{(\phantom{A})^{\tau}} = \frac{1 + \beta}{2} \overline{(\phantom{A})^{\tau + \Delta \tau}} + \frac{1 - \beta}{2} \overline{(\phantom{A})^{\tau}}$$

Slightly forward centering the vertical pressure gradient damps 3-D divergence as demonstrated for the divergence damper

$$\beta$$
= 0.1 recommended (default)

#### ARW Filters: External Mode Filter

Purpose: filter the external mode

Vertically integrated horizontal divergence,  $D_h = \int_1^0 (\nabla_{\eta} \cdot \mu \mathbf{V}_h) d\eta$ 

$$\left\{ \frac{\partial \mu \mathbf{V}_h}{\partial t} + \ldots = -\gamma_e \nabla_{\eta} D_h \right\}$$

$$\int_{1}^{0} \nabla_{\eta} \cdot \left\{ \right\} d\eta \quad \to \quad \frac{\partial D_{h}}{\partial t} + \dots = \gamma_{e} \nabla^{2} D_{h}$$

Continuity equation:  $\frac{\partial \mu}{\partial t} = -\nabla_{\eta} \cdot \mu \mathbf{V}_h - \frac{\partial \mu \dot{\eta}}{\partial \eta} = D_h$ 

$$\frac{\partial \mu \mathbf{V}_h}{\partial \tau} + \dots = -\gamma_e \frac{\Delta x^2}{\Delta \tau^2} \nabla_{\eta} (\mu^{\tau} - \mu^{\tau - \Delta \tau})$$

 $\gamma_e = 0.01$  recommended (default)

(Primarily for real-data applications)

## **ARW Filters: Vertical Velocity Damping**

#### Purpose: damp anomalously-large vertical velocities

(usually associated with anomalous physics tendencies)

#### Additional term:

$$\partial_t W = \dots - \mu_d \operatorname{sign}(W) \gamma_w (Cr - Cr_\beta)$$

$$Cr = \left| \frac{\Omega dt}{\mu d\eta} \right|$$

$$Cr_{\beta}$$
=1.0 typical value (default)  
 $\gamma_{w}$  = 0.3 m/s<sup>2</sup> recommended (default)

## ARW Filters: 2nd-Order Horizontal Mixing, Horizontal-Deformation-Based K<sub>h</sub>

Purpose: mixing on horizontal coordinate surfaces (real-data applications)

$$K_h = C_s^2 l^2 \left[ 0.25(D_{11} - D_{22})^2 + \overline{D_{12}^2}^{xy} \right]^{\frac{1}{2}}$$

where 
$$l = (\Delta x \Delta y)^{1/2}$$

$$D_{11} = 2 m^{2} [\partial_{x}(m^{-1}u) - z_{x}\partial_{z}(m^{-1}u)]$$

$$D_{22} = 2 m^{2} [\partial_{y}(m^{-1}v) - z_{y}\partial_{z}(m^{-1}v)]$$

$$D_{12} = m^{2} [\partial_{y}(m^{-1}u) - z_{y}\partial_{z}(m^{-1}u) + \partial_{x}(m^{-1}v) - z_{x}\partial_{z}(m^{-1}v)]$$

 $C_s = 0.25$  (Smagorinsky coefficient, default value)

## Implicit Rayleigh w Damping Layer for Split-Explicit Nonhydrostatic NWP Models (gravity-wave absorbing layer)

#### Modification to small time step:

 Step horizontal momentum, continuity, and potential temperature equations to new time level:

$$U^{\tau + \Delta \tau} \qquad \mu^{\tau + \Delta \tau}$$

$$\Omega^{\tau + \Delta \tau} \qquad \Theta^{\tau + \Delta \tau}$$

 Step vertical momentum and geopotential equations (implicit in the vertical):

$$W^{*\tau+\Delta\tau}$$
  $\phi^{*\tau+\Delta\tau}$ 

 Apply implicit Rayleigh damping on W as an adjustment step:

$$W^{\tau + \Delta \tau} = W^{*\tau + \Delta \tau} - \Delta \tau R_w(\eta) W^{\tau + \Delta \tau}$$

 Update final value of geopotential at new time level:

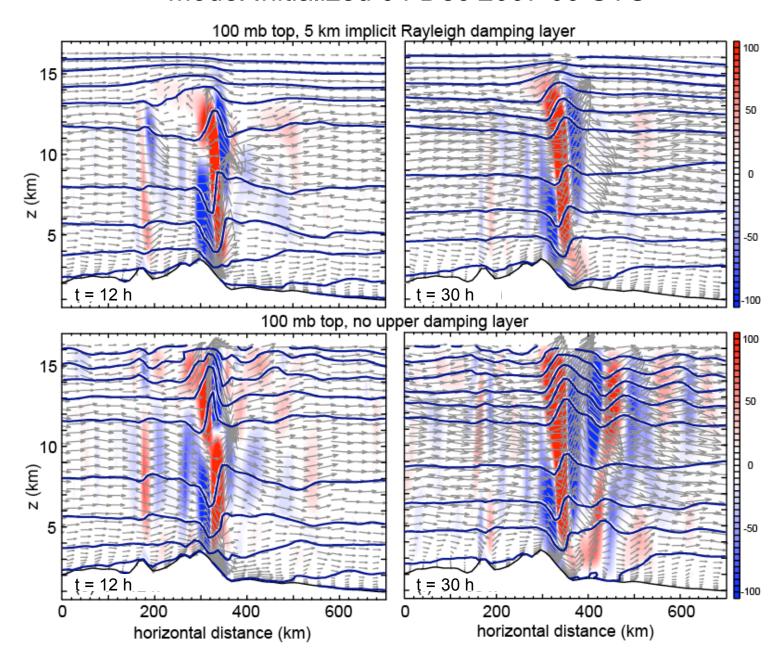
$$\phi^{\tau + \Delta \tau}$$

$$R_w(\eta) = \begin{cases} \gamma_r \sin^2 \left[ \frac{\pi}{2} \left( 1 - \frac{z_{top} - z}{z_d} \right) \right] & \text{for } z \ge (z_{top} - z_d); \\ 0 & \text{otherwise,} \end{cases}$$

$$\tau(z)$$
 - damping rate (t<sup>-1</sup>)  
 $z_d$  - depth of the damping layer  
 $\gamma_r$  - dimensionless damping coefficient

## WRF Forecast over Colorado Front Range

#### Model Initialized 04 Dec 2007 00 UTC

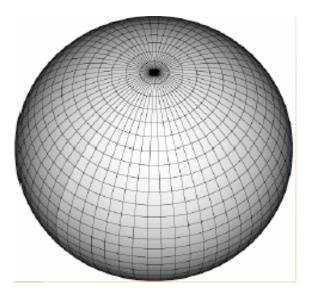


#### **ARW Model: Coordinate Options**

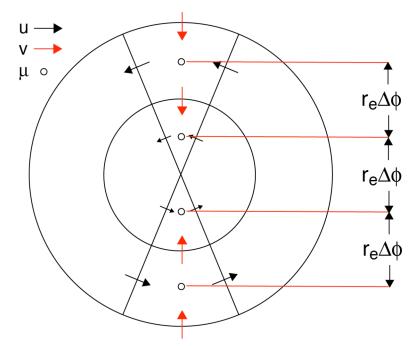
- 1. Cartesian geometry: idealized cases
- 2. Lambert Conformal: mid-latitude applications
- 3. Polar Stereographic: high-latitude applications
- 4. Mercator: low-latitude applications
- 5. Latitude-Longitude (new in ARW V3) global regional

Projections 1-4 are isotropic  $(m_x = m_y)$ Latitude-Longitude projection is anistropic  $(m_x \neq m_y)$ 

## Global ARW - Latitude-Longitude Grid



- Map factors m<sub>x</sub> and m<sub>y</sub>
  - Computational grid poles need not be geographic poles.
  - Limited area and nesting capable.
- Polar boundary conditions
- Polar filtering

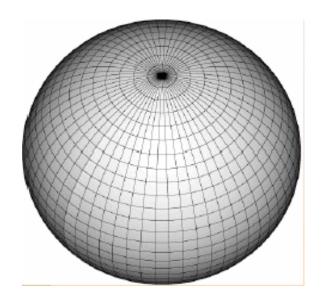


Zero meriodional flux at the poles (cell-face area is zero).

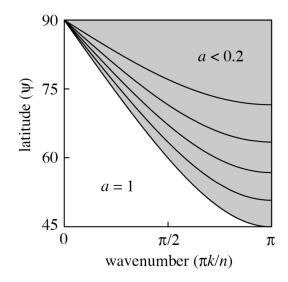
v (poles) only needed for meridional derivative of v near the poles (we interpolate).

All other meriodional derivatives are well-defined near/at poles.

## **ARW Filters: Polar Filter**



Filter Coefficient a(k),  $\psi_0 = 45^\circ$ 



Converging gridlines severely limit timestep. The polar filter removes this limitation.

Filter procedure - Along a grid latitude circle:

- 1. Fourier transform variable.
- 2. Filter Fourier coefficients.
- 3. Transform back to physical space.

$$\hat{\phi}(k)_{filtered} = a(k)\,\hat{\phi}(k), \text{ for all } k$$

$$a(k) = \min \left[ 1., \max \left( 0., \left( \frac{\cos \psi}{\cos \psi_o} \right)^2 \frac{1}{\sin^2(\pi k/n)} \right) \right]$$

k = dimensionless wavenumber

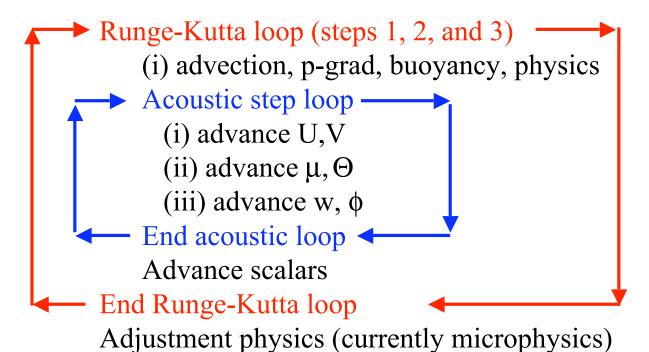
 $\hat{\phi}(k)$  = Fourier coefficients from forward transform

a(k) =filter coefficients

 $\psi = \text{ latitude } \psi_o = \text{ polar filter latitude, filter when } |\psi| > \psi_o$ 

## WRF ARW Model Integration Procedure

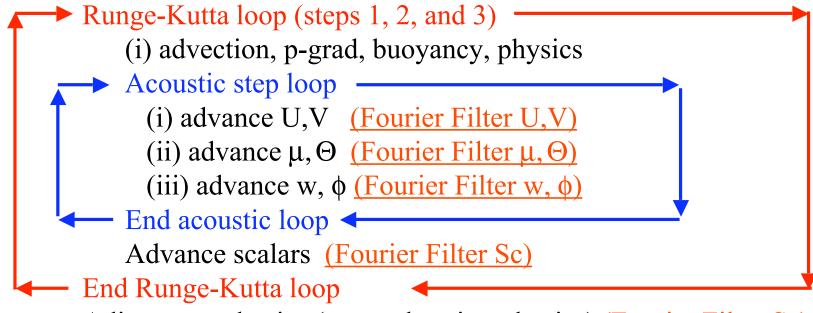
#### Begin time step



End time step

## WRF ARW Model Integration Procedure

Begin time step



Adjustment physics (currently microphysics) (Fourier Filter Sc)

End time step

Timestep limited by minimum  $\Delta x$  outside of polar-filter region. Monotonic and PD transport is not available for global model.

#### **ARW Model: Boundary Condition Options**

#### Lateral boundary conditions

- 1. Specified (Coarse grid, real-data applications).
- 2. Open lateral boundaries (gravity-wave radiative).
- 3. Symmetric lateral boundary condition (free-slip wall).
- 4. Periodic lateral boundary conditions.
- 5. Nested boundary conditions (specified).

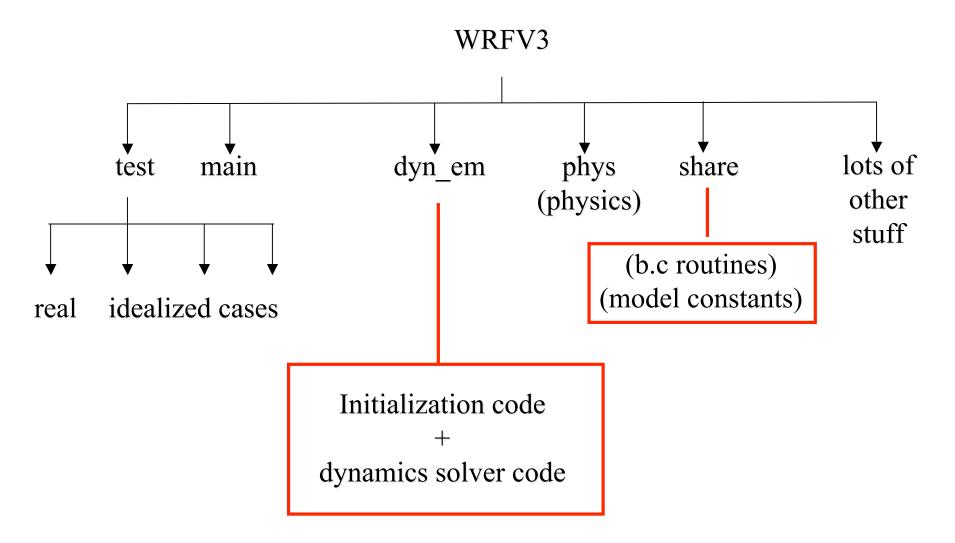
#### Top boundary conditions

1. Constant pressure.

#### Bottom boundary conditions

- 1. Free slip.
- 2. Various B.L. implementations of surface drag, fluxes.

## WRF ARW code



#### **WRF ARW Tech Note**

A Description of the Advanced Research WRF Version 3 (June 2008) http://www.mmm.ucar.edu/wrf/users/pub-doc.html