





WRF Four-Dimensional Data Assimilation (FDDA)

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FDDA

- Method of nudging model towards observations or analysis
- May be used for
 - Dynamical initialization (pre-forecast period)
 - Creating 4D meteorological datasets (e.g. for air quality model)
 - Boundary conditions (outer domain nudged towards analysis)

Method

- Model is run with extra nudging terms for horizontal winds, temperature and water vapor
- In analysis nudging, these terms nudge point-bypoint to a 3d space- and time-interpolated analysis field
- In obs-nudging, points near observations are nudged based on model error at obs site
- The nudging is a relaxation term with a user-defined time scale around an hour or more
- Nudging will work with nesting and restarts

Dynamic Initialization

- Model domains are nudged towards analysis in a pre-forecast period of 6-12 hours
- This has benefit of smooth start up at forecast time zero



Four-Dimensional Met Analysis

- Produces analyses between normal analysis times
- High-resolution balanced and mass-continuity winds can be output to drive off-line air quality models



Boundary Conditions

- Nudge an outer domain towards analysis through forecast
- This has benefit of providing smoother boundary conditions to domain of interest than if 15 km domain is the outer domain with interpolated-analysis boundary conditions



FDDA Methods

- Two Methods
 - Grid or analysis nudging (suitable for coarse resolution)
 - Observation or station nudging (suitable for fine-scale or asynoptic obs)
- Nudging can be applied to winds, temperature, and water vapor
- **Note:** nudging terms are fake sources, so avoid FDDA use in dynamics or budget studies

Analysis Nudging (grid_fdda=1)

• Each grid-point is nudged towards a value that is time-interpolated from analyses

$$\frac{\partial p^* \alpha}{\partial t} = F(\alpha, \mathbf{x}, t) + G_{\alpha} \cdot W_{\alpha} \cdot \epsilon_{\alpha}(\mathbf{x}) \cdot p^*(\hat{\alpha}_0 - \alpha)$$

In WRF p* is m and a is *u*,*v*,*T* or *q F* includes all the regular WRF terms

Analysis Nudging

$$\frac{\partial p^* \alpha}{\partial t} = F(\alpha, \mathbf{x}, t) + G_{\alpha} \cdot W_{\alpha} \cdot \epsilon_{\alpha}(\mathbf{x}) \cdot p^*(\hat{\alpha}_0 - \alpha)$$

- G is nudging inverse time scale
- W is vertical weight (upper air and surface)
- e is a horizontal weight for obs density (not implemented yet)

Analysis Nudging

- 3d analysis nudging uses the WRF input fields at multiple times that are put in wrffdda_d01 file by program real when run with grid_fdda=1
 - With low time-resolution analyses, it is recommended not to use 3d grid-nudging in the boundary layer, especially for temperature
- Surface (2d) analysis nudging available in Version 3.1
 - Nudges surface and boundary layer only

Analysis-Nudging namelist options

Can choose

- Frequency of nudging calculations (fgdt in minutes)
- Nudging time scale for each variable (guv, gt, gq in inverse seconds)
- Which variables not to nudge in the PBL (if_no_pbl_nudging_uv, etc.)
- Model level for each variable below which nudging is turned off (if_zfac_uv, k_zfac_uv, etc.)
- Ramping period over which nudging is turned off gradually (if_ramping, dt_ramp_min)

Surface Analysis Nudging

- In Version 3.1 added 2d (surface) nudging (grid_fdda=1 and grid_sfdda=1) for surface analyses
 - wrfsfdda_d01 file created by obsgrid.exe
 - Weights given by guv_sfc, gt_sfc, and gq_sfc
 - Note: grid_fdda=1 must be used to activate this. If upper-air nudging not wanted, set upper weights guv, gt, gq =0.

Spectral Nudging

- In Version 3.1 added spectral nudging (grid_fdda=2) to do 3d nudging of only selected larger scales
- This may be useful for controlling longer wave phases for long simulations. Compensates for error due to low-frequency lateral boundaries.
 - Top wavenumber nudged is selected in namelist (xwavenum, ywavenum, e.g. =3)
 - Typically choose so that (domain size)/(wavenumber)=~1000 km in each direction
 - Nudges u, v, theta, geopotential (not q)
 - Can nudge in all levels or use ramp above a specified model level (if_zfac_ph, k_zfac_ph, dk_zfac_ph, etc.)

Obs Nudging (obs_nudge_opt=1)

 Each grid point is nudged using a weighted average of differences from observations within a radius of influence and time window

$$egin{aligned} &rac{\partial p^* lpha}{\partial t} = F(lpha, \mathbf{x}, t) + G_lpha \cdot p^* rac{\sum_{i=1}^N W_i^2(\mathbf{x}, t) \cdot \gamma_i \cdot (lpha_o - \hat{lpha})_i}{\sum_{i=1}^N W_i(\mathbf{x}, t)} \ &W(\mathbf{x}, t) = w_{xy} \cdot w_\sigma \cdot w_t \end{aligned}$$



Note: errors at obs sites are weighted by distance for nudging

$$w_{xy} = rac{R^2 - D^2}{R^2 + D^2}$$
 $0 \le D \le R$

$$w_{xy} = 0$$
 $D > R,$

- R is radius of influence
- D is distance from ob modified by elevation difference

$$w_t = 1$$
 $|t - t_0| < \tau/2$
 $w_t = rac{ au - |t - t_0|}{ au/2}$ $au/2 \le |t - t_0| \le au$

• t is the specified time window for the obs

• This is a function that ramps up and down

 w_s is the vertical weighting – usually the vertical influence is set small (0.005 eta-difference) so that data is only assimilated on its own eta level

- obs input file is a special ascii file (OBS_DOMAIN101) with obs sorted in chronological order
 - each record is the obs (u, v, T, Q) at a given model position and time
 - •Utility programs exist to convert data to this format from other common formats
 - In V3.1 obsgrid.exe can create this file from standard observations that are in little_r format

Obs-Nudging namelist options

Can choose

- Frequency of nudging calculations (iobs_ionf)
- Nudging time scale for each variable (obs_coef_wind, etc.)
- Horizontal and vertical radius of influence (obs_rinxy, obs_rinsig)
- Time window (obs_twindo)
- Ramping period over which nudging is turned off gradually (obs_idynin, obs_dtramp)

Vertical weighting functions

- Added flexibility options for advanced usage of obsnudging with surface observations (switches in run/ README.namelist, e.g. obsnudgezfullr1_uv, etc.)
 - These allow specifying how variables are nudged in a profile with their full weight and/or ramp down function relative to the surface or PBL top in different regimes (stable or unstable).
 - Defaults are set to reasonable values, so these can be left out of namelist unless needed.

FDDA Summary

- FDDA grid nudging is suitable for coarser grid sizes where analysis can be better than model-produced fields
- Obs nudging can be used to assimilate asynoptic or high-frequency observations
- Grid and obs nudging can be combined
- FDDA has fake sources and sinks and so should not be used on the domain of interest and in the time period of interest for scientific studies and simulations

End