

Fundamentals in Atmospheric Modeling

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List of presentations

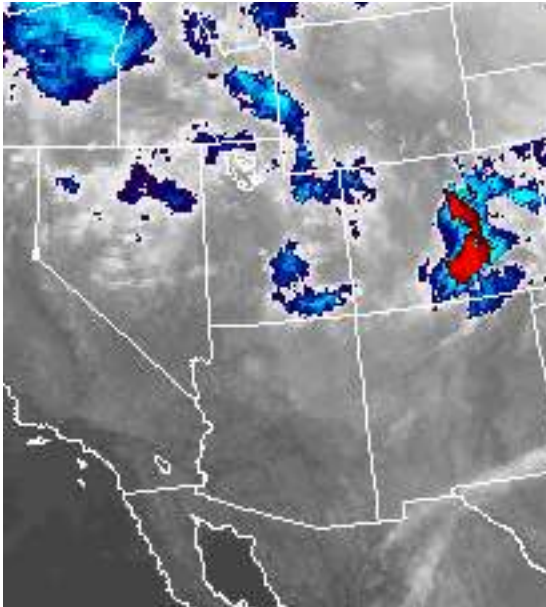
- **Concept of modeling**
- **Structure of models**
- **Predictability**

How the today's forecasts were made ?

Observation



Forecasts



NO!

Boulder CO

7 Day Forecast

OVERNIGHT



Partly
Cloudy
Low: 29 °F

TUESDAY



Mostly
Sunny
High: 50 °F

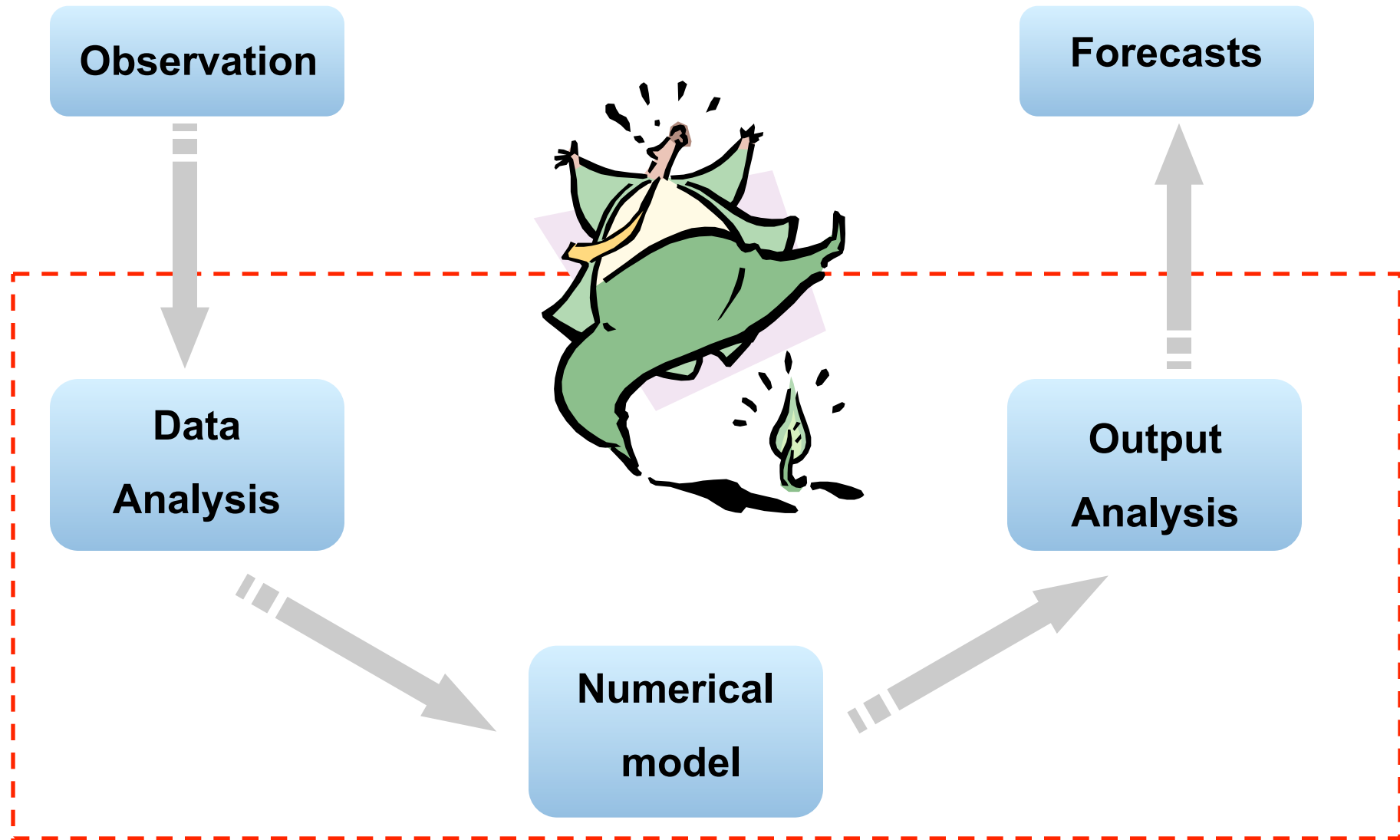
TUESDAY
NIGHT



Chance
Snow
Low: 19 °F

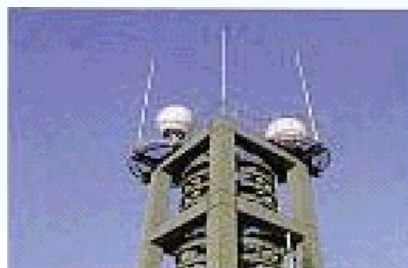
Then, what ?

Weather forecasts

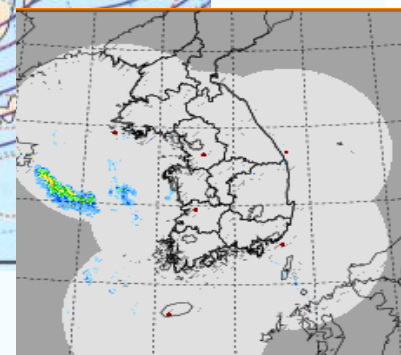
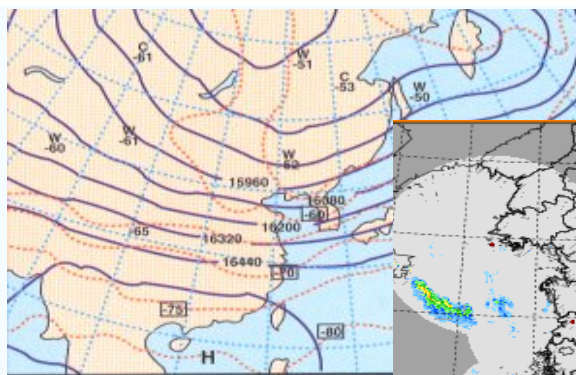




Step1: Observation



Step2: Data analysis



Theory ?

Thermodynamics

Heat = Energy + Work

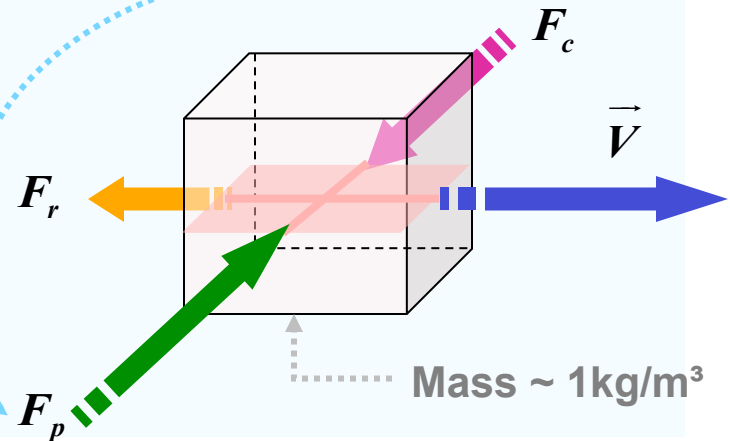


$$\begin{aligned}\Delta H &= c_p \Delta T - \alpha \Delta p \\ &= c_v \Delta T + p \Delta \alpha\end{aligned}$$

Dynamics

Force = Mass $\times$ Acceleration

- Mass $\doteq 1 \text{ kg/m}^3$
- Force: **PGF**, **CO**, **Friction**...





Theory ?



- Momentum

$$F = ma$$

- Mass

$$\frac{1}{M} \frac{dM}{dt} = 0$$

- Moisture

$$\frac{dq}{dt} = E - C$$

- Ideal gas

$$p\alpha = RT$$

- Energy

$$Q = C_v \frac{dT}{dt} + p \frac{d\alpha}{dt}$$

CONSERVATION

The governing equations

V. Bjerknes (1904) pointed out for the first time that there is a complete set of **7 equations with 7 unknowns** that governs the evolution of the atmosphere:

$$\frac{d\mathbf{v}}{dt} = -\alpha\nabla p - \nabla\phi + \mathbf{F} - 2\boldsymbol{\Omega} \times \mathbf{v} \quad (1-3)$$

$$\frac{\partial\rho}{\partial t} = -\nabla\cdot(\rho\mathbf{v}) \quad (4)$$

$$p = \rho RT \quad (5)$$

$$\frac{ds}{dt} = C_p \frac{1}{\theta} \frac{d\theta}{dt} = \frac{Q}{T} \quad (6)$$

$$\frac{dq}{dt} = E - C \quad (7)$$

7 equations, 7 unknown (u,v,w,T, p, den and q)

solvable

History of numerical weather forecasts

1904 : Norwegian V. [Bjerknes](#) (1862-1951) :

Setup the governing equations

1922 : British L. F. [Richardson](#) (1881-1953) :

Integrate model → failed

1939 : Swedish C.-G. Rossby :

1948, 1949, J. G. Charney (1917-1981)

1950 : Princeton Group

(Charney, Fjortoft,
von Newman)

ENIAC

(Electrical Numerical
Integrator and Computer)

→ first success

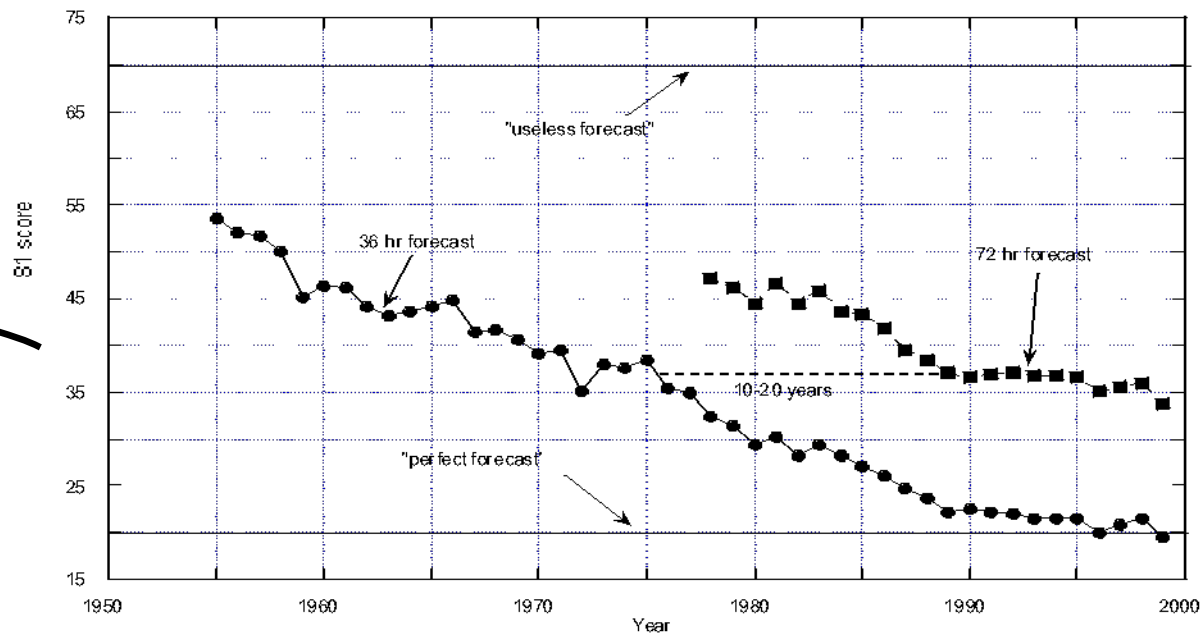
Computer Age (1946~)

- von Neumann and Charney
 - Applied ENIAC to weather prediction
- Carl-Gustaf Rossby
 - The Swedish Institute of Meteorology
 - First routine real-time numerical weather forecasting. (1954)
 - (US in 1958, Japan in 1959)



Tendency of forecast error (1955-1998) : NCEP

NCEP operational S1 scores at 36 and 72 hr
over North America (500 hPa)

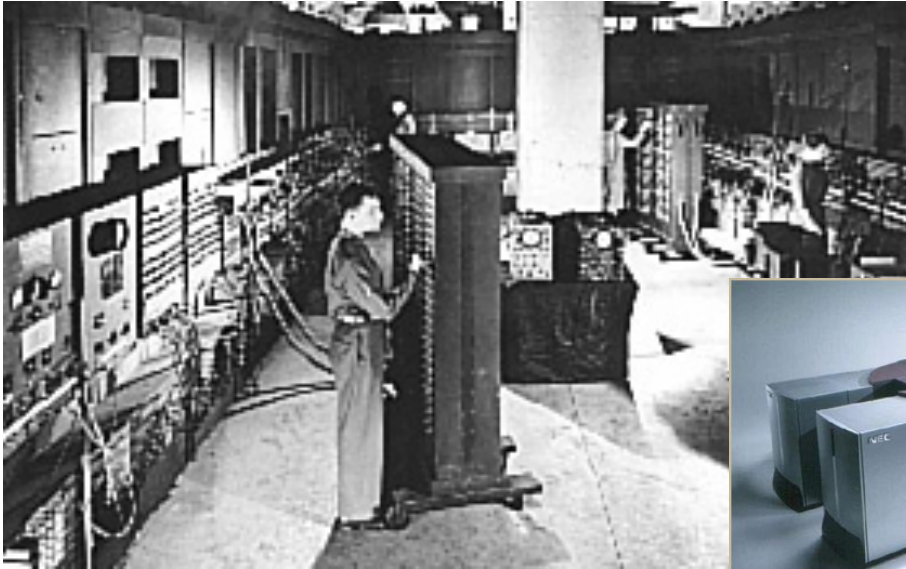


1day / 8 yrs

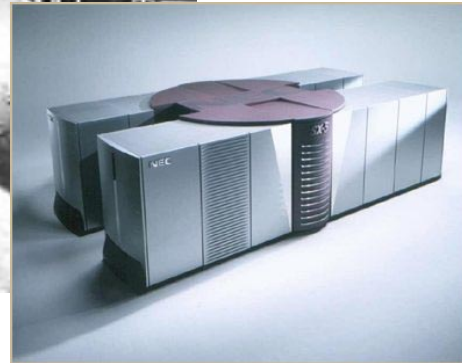
Factors for the improvement (Kalnay 2002)

- Supercomputers
- Physical processes
- Initial conditions

Super-computer for weather models



ENIAC, 1946



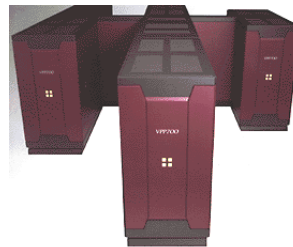
NEC SX-5



Cray T3E



Cray SV1



Fujitsu VPP700E



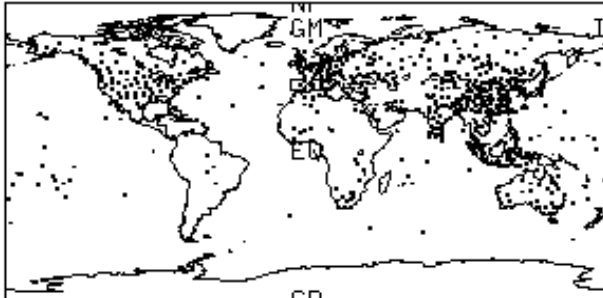
Cray T90



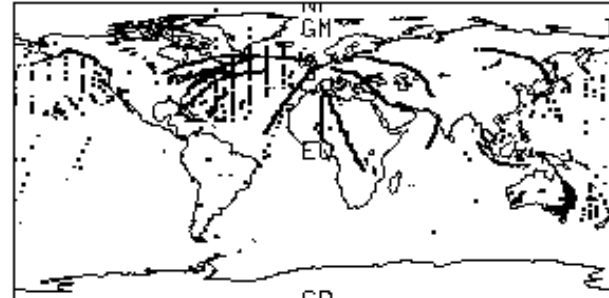
**Initial condition
(data assimilation)**

Various observations

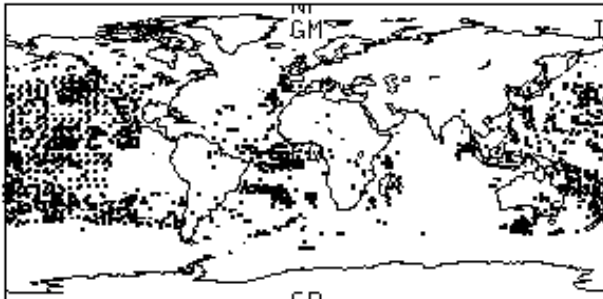
RAOBS



AIRCRAFT



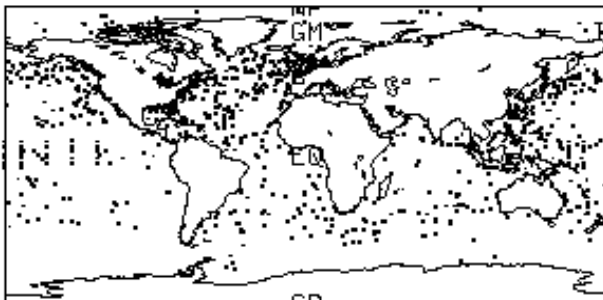
SAT WIND



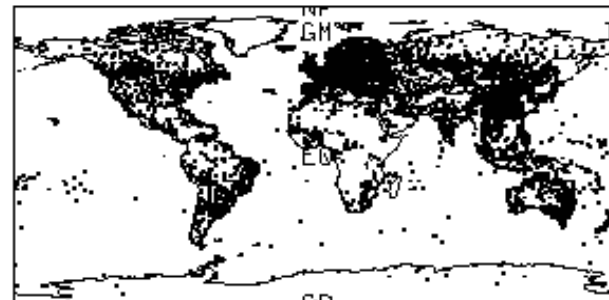
SAT TEMP



SFC SHIP



SFC LAND



heterogeneous in space and time....

Data Assimilation

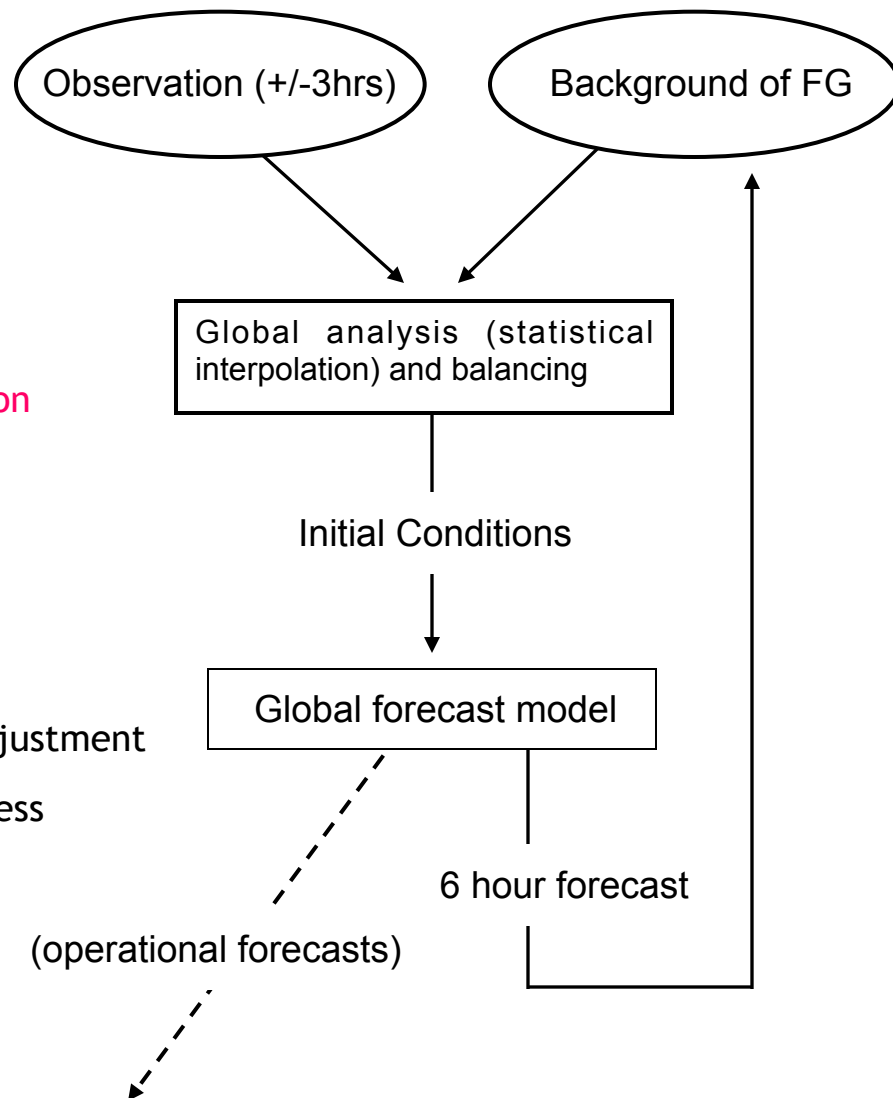
- Model $1^\circ \times 1^\circ$ resolution, 20 levels

u, v, T, q, Ps, Tg

$$360 \times 180 \times 20 = 1.3 \times 10^6 \times 4 \text{ variabl} = 5 \times 10^6$$

- observation : $10^4 \sim 10^5$ non-uniform distribution
 ± 3 hour window

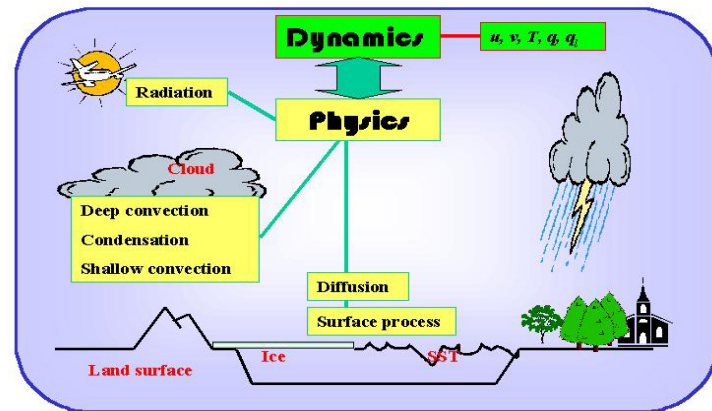
- Data assimilation cycle
 - 1) data checking
 - 2) objective analysis
 - 3) Initialization: dynamical adjustment
 - 4) short-range fcst for first guess



Model

- Dynamics : Identity (Speed)
- Physics : Components (Predictability)

Step3: Integration



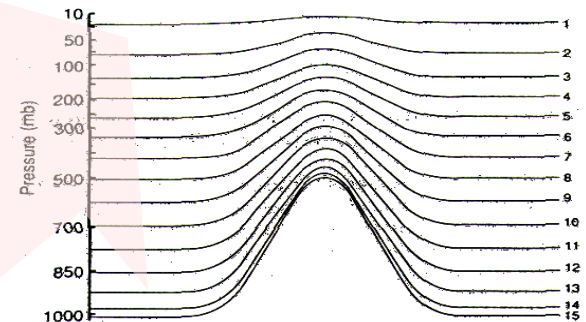
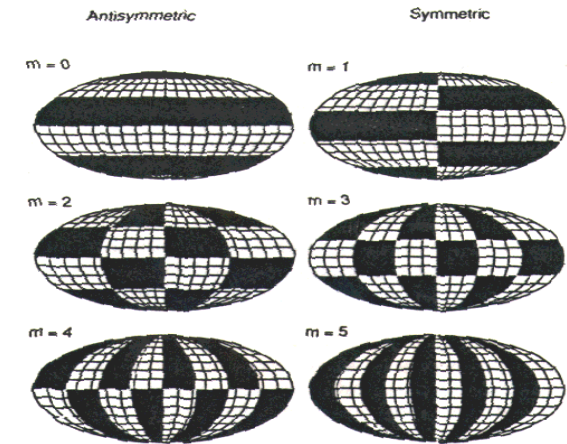
$$\frac{\partial u}{\partial t} = -u \frac{\partial u}{\partial x} - v \frac{\partial u}{\partial y} - \omega \frac{\partial u}{\partial p} - \frac{\partial \Phi}{\partial x} + f v + F_x$$

$$\frac{\partial v}{\partial t} = -u \frac{\partial v}{\partial x} - v \frac{\partial v}{\partial y} - \omega \frac{\partial v}{\partial p} - \frac{\partial \Phi}{\partial y} - f u + F_y$$

$$\frac{\partial \Phi}{\partial t} = - \frac{RT}{p}$$

$$\frac{\partial T}{\partial t} = -u \frac{\partial T}{\partial x} - v \frac{\partial T}{\partial y} + \omega \left(\frac{\kappa T}{p} - \frac{\partial T}{\partial p} \right) + \frac{\dot{H}}{c_p}$$

$$\frac{\partial \omega}{\partial p} = - \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right)$$



15-level sigma-coordinate model

Dynamics : model frame

Finite difference method (FDM) :

Spectral method (SPM) :

Finite element method (FEM) :

Ex) $\frac{\partial \phi}{\partial t} = -c \frac{\partial \phi}{\partial x}$; advection eq.

1) FDM (Finite difference)

$$\frac{\Delta \phi}{\Delta t} = \frac{\phi_2 - \phi_1}{t_2 - t_1}$$

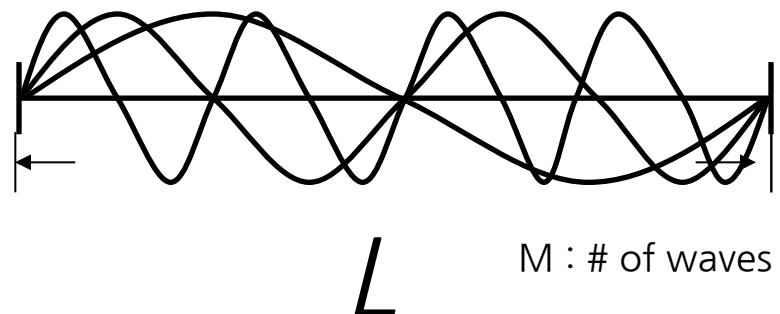
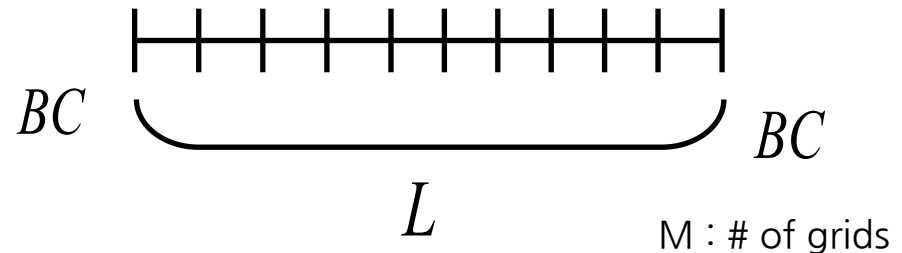
2) Spectral Method

- Determine basis function to get $H(\phi(x))$

- Expand ϕ in terms of a time series

$e_m(x)$ (basis funct), $m = m_1 \dots m_n \rightarrow$ infinite

$$\Rightarrow \phi(x, t) = \sum_{m=m_1}^{m_2} \phi_m(t) e_m(x)$$



* Resolution Increases $\left(\begin{array}{l} \Delta x \rightarrow \text{decreases} \\ m \rightarrow \text{increases} \end{array} \right.$ 18

Integration scheme ...

a) $\frac{u^{n+1} - u^{n-1}}{2\Delta t} = F(u^n)$: leap-frog **good for hyperbolic**
unstable for parabolic

b) $\frac{u^{n+1} - u^n}{\Delta t} = F(u^n)$: Euler-forward **good for diffusion**
unstable for hyperbolic

c) $\frac{u^{n+1} - u^n}{\Delta t} = F\left(\frac{u^n + u^{n+1}}{2}\right)$: **Crank-Nicholson**

d) $\frac{u^{n+1} - u^n}{\Delta t} = F(u^{n+1})$: **Fully implicit, backward**

e) $\frac{u^* - u^n}{\Delta t} = F(u^n)$: $\frac{u^{n+1} - u^n}{\Delta t} = F(u^*)$: **Euler-backward (Matzuno)**

f) $\frac{u^{n+\frac{1}{2}*} - u^n}{\Delta t/2} = F(u^n)$: $\frac{u^{n+\frac{1}{2}**} - u^n}{\Delta t/2} = F\left(u^{n+\frac{1}{2}*}\right)$

$\frac{u^{n+1} - u^n}{\Delta t} = \frac{1}{6} \left[F(u^n) + 2F\left(u^{n+\frac{1}{2}*}\right) + 2F\left(u^{n+\frac{1}{2}**}\right) + F(u^{n+1*}) \right]$: **RK(Runge-Kuta)-4th order**

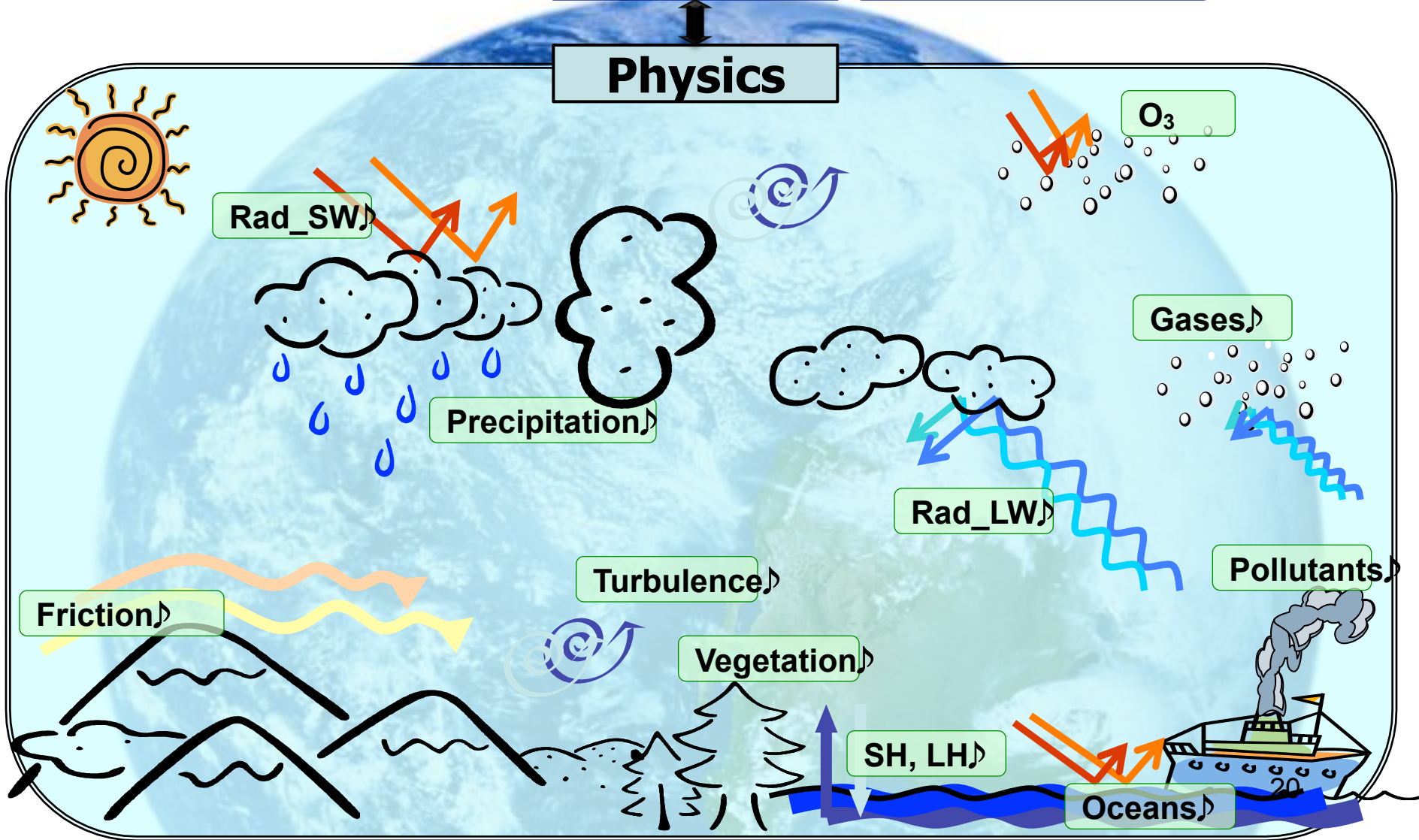
g) $\frac{u^{n+1} - u^{n-1}}{2\Delta t} = F_1(u^n) + F_2\left(\frac{u^{n+1} - u^{n-1}}{2}\right)$: **Semi-Implicit**

h) $\frac{u^* - u^n}{\Delta t} = F_1(u^n)$; $\frac{u^{n+1} - u^*}{\Delta t} = F_2(u^*)$: **Fractional steps**

Dynamics

$PGF, F_{co}, F_r, F_{ce}, F_g$

Physics



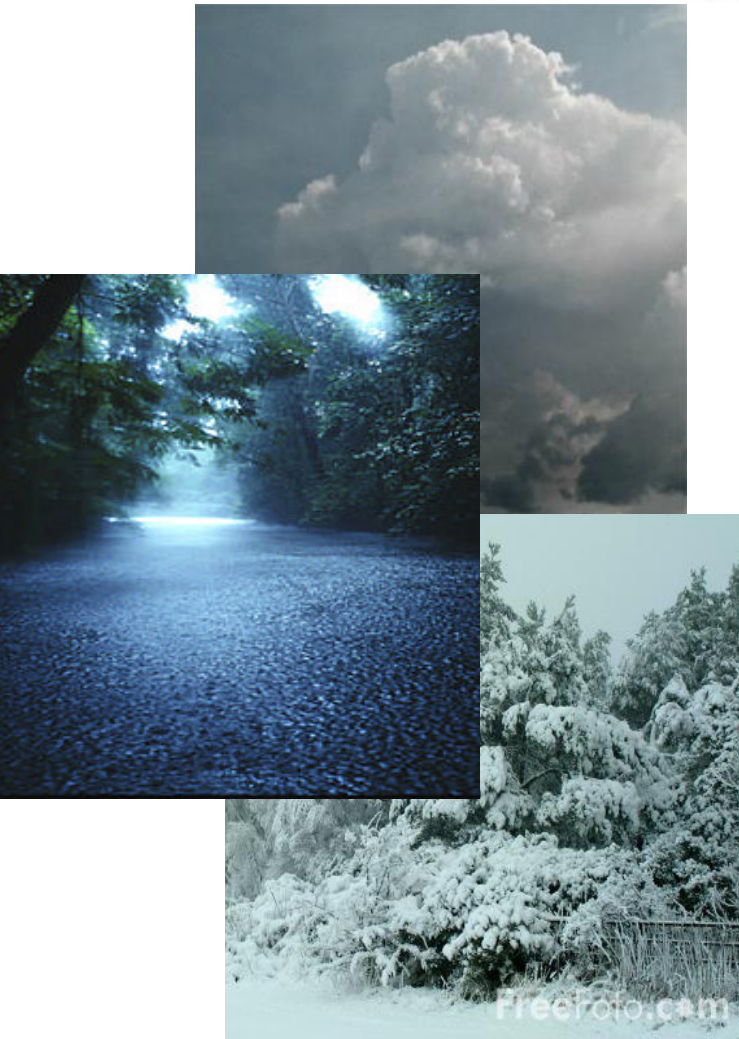
Example : Cloud and precipitation

Real atmosphere

Theory

Formulation

Model (computer program)



```
login1
MODULE module_mp_wsm3

REAL, PARAMETER, PRIVATE :: ...

login1
=====
compute internal functions
cpmcal(x) = cpd*(1.-max(x,qmin))+max(x,qmin)*cpv

=====
login1
=====
compute the minor time steps,
loops = max(int(delt/dtclcdr),1)
dtclcd = delt/loops
if(delt.le.dtclcdr) dtclcd = delt
do loop = 1,loops

=====
initialize the large scale variables
do i = its, ite
  mstep(i) = 1
  flgclcd(i) = .true.
enddo

do k = kts, kte
  CALL vsrec(tvec1(its),den(its,k),ite -its+1)
  do i = its, ite
    tvec1(i) = tvec1(i)*den0
  enddo
  CALL vssqrt(denfacs(its,k),tvec1(its),ite -its+1)
enddo

cvap = cpv
hvap=xlv0
hsub=xls
ttp=t0c+0.01
dldt=cvap-cliq
xai=-dldt/rv
xb=xai*hvap/(rv*ttp)
dldti=cvap-cice
xai=-dldti/rv
xbi=xai+hsub/(rv*ttp)
do k = kts, kte
  do i = its, ite
    tr=ttp/t(i,k)
    if(tr.lt.ttp) then
      qs(i,k) = psat*(exp(log(tr)*xai))*exp(xbi*(1.-tr))
    else
      qs(i,k) = psat*(exp(log(tr)*xai))*exp(xb*(1.-tr))
    endif
    qs0(i,k) = psat*(exp(log(tr)*xai))*exp(xb*(1.-tr))
    qs0(i,k) = (qs0(i,k)-qs(i,k))/qs(i,k)
    qs(i,k) = ep2 * qs(i,k) / (p(i,k) - qs(i,k))
    qs(i,k) = max(qs(i,k),qmin)
    rh(i,k) = max(q(i,k) / qs(i,k),qmin)
```

Cloud and precipitation

login1

```
do k = kts, kte
do i = its, ite
supsat = max(q(i,k),qmin)-qs(i,k)
satdt = supsat/dtclld
if(t(i,k).ge.t0c) then
```

$T > 0^\circ\text{C}$

```
=====
warm rain processes
```

```
- follows the processes in RH83 and LFD except for autoconversion
```

```
=====
paut1: auto conversion rate from cloud to rain [HDC 16]
(C->R)
```

```
if(qci(i,k).gt.qc0) then
paut(i,k) = qck1*exp(log(qci(i,k))*((7./3.)))
paut(i,k) = min(paut(i,k),qci(i,k)/dtclld)
endif
```

```
=====
pracw: accretion of cloud water by rain [D89 B15]
(C->R)
```

```
if(qrs(i,k).gt.qcrmin.and,qci(i,k).gt.qmin) then
pacr(i,k) = min(pacrr*rslope3(i,k)*rslopeb(i,k)
*qci(i,k)*denfac(i,k),qci(i,k)/dtclld)
endif
```

```
=====
pres1: evaporation/condensation rate of rain [HDC 14]
(V->R or R->V)
```

```
if(qrs(i,k).gt.0.) then
coeres = rslope2(i,k)*sqrt(rslope(i,k)*rslopeb(i,k))
pres(i,k) = (rh(i,k)-1.)*(precr1*rslope2(i,k)
+precr2*work2(i,k)*coeres)/work1(i,k)
if(pres(i,k).lt.0.) then
pres(i,k) = max(pres(i,k),-qrs(i,k)/dtclld)
pres(i,k) = max(pres(i,k),satdt/2)
else
pres(i,k) = min(pres(i,k),satdt/2)
endif
endif
endif
else
```

$$P_{aut1} = \min \left(\frac{0.104 g E_c \rho^{\frac{4}{3}}}{\mu (N_c \rho_w)^{\frac{1}{3}}} q_c^{\frac{7}{3}}, \frac{q_c}{dt} \right)$$

$$P_{racw} = \frac{\pi a_r E_{CR} N_{0r} q_c}{4} \left(\frac{\rho_0}{\rho} \right)^{\frac{1}{2}} \frac{\Gamma(3+b_r)}{\lambda_r^{3+b_r}}$$

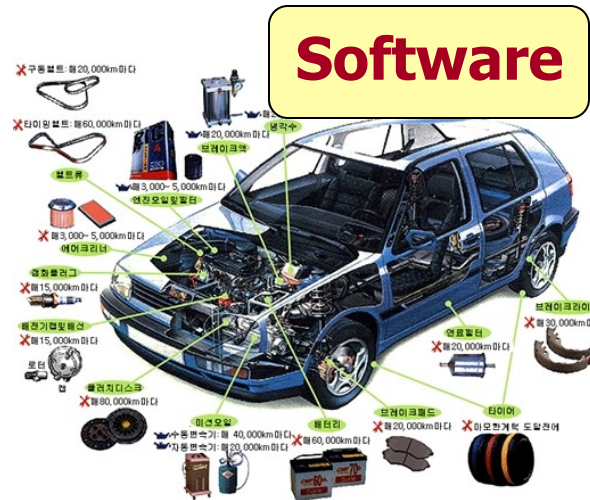
$$Pres1 = \frac{2\pi N_{0r} (S_w - 1)}{(A_w + B_w)} \left[\frac{0.78}{\lambda_r^2} + \frac{a_r^{\frac{1}{2}} 0.31 \Gamma(b_r/2 + 5/2)}{\lambda_r^{b_r/2 + 5/2}} \left(\frac{\mu}{D} \right)^{\frac{1}{3}} \left(\frac{1}{\mu} \right)^{\frac{1}{2}} \left(\frac{\rho_0}{\rho} \right)^{\frac{1}{4}} \right]$$

Car and model



아시아루테이

Dynamics



Physics



Data assimilation

Driver ? ➡ Could be forecaster ???

Classification of models

- Dynamic frame

Hydrostatic	Non-hydrostatic
Large-scale	Small-scale (heavy rainfall, complex mountain)

- Scale

Global	Regional
10 km - 100 km	1 km-10 km

- Purpose

FORECAST	Forcing → RESPONSE
NWP : upto 2 weeks	GCM (General circulation model)

Predictability



Chaos theory (Lorenz)



Charney (1951) : Uncertainties in initial condition and model



Lorenz (1962,1963) : Unstable nature of atmosphere



Purpose : NWP is better than statistical forecast

Tool : 4 K memory computer

Model : 12 variables (heating and dissipation forcing)

Results : differences -> non-periodicity



Initial condition (3 decimal point) : different after 2 month

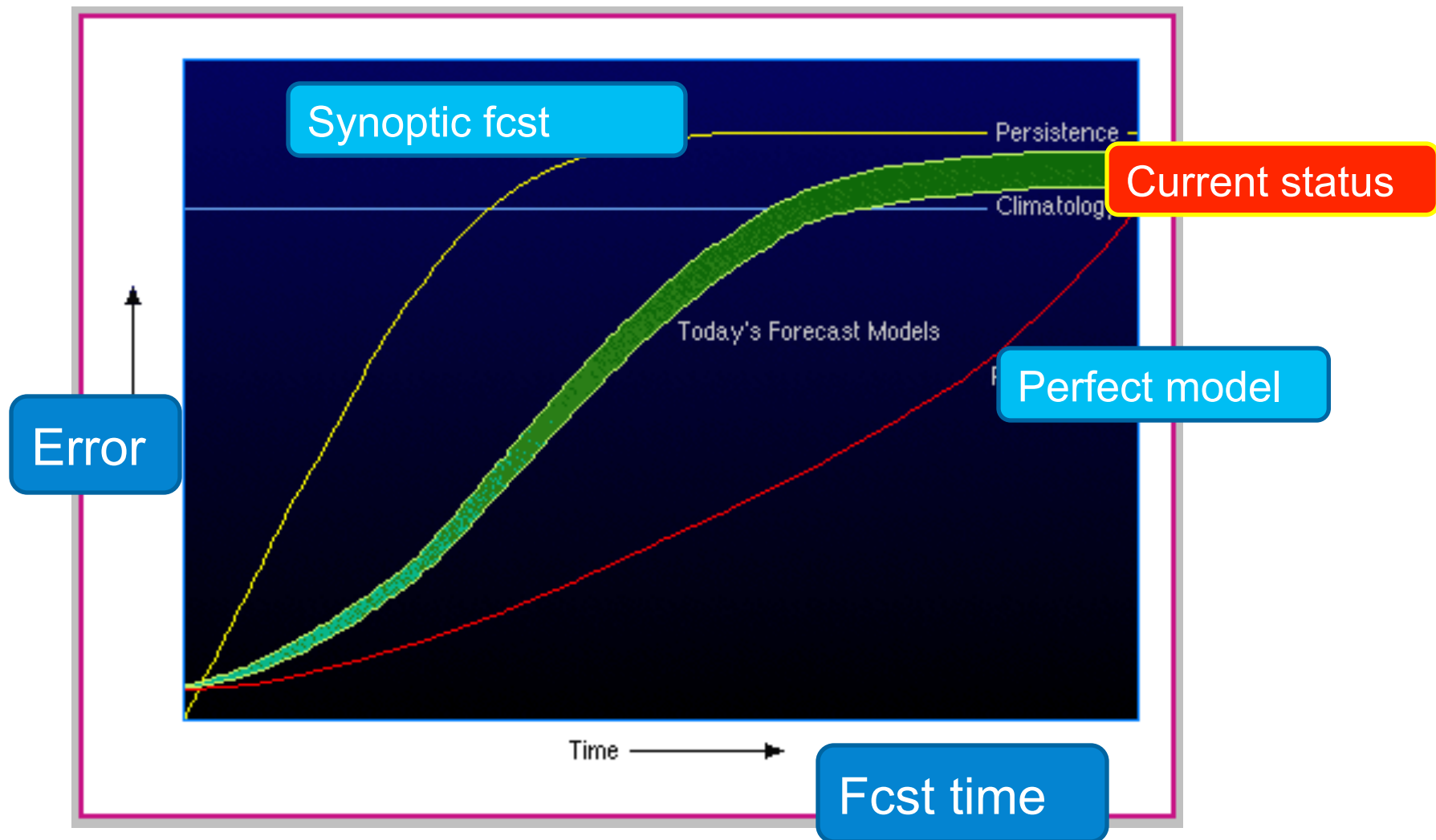


Round-off error -> cause of non-periodicity

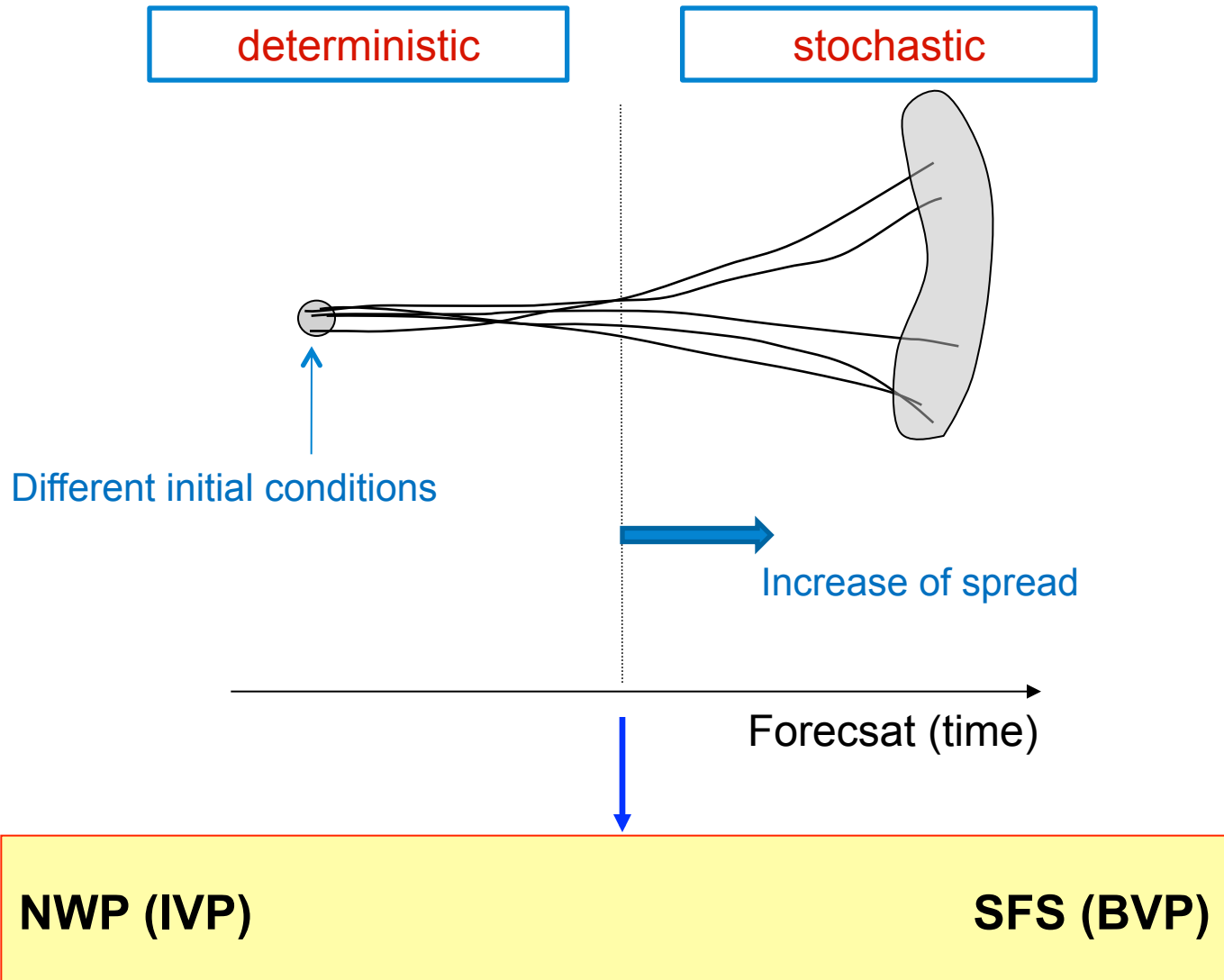


Chaos theory– two weeks

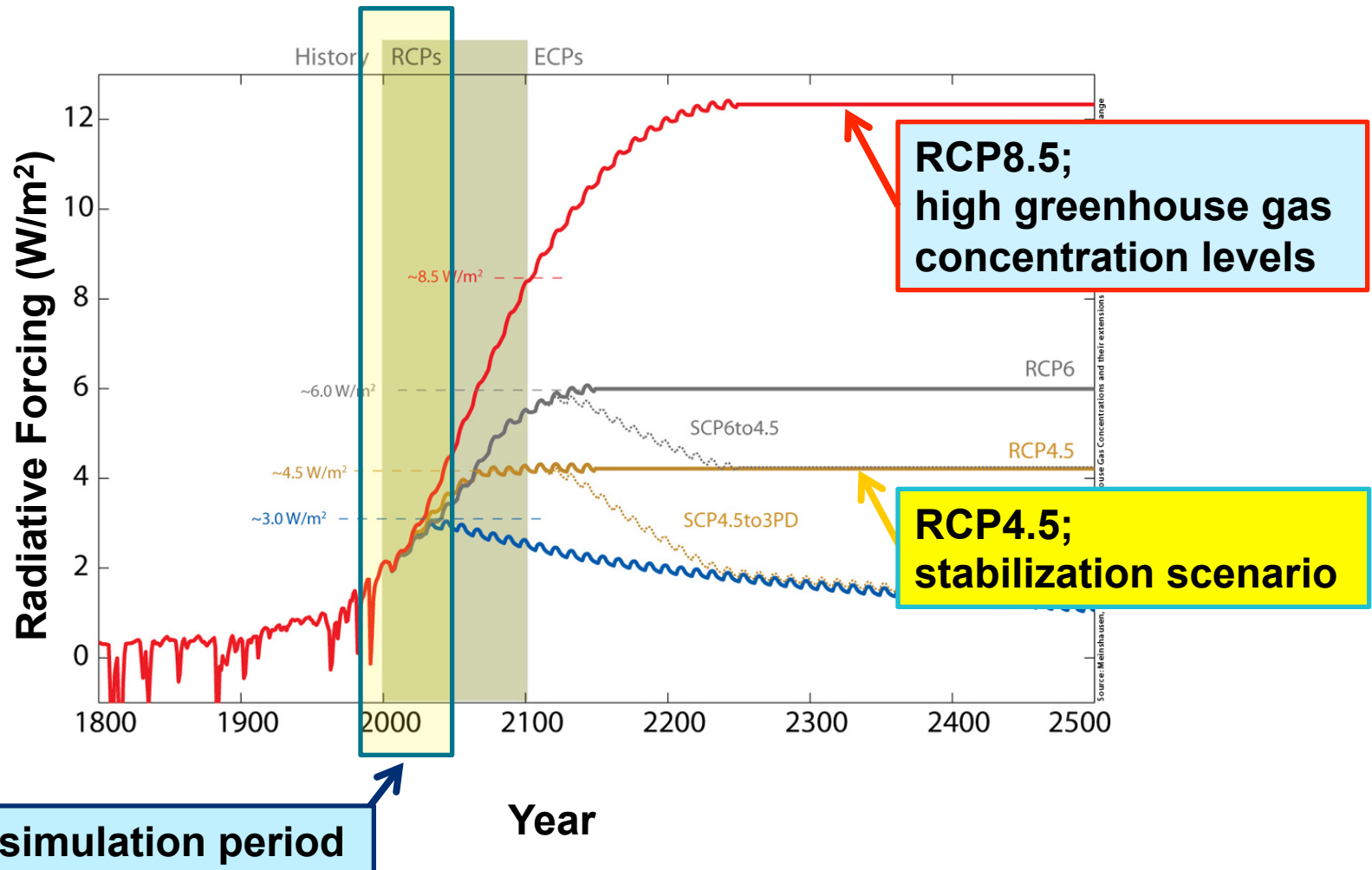
Predictability



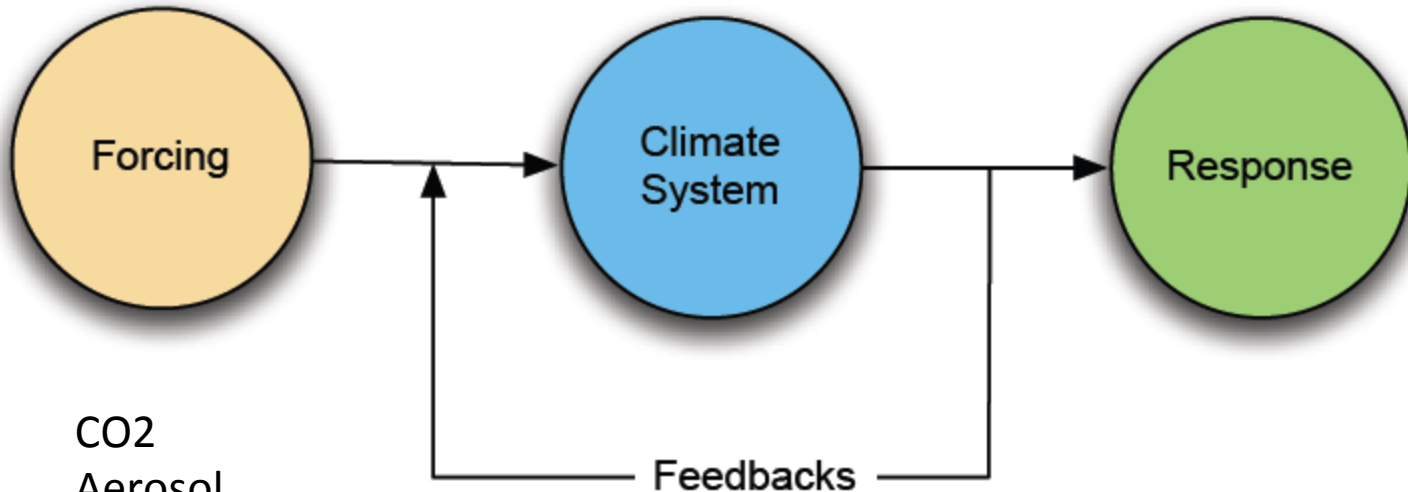
Ensemble forecasts



RCP scenarios



Climate system sensitivity

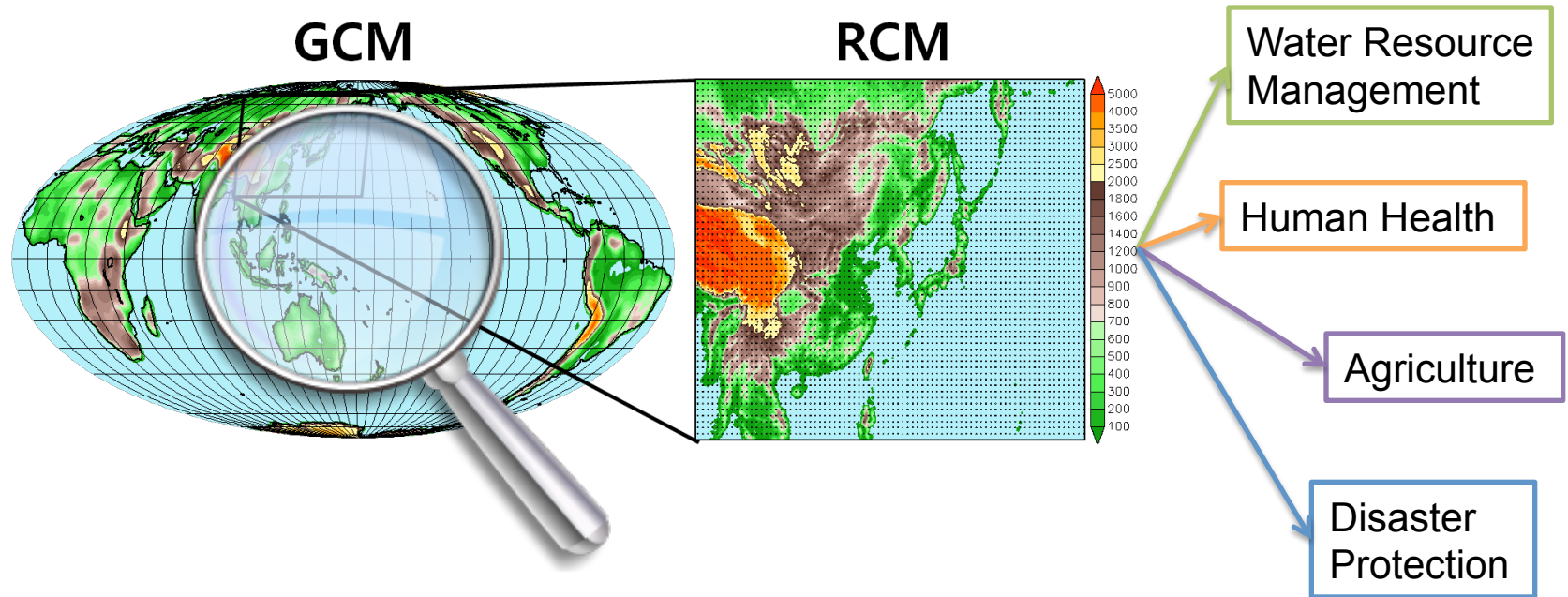


CO2
Aerosol
Volcanic

Water vapor feedback
Ice-albedo feedback
Vegetation feedbacks
Cloud (radiative) feedback
(Great debate!, Mostly still uncertain)

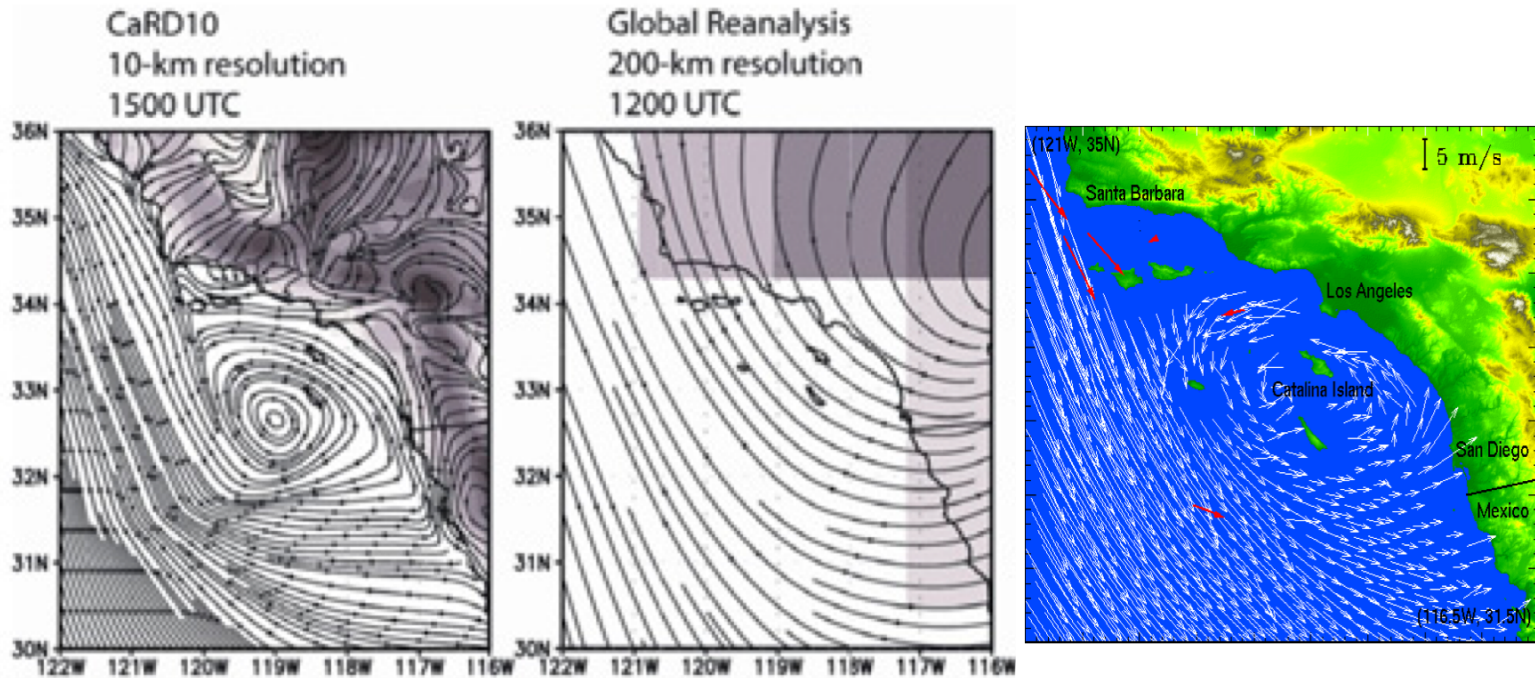
...

Global versus Regional



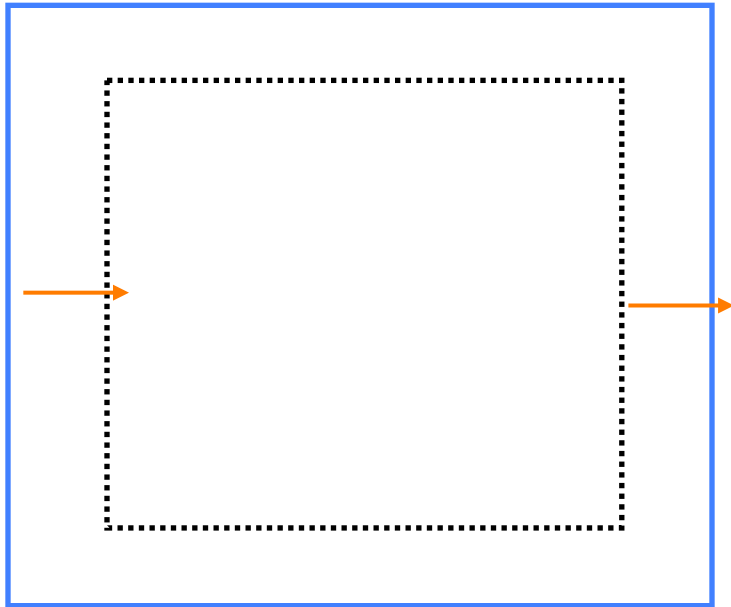
Regional model is a magnifying glass

Benefit ? ---- Very clear !

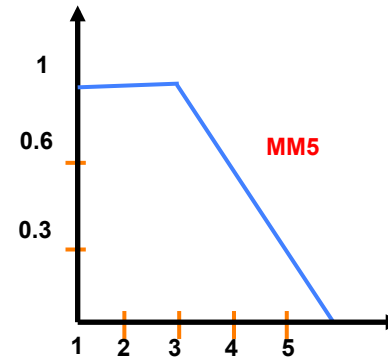


But, there is another issue on lateral boundary treatment

Buffer zone



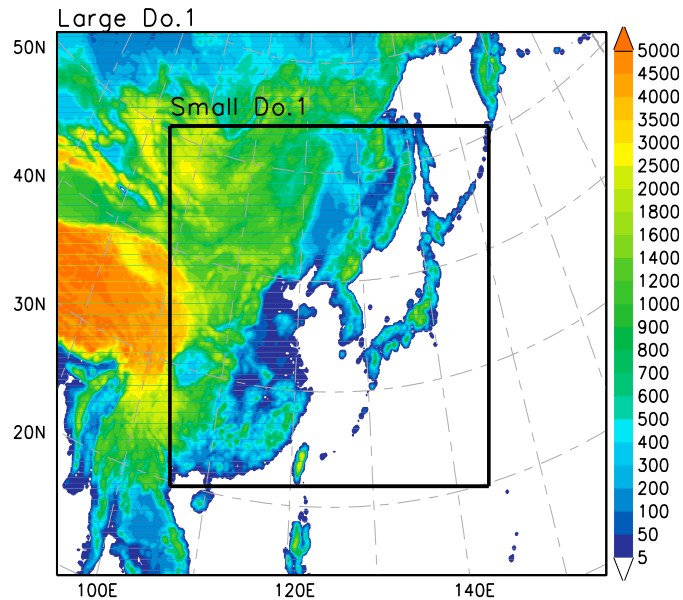
$F(n)$: weighting of global



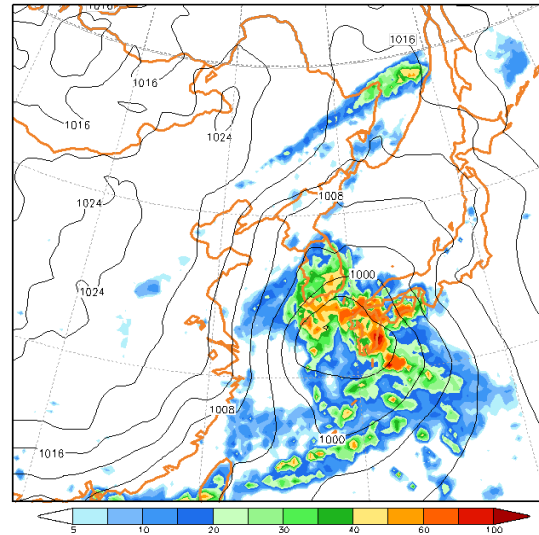
$$\left. \frac{\partial A}{\partial t} \right|_n = F(n)F_1(A_{CM} - A_{FM}) - F(n)F_2\nabla^2(A_{CM} - A_{FM})$$

So, empirical

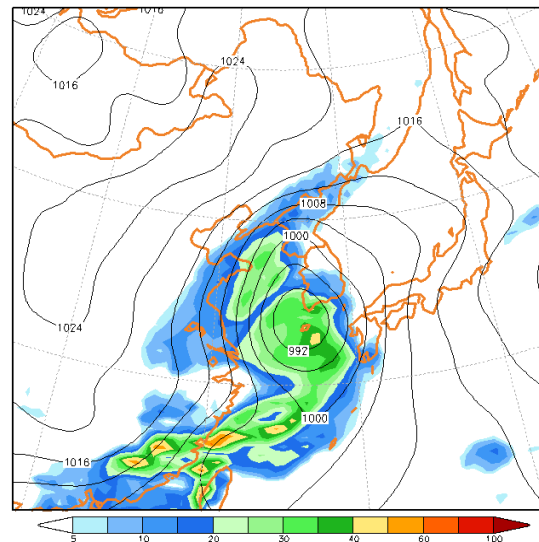
Domain size sensitivity



Mid-latitude cyclone on April 6th, 2013



TMPA
and FNL

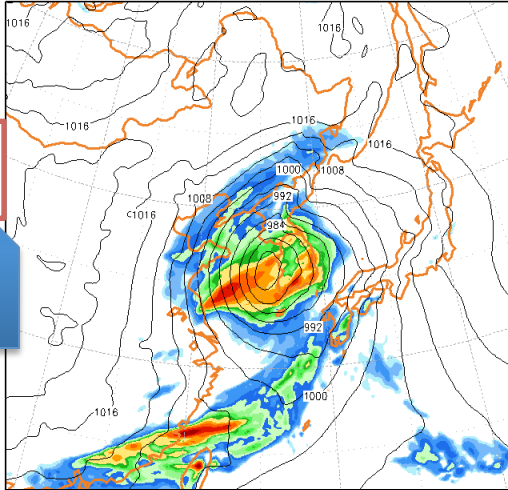


GFS 72 hr
fcst

WRF fcst driven by GFS fcst

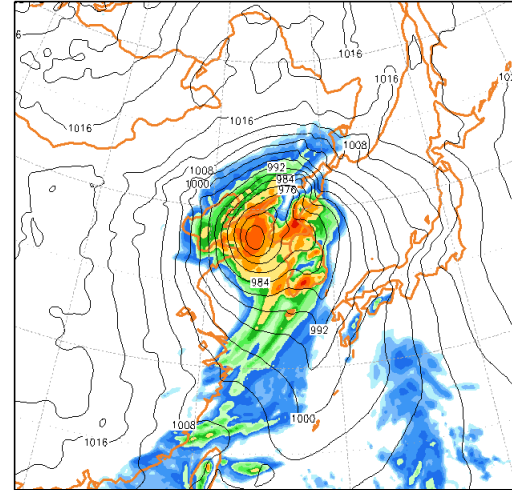
Small

Close to GFS

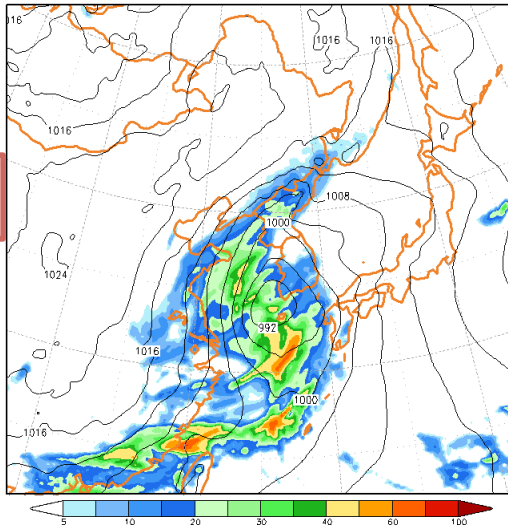


Large

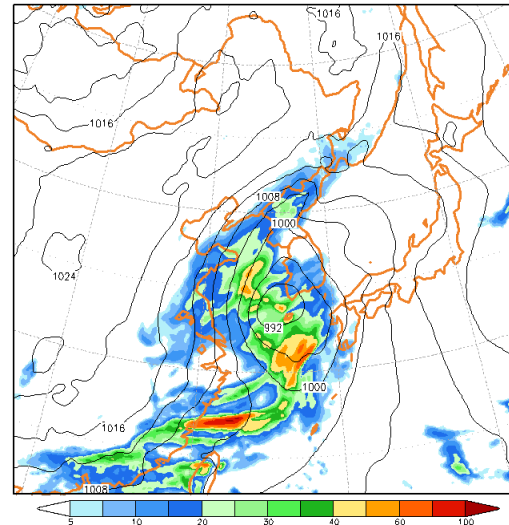
Away from GFS



Small_SP

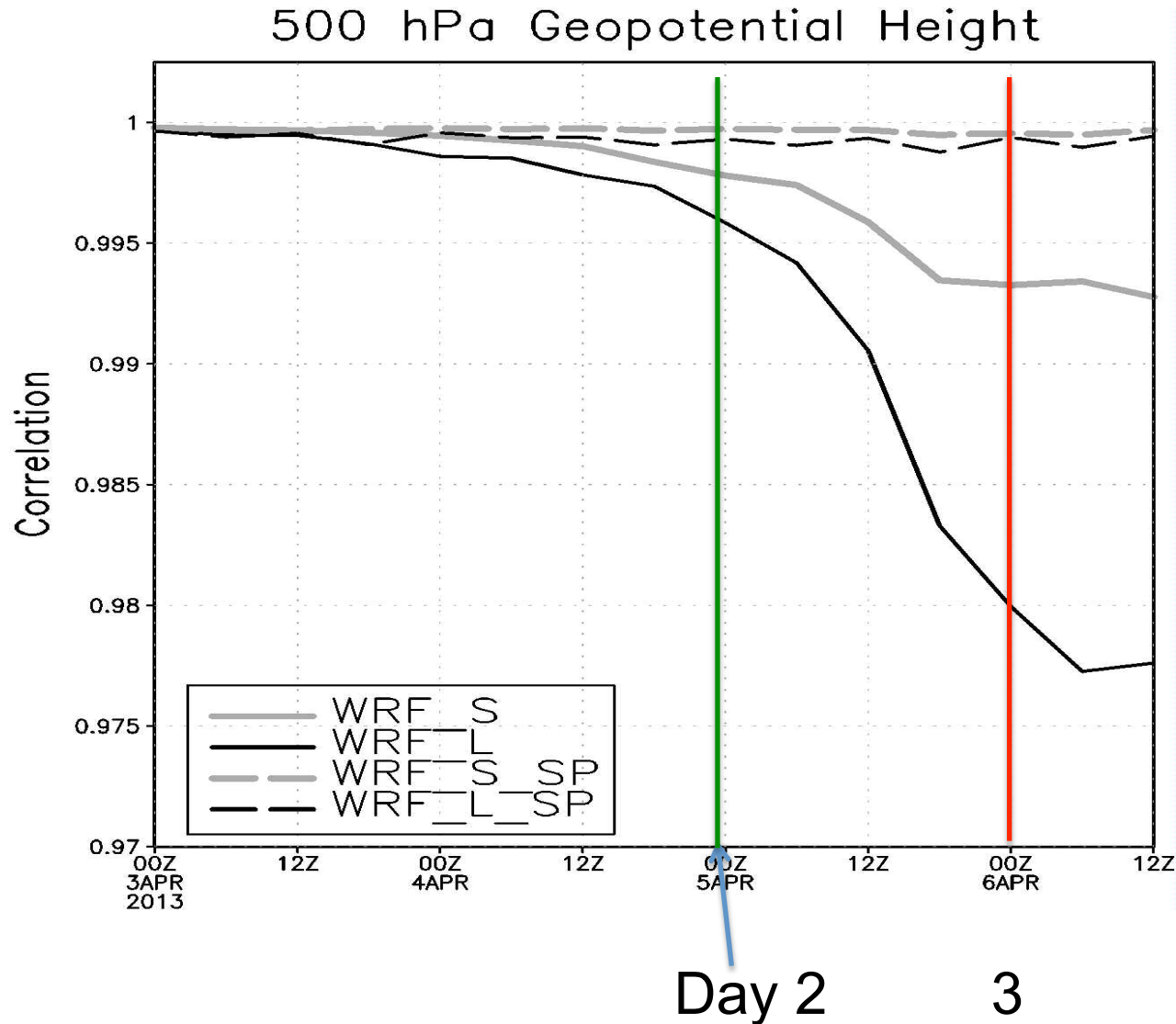


Large_SP



Spectral nudging (SP): WRF approaches to GFS forecasts ...but loses regional details

Domain-averaged PC



Fundamental limit of the regional model : low resolution global and mathematically ill-posed setup

Small domain keeps the large-scale from the global but loses its freedom

Spectral nudging keeps the large-scale, but may lose the regional details

Thanks for your attention !
songyouhong@gmail.com

Hong, S.-Y., and M. Kanamitsu, 2014: Dynamical downscaling: Fundamental issues from an NWP point of view and recommendations. *Asia-Pac. J. Atmos. Sci.*, **50**, 83-104, doi: 10.1007/s13143-014-0029-2.

Dudhia, J., 2014: A history of mesoscale model Development. *Asia-Pac. J. Atmos. Sci.*, **50**, 121-131.