#### **Dynamics: Introduction**

# The Advanced Research WRF (ARW) Dynamics Solver

- 1. What is a dynamics solver?
- 2. Variables and coordinates
- 3. Equations
- 4. Time integration scheme
- 5. Grid staggering
- 6. Advection (transport) and conservation
- 7. Time step parameters
- 8. Filters
- 9. Map projections and global configuration
- 10. Boundary condition options

#### WRF ARW Tech Note

A Description of the Advanced Research WRF Version 3 (June 2008, 2012 update) http://www.mmm.ucar.edu/wrf/users/pub-doc.html

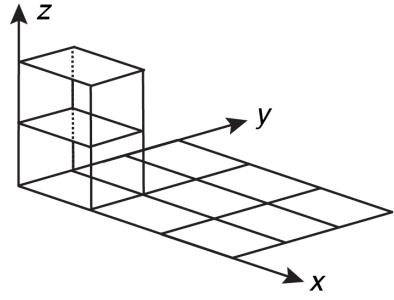
#### Dynamics: 1. What is a *dynamics solver?*

A dynamical solver (or a dynamical core, or dycore) performs a time (t) and space (x,y,z) integration of the equations of motion.

Given the 3D atmospheric state at time t, S(x,y,z,t), we integrate the equations forward in time from  $t \longrightarrow T$ , i.e. we run the model and produce a forecast.

The equations cannot be solved analytically, so we *discretize* the equations on a *grid* and compute *approximate* solutions.

The accuracy of the solutions depend on the numerical method and the mesh spacing (grid).



#### Dynamics: 2. Variables and coordinates

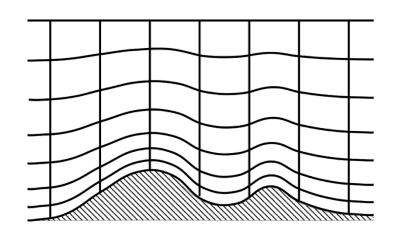
Hydrostatic pressure  $\pi$ 

Column mass 
$$\mu = \pi_s - \pi_t$$
 (per unit area)

(per unit area)

Vertical coordinate 
$$\eta = \frac{(\pi - \pi_t)}{\mu}$$

Layer mass 
$$\mu\Delta\eta = \Delta\pi = g\rho\Delta z$$
 (per unit area)



Conserved state (prognostic) variables:

$$\mu$$
,  $U = \mu u$ ,  $V = \mu v$ ,  $W = \mu w$ ,  $\Theta = \mu \theta$ 

Non-conserved state variable:  $\phi = gz$ 

#### Dynamics: 2. Variables and coordinates

Vertical momentum eqn.

$$\frac{\partial W}{\partial t} + g \left( \mu_d - \frac{\alpha}{\alpha_d} \frac{\partial p}{\partial \eta} \right) = -\frac{\partial Uw}{\partial x} - \frac{\partial \Omega w}{\partial \eta}$$

Subscript d denotes dry, and

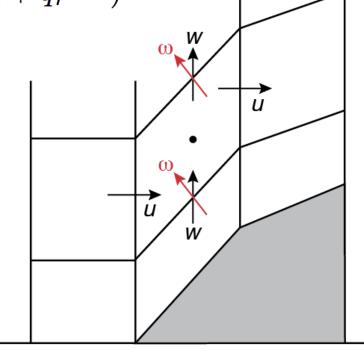
$$\alpha_d = \frac{1}{\rho_d} \qquad \alpha = \alpha_d \left( 1 + q_v + q_c + q_r \cdots \right)^{-1}$$

$$\rho = \rho_d \left( 1 + q_v + q_c + q_r \cdots \right)$$

covariant  $(u, \omega)$  and contravariant w velocities

$$u = \frac{dx}{dt}, \quad w = \frac{dz}{dt}, \quad \omega = \frac{d\eta}{dt}$$

$$U = \mu u, \quad W \mu w, \quad \Omega = \mu \omega$$



#### Dynamics: 3. Equations

transport pressure gradient
$$\frac{\partial U}{\partial t} = -\frac{\partial Uu}{\partial x} - \frac{\partial Vu}{\partial y} - \frac{\partial \Omega u}{\partial \eta} - \alpha \mu_d \frac{\partial p}{\partial x} - \frac{\alpha}{\alpha_d} \frac{\partial p}{\partial \eta} \frac{\partial \phi}{\partial x} + R_u + Q_u$$

$$\frac{\partial V}{\partial t} = -\frac{\partial Uv}{\partial x} - \frac{\partial Vv}{\partial y} - \frac{\partial \Omega v}{\partial \eta} - \alpha \mu_d \frac{\partial p}{\partial y} - \frac{\alpha}{\alpha_d} \frac{\partial p}{\partial \eta} \frac{\partial \phi}{\partial y} + R_v + Q_v$$

$$\frac{\partial W}{\partial t} = -\frac{\partial Uw}{\partial x} - \frac{\partial Vw}{\partial y} - \frac{\partial \Omega w}{\partial \eta} - g\left(\mu_d - \frac{\alpha}{\alpha_d} \frac{\partial p}{\partial \eta}\right) + R_w + Q_w$$

$$\frac{\partial \mu_d}{\partial t} = -\frac{\partial U}{\partial x} - \frac{\partial V}{\partial y} - \frac{\partial \Omega}{\partial \eta} + R_{\theta} + Q_{\theta}$$

$$\frac{\partial \Theta}{\partial t} = -\frac{\partial U\theta}{\partial x} - \frac{\partial V\theta}{\partial y} - \frac{\partial \Omega\theta}{\partial \eta} + R_{q_j} + Q_{q_j}$$
numerical filters,
$$\frac{\partial \mu_d q_j}{\partial t} = -\frac{\partial Uq_j}{\partial x} - \frac{\partial Vq_j}{\partial y} - \frac{\partial \Omega q_j}{\partial \eta} + R_{q_j} + Q_{q_j}$$
projection terms
$$\frac{\partial \phi}{\partial t} = -u \frac{\partial \phi}{\partial x} - v \frac{\partial \phi}{\partial y} - \omega \frac{\partial \phi}{\partial \eta} + gw$$
geopotential eqn term

Diagnostic relations: 
$$\frac{\partial \phi}{\partial \eta} = -\alpha_d \mu_d, p = \left(\frac{R_d \Theta_m}{p_o \mu_d \alpha_d}\right)^T, \ \Theta_m = \Theta\left(1 + \frac{R_v}{R_d} q_v\right)$$

#### Dynamics: 4. Time integration scheme

## 3<sup>rd</sup> Order Runge-Kutta time integration

advance 
$$\phi^t \to \phi^{t+\Delta t}$$

$$\frac{\partial U}{\partial t} = RHS_u$$

$$\frac{\partial V}{\partial t} = RHS_v$$

$$\frac{\partial W}{\partial t} = RHS_w$$

$$\phi^{**} = \phi^t + \frac{\Delta t}{3}RHS(\phi^t)$$

$$\phi^{**} = \phi^t + \frac{\Delta t}{2}RHS(\phi^*)$$

$$\phi^{t+\Delta t} = \phi^t + \Delta t RHS(\phi^{**})$$

Amplification factor 
$$\phi_t = ik\phi$$
;  $\phi^{n+1} = A\phi^n$ ;  $|A| = 1 - \frac{(k\Delta t)^4}{24}$ 

#### Dynamics: 4. Time integration scheme – time splitting

$$U_{t} = L_{fast}(U) + L_{slow}(U)$$

3rd order Runge-Kutta, 3 steps  $L_{s}(U^{t})$ t+dt/3t+dt  $L_s(U^*)$ t+dt/2t+dt $L_s(U^{**})$ I Jt+dt t+dt

fast: acoustic and gravity wave terms.

slow: everything else.

- RK3 is 3rd order accurate for linear eqns, 2nd order accurate for nonlinear eqns.
- Stable for centered and upwind advection schemes.
- Stable for Courant number Udt/dx < 1.73
- Three  $L_{slow}(U)$  evaluations per timestep.

#### Dynamics: 4. Time integration scheme – acoustic step

$$U^{t+\Delta t}, \ V^{t+\Delta t} \qquad \frac{\partial U}{\partial t} + \left(\mu_{d}\alpha \frac{\partial p}{\partial x} + \frac{\alpha}{\alpha_{d}} \frac{\partial p}{\partial \eta} \frac{\partial \phi}{\partial x}\right)^{\tau} = R_{U}^{t}$$

$$\mu_{d}^{\tau+\Delta \tau} \quad \Omega^{\tau+\Delta \tau} \qquad \frac{\partial \mu_{d}}{\partial t} + \frac{\partial U}{\partial x}^{\tau+\Delta \tau} + \frac{\partial \Omega}{\partial \eta}^{\tau+\Delta \tau} = 0$$

$$\Theta^{\tau+\Delta \tau} \qquad \frac{\partial \Theta}{\partial t} + \left(\frac{\partial U\theta^{t}}{\partial x} + \frac{\partial \Omega\theta^{t}}{\partial \eta}\right)^{\tau+\Delta \tau} = R_{\Theta}^{t}$$

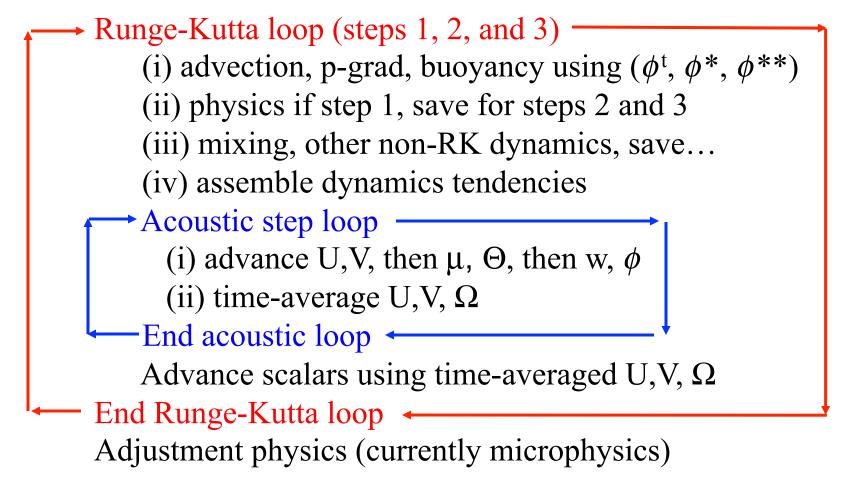
$$W^{\tau+\Delta \tau} \qquad \frac{\partial W}{\partial t} + g\left(\mu_{d} - \frac{\alpha}{\alpha_{d}} \frac{\partial p}{\partial \eta}\right)^{\tau} = R_{W}^{t}$$

$$\phi^{\tau+\Delta \tau} \qquad \mu_{d}^{t} \frac{\partial \phi}{\partial t} + U^{\tau+\Delta \tau} \frac{\partial \phi}{\partial x}^{t} + \Omega^{\tau+\Delta \tau} \frac{\partial \phi}{\partial \eta}^{t} - g\overline{W}^{\tau} = R_{\phi}^{t}$$

- Forward-backward differencing on U,  $\Theta$ , and  $\mu$  equations
- Vertically implicit differencing on W and  $\phi$  equations

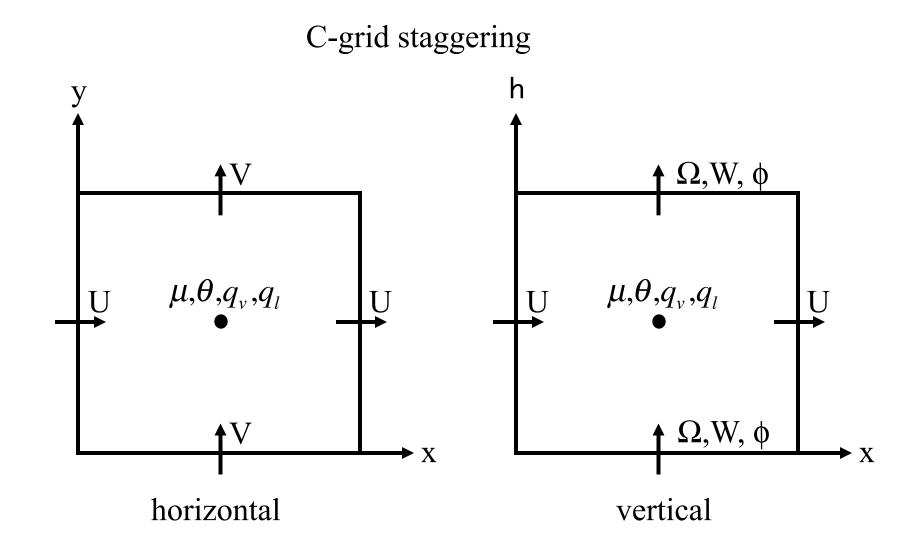
#### Dynamics: 4. Time integration scheme - implementation

#### Begin time step



End time step

#### Dynamics: 5. Grid staggering – horizontal and vertical



#### Dynamics: 6. Advection (transport) and conservation

2<sup>nd</sup>, 3<sup>rd</sup>, 4<sup>th</sup>, 5<sup>th</sup> and 6<sup>th</sup> order centered and upwind-biased schemes are available in the ARW model.

Example: 5<sup>th</sup> order scheme

$$\frac{\partial(U\psi)}{\partial x} = \frac{1}{\Delta x} \left( F_{i+\frac{1}{2}}(U\psi) - F_{i-\frac{1}{2}}(U\psi) \right)$$

where

$$F_{i-\frac{1}{2}}(U\psi) = U_{i-\frac{1}{2}} \left\{ \frac{37}{60} (\psi_i + \psi_{i-1}) - \frac{2}{15} (\psi_{i+1} + \psi_{i-2}) + \frac{1}{60} (\psi_{i+2} + \psi_{i-3}) \right\}$$
$$-sign(1,U) \frac{1}{60} \left\{ (\psi_{i+2} - \psi_{i-3}) - 5(\psi_{i+1} - \psi_{i-2}) + 10(\psi_i - \psi_{i-1}) \right\}$$

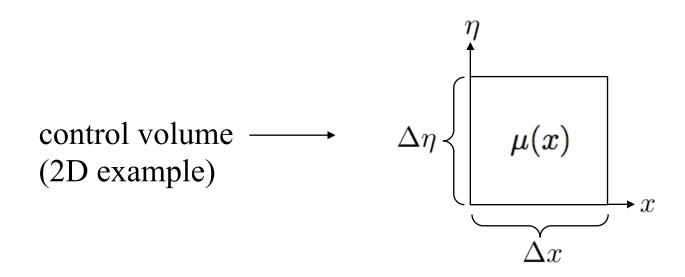
Dynamics: 6. Advection (transport) and conservation

For constant U, the 5<sup>th</sup> order flux divergence tendency becomes

$$\Delta t \frac{\delta(U\psi)}{\Delta x} \bigg|_{5th} = \Delta t \frac{\delta(U\psi)}{\Delta x} \bigg|_{6th}$$

$$- \underbrace{\left| \frac{U\Delta t}{\Delta x} \right| \frac{1}{60} \left( -\psi_{i-3} + 6\psi_{i-2} - 15\psi_{i-1} + 20\psi_{i} - 15\psi_{i+1} + 6\psi_{i+2} - \psi_{i+3} \right)}_{\frac{Cr}{60}} \frac{\partial^{6}\psi}{\partial x^{6}} + H.O.T$$

The odd-ordered flux divergence schemes are equivalent to the next higher ordered (even) flux-divergence scheme plus a dissipation term of the higher even order with a coefficient proportional to the Courant number.



Mass in a control volume is proportional to

$$(\Delta x \Delta \eta)(\mu)^t$$

since 
$$\mu(x)\Delta\eta = \Delta\pi = -g\rho\Delta z$$

Mass in a control volume  $(\Delta x \Delta \eta)(\mu)^t$ 2D example

Mass conservation equation

$$\Delta t^{-1}(\Delta x \Delta \eta) \cdot \left[ (\mu)^{t+\Delta t} - (\mu)^{t} \right] = \left[ (\mu u \Delta \eta)_{x-\Delta x/2,\eta} - (\mu u \Delta \eta)_{x+\Delta x/2,\eta} \right] + \left[ (\mu \omega \Delta x)_{x,\eta-\Delta \eta/2} - (\mu \omega \Delta x)_{x,\eta+\Delta \eta/2} \right]$$

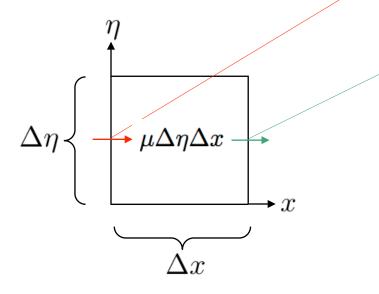
Change in mass over a time step

mass fluxes through control volume faces

Mass in a control volume  $(\Delta x \Delta \eta)(\mu)^t$ 

Mass conservation equation

$$\Delta t^{-1} (\Delta x \Delta \eta) \cdot \left[ (\mu)^{t+\Delta t} - (\mu)^t \right] = \left[ (\mu u \Delta \eta)_{x-\Delta x/2,\eta} - (\mu u \Delta \eta)_{x+\Delta x/2,\eta} \right] + \left[ (\mu \omega \Delta x)_{x,\eta-\Delta \eta/2} - (\mu \omega \Delta x)_{x,\eta+\Delta \eta/2} \right]$$



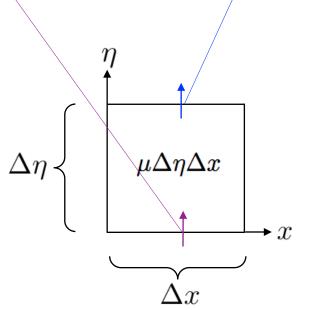
Horizontal fluxes through the vertical control-volume faces

Mass in a control volume  $(\Delta x \Delta \eta)(\mu)^t$ 

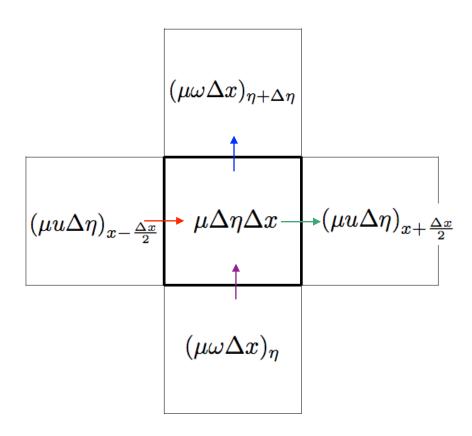
Mass conservation equation

$$\Delta t^{-1} (\Delta x \Delta \eta) \cdot \left[ (\mu)^{t+\Delta t} - (\mu)^t \right] = \left[ (\mu u \Delta \eta)_{x-\Delta x/2,\eta} - (\mu u \Delta \eta)_{x+\Delta x/2,\eta} \right] + \left[ (\mu \omega \Delta x)_{x,\eta-\Delta \eta/2} - (\mu \omega \Delta x)_{x,\eta+\Delta \eta/2} \right]$$

Vertical fluxes through the horizontal control-volume faces



The same mass fluxes are used for neighboring grid cells - hence mass is conserved locally and globally.



#### Dynamics: 6. Advection (transport) and conservation – scalars

Mass in a control volume 
$$(\Delta x \Delta \eta)(\mu)^t$$
  
Scalar mass  $(\Delta x \Delta \eta)(\mu \phi)^t$ 

Mass conservation equation:

Scalar mass conservation equation:

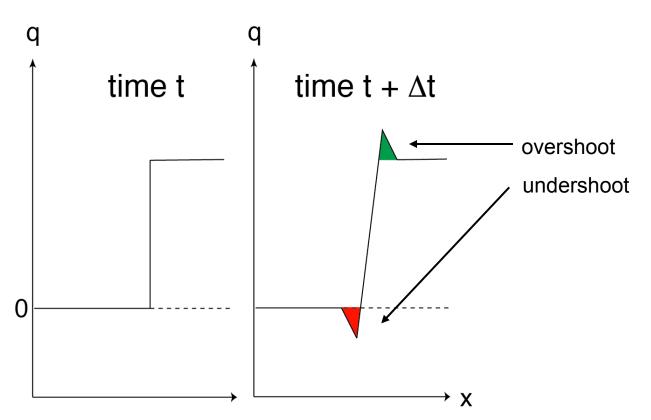
$$\Delta t^{-1} (\Delta x \Delta \eta) \cdot \left[ (\mu \phi)^{t+\Delta t} - (\mu \phi)^t \right] = \left[ (\mu u \phi \Delta \eta)_{x-\Delta x/2,\eta} - (\mu u \phi \Delta \eta)_{x+\Delta x/2,\eta} \right] + \left[ (\mu \omega \phi \Delta x)_{x,\eta-\Delta \eta/2} - (\mu \omega \phi \Delta x)_{x,\eta+\Delta \eta/2} \right]$$

change in tracer mass over a time step

tracer mass fluxes through control volume faces

#### Dynamics: 6. Advection (transport) and conservation – shape preserving





ARW transport is conservative, but not positive definite nor monotonic. Removal of negative q results in spurious source of q.

Dynamics: 6. Advection (transport) and conservation – shape preserving

Scalar update, last RK3 step

$$(\mu\phi)^{t+\Delta t} = (\mu\phi)^t - \Delta t \sum_{i=1}^n \delta_{x_i}[f_i] \qquad (1)$$

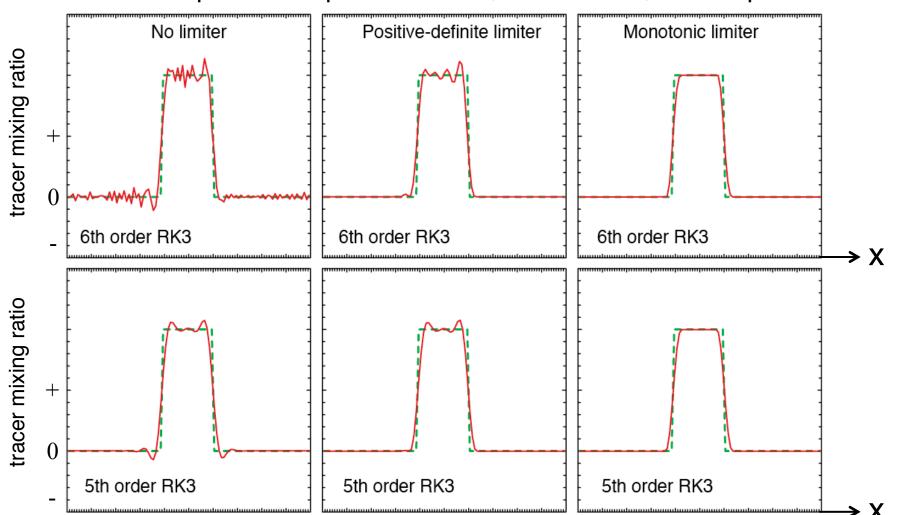
- (1) Decompose flux:  $f_i = f_i^{upwind} + f_i^c$
- (2) Renormalize high-order correction fluxes  $f_i^c$  such that solution is positive definite or monotonic:  $f_i^c = R(f_i^c)$
- (3) Update scalar eqn. (1) using  $f_i = f_i^{upwind} + R(f_i^c)$

Skamarock, MWR 2006, 2241-2250

#### Dynamics: 6. Advection (transport) and conservation – examples

1D Example: Top-Hat Advection

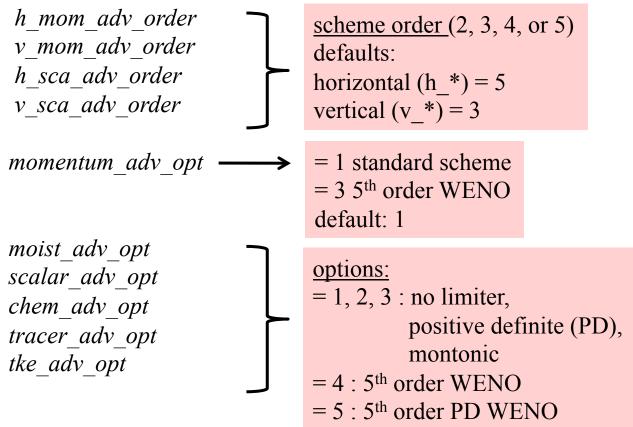
1D Top-hat transport Cr = 0.5, 1 revolution, 200 steps



#### Dynamics: 6. Advection (transport) and conservation

Where are the transport-scheme parameters?

# The namelist.input file: &dynamics



#### Dynamics: 7. Time step parameters

```
3^{\rm rd} order Runge-Kutta time step \Delta t_{RK}
```

Courant number limited, 1D:  $C_r = \frac{U\Delta t}{\Delta x} < 1.43$ 

Generally stable using a timestep approximately twice as large as used in a leapfrog model.

```
Where?
The namelist.input file:
    &domains

    time_step (integer seconds)
    time_step_fract_num
    time_step_fract_den
```

#### Dynamics: 7. Time step parameters

3rd order Runge-Kutta time step 
$$\Delta t_{RK}$$
 (&domains  $time\_step$ )

Acoustic time step

2D horizontal Courant number limited:  $C_r = \frac{C_s \Delta \tau}{\Delta h} < \frac{1}{\sqrt{2}}$ 
 $\Delta \tau_{sound} = \Delta t_{RK} / \text{(number of acoustic steps)}$ 

Where?

The namelist.input file:
&dynamics

 $time\ step\ sound\ (integer)$ 

#### Dynamics: 7. Time step parameters

 $3^{rd}$  order Runge-Kutta time step  $\Delta t_{RK}$  (&domains time\_step)

Acoustic time step [&dynamics time\_step\_sound (integer)]

Guidelines for time step

 $\Delta t_{RK}$  in seconds should be about  $6*\Delta x$  (grid size in kilometers). Larger  $\Delta t$  can be used in smaller-scale dry situations, but  $time\_step\_sound$  (default = 4) should increase proportionately if larger  $\Delta t$  is used.

If ARW blows up (aborts) quickly, try:

Decreasing  $\Delta t_{RK}$  (that also decreases  $\Delta t_{sound}$ ),

Or increasing time\_step\_sound (that decreases  $\Delta t_{sound}$  but does not change  $\Delta t_{RK}$ )

#### Dynamics: 8. Filters – divergence damping

Purpose: filter acoustic modes (3-D divergence,  $D = \nabla \cdot \rho \mathbf{V}$ )

$$\left\{ \frac{\partial \rho \mathbf{V}}{\partial t} + \nabla p + \dots = \gamma_d' \nabla D \right\}$$

$$\nabla \cdot \left\{ \quad \right\} \quad \rightarrow \quad \frac{\partial D}{\partial t} + \nabla^2 p + \dots = \gamma_d' \nabla^2 D$$

From the pressure equation:  $p_t \simeq c^2 D$ 

$$\frac{\partial \rho \mathbf{V}}{\partial t} + \nabla [p_{\tau} + \gamma_d (p^{\tau} - p^{\tau - \Delta \tau})] + \dots = 0$$

 $\gamma_d = 0.1$  recommended (default) (&dynamics *smdiv*)

(Illustrated in height coordinates for simplicity)

#### Dynamics: 8. Filters – time off-centering the vertical acoustic modes

Purpose: damp vertically-propagating acoustic modes

$$\frac{\partial W}{\partial t} + g \overline{\left(\mu_d - \frac{\alpha}{\alpha_d} \frac{\partial p}{\partial \eta}\right)}^{\tau} = \dots$$

$$\frac{\partial \phi}{\partial t} - \frac{g}{\mu_d^t} \overline{W}^{\tau} = \dots$$

$$\overline{(\phantom{A})}^{\tau} = \frac{1 + \beta}{2} \overline{(\phantom{A})}^{\tau + \Delta \tau} + \frac{1 - \beta}{2} \overline{(\phantom{A})}^{\tau}$$

Slightly forward centering the vertical pressure gradient damps 3-D divergence as demonstrated for the divergence damper

 $\beta$ = 0.1 recommended (default) [&dynamics *epssm*]

#### Dynamics: 8. Filters – external mode filter

Purpose: filter the external mode

Vertically integrated horizontal divergence, 
$$D_h = \int_1^0 (\nabla_{\eta} \cdot \mu \mathbf{V}_h) d\eta$$

$$\left\{ \frac{\partial \mu \mathbf{V}_h}{\partial t} + \dots = -\gamma_e \nabla_{\eta} D_h \right\}$$

$$\int_{1}^{0} \nabla_{\eta} \cdot \left\{ \right\} d\eta \quad \to \quad \frac{\partial D_h}{\partial t} + \dots = \gamma_e \nabla^2 D_h$$

Continuity equation: 
$$\frac{\partial \mu}{\partial t} = -\nabla_{\eta} \cdot \mu \mathbf{V}_h - \frac{\partial \mu \dot{\eta}}{\partial \eta} = D_h$$

$$\frac{\partial \mu \mathbf{V}_h}{\partial \tau} + \dots = -\gamma_e \frac{\Delta x^2}{\Delta \tau^2} \nabla_{\eta} (\mu^{\tau} - \mu^{\tau - \Delta \tau})$$

 $\gamma_e = 0.01$  recommended (default) [&dynamics *emdiv*]

(Primarily for real-data applications)

#### Dynamics: 8. Filters – vertical velocity damping

### Purpose: damp anomalously-large vertical velocities

(usually associated with anomalous physics tendencies)

#### Additional term:

$$\partial_t W = \dots - \mu_d \operatorname{sign}(W) \gamma_w (Cr - Cr_\beta)$$
$$Cr = \left| \frac{\Omega dt}{\mu d\eta} \right|$$

```
Cr_{\beta}=1.0 typical value (default)

[share/module_model_constants.F w_beta]

\gamma_w = 0.3 m/s² recommended (default)

[share/module_model_constants.F w_alpha]

[&dynamics w damping 0 (off; default) 1 (on)]
```

#### Dynamics: 8. Filters – 2D Smagorinsky

# 2nd-Order Horizontal Mixing, Horizontal-Deformation-Based K<sub>h</sub>

Purpose: mixing on horizontal coordinate surfaces (real-data applications) [&dynamics  $diff\ opt=1, km\ opt=4$ ]

$$K_{h} = C_{s}^{2} l^{2} \left[ 0.25(D_{11} - D_{22})^{2} + \overline{D_{12}^{2}}^{xy} \right]^{\frac{1}{2}}$$
where
$$l = (\Delta x \Delta y)^{1/2}$$

$$D_{11} = 2 m^{2} [\partial_{x} (m^{-1}u) - z_{x} \partial_{z} (m^{-1}u)]$$

$$D_{22} = 2 m^{2} [\partial_{y} (m^{-1}v) - z_{y} \partial_{z} (m^{-1}v)]$$

$$D_{12} = m^{2} [\partial_{y} (m^{-1}u) - z_{y} \partial_{z} (m^{-1}u)$$

$$+ \partial_{x} (m^{-1}v) - z_{x} \partial_{z} (m^{-1}v)]$$

 $C_s = 0.25$  (Smagorinsky coefficient, default value) [&dynamics  $c_s$ ]

#### Dynamics: 8. Filters – gravity-wave absorbing layer

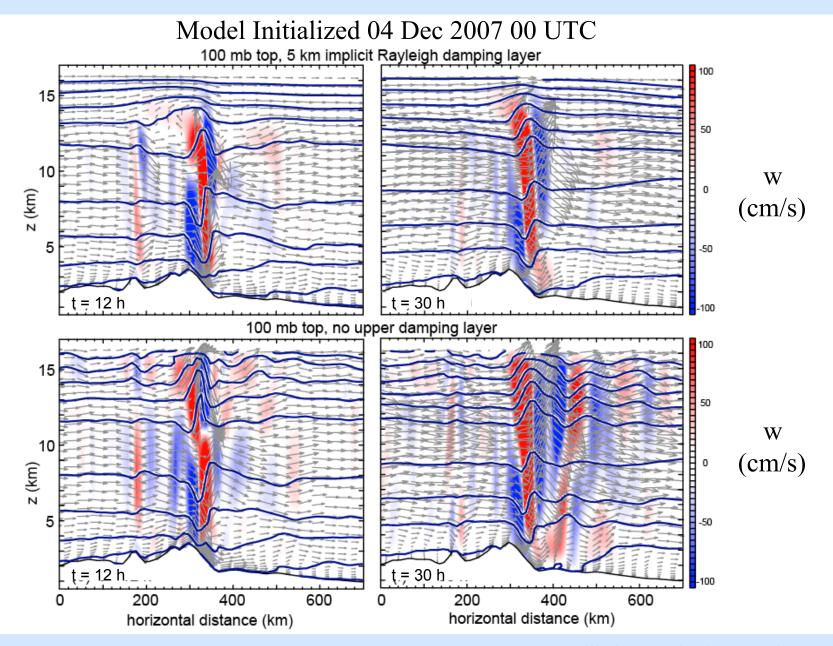
Implicit Rayleigh w Damping Layer for Split-Explicit Nonhydrostatic NWP Models (gravity-wave absorbing layer)

$$W^{\tau + \Delta \tau} = W^{*\tau + \Delta \tau} - \Delta \tau R_w(\eta) W^{\tau + \Delta \tau}$$

$$R_w(\eta) = \begin{cases} \gamma_r \sin^2 \left[ \frac{\pi}{2} \left( 1 - \frac{z_{top} - z}{z_d} \right) \right] & \text{for } z \ge (z_{top} - z_d); \\ 0 & \text{otherwise,} \end{cases} \begin{cases} R_w(\eta) - \text{damping rate (t^1)} \\ z_d - \text{depth of the damping layer} \\ \gamma_r - \text{damping coefficient} \end{cases}$$

[&dynamics  $damp\_opt = 3$  (default = 0)] [&dynamics  $damp\_coef = 0.2$  (recommended, = 0. default)] [&dynamics zdamp = 5000. ( $z_d$  (meters); default); height below model top where damping begins]

#### Dynamics: 8. Filters – gravity-wave absorbing layer example



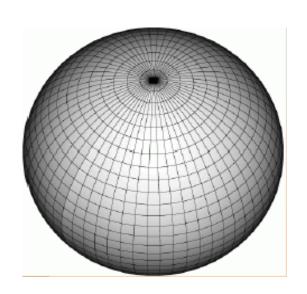
#### Dynamics: 9. Map projections and global configuration

#### ARW Model: projection options

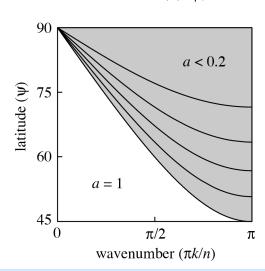
- 1. Cartesian geometry: idealized cases
- 2. Lambert Conformal: mid-latitude applications
- 3. Polar Stereographic: high-latitude applications
- 4. Mercator: low-latitude applications
- 5. Latitude-Longitude global, regional

Projections 1-4 are isotropic  $(m_x = m_y)$ Latitude-longitude projection is anistropic  $(m_x \neq m_y)$ 

#### Dynamics: 9. Map projections and global configuration



Filter Coefficient a(k),  $\psi_0 = 45^\circ$ 



#### Global ARW – Polar filters

Converging gridlines severely limit timestep. The polar filter removes this limitation.

Filter procedure - Along a grid latitude circle:

- 1. Fourier transform variable.
- 2. Filter Fourier coefficients.
- 3. Transform back to physical space.

$$\hat{\phi}(k)_{filtered} = a(k)\,\hat{\phi}(k), \text{ for all } k$$

$$a(k) = \min \left[ 1., \max \left( 0., \left( \frac{\cos \psi}{\cos \psi_o} \right)^2 \frac{1}{\sin^2(\pi k/n)} \right) \right]$$

k = dimensionless wavenumber

 $\hat{\phi}(k)$  = Fourier coefficients from forward transform

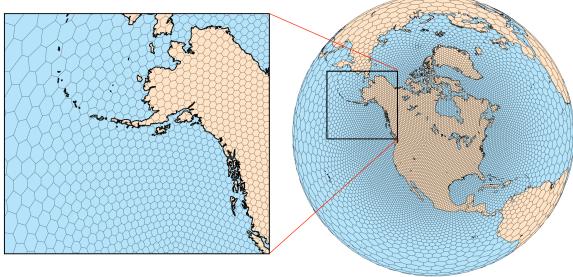
a(k) =filter coefficients

 $\psi = \text{ latitude } \psi_o = \text{ polar filter latitude, filter when } |\psi| > \psi_o$ 

#### Dynamics: 9. Map projections and global configuration

An alternative to global ARW...





- Global, nonhydrostatic, C-grid Voronoi mesh
- Numerics similar to WRF; WRF-NRCM physics
- No pole problems
- Variable-resolution mesh no nested BC problems

Available at: http://mpas-dev.github.io/









#### Dynamics: 10. Boundary condition options

#### ARW Model: Boundary Condition Options

#### Lateral boundary conditions

- 1. Specified (Coarse grid, real-data applications).
- 2. Open lateral boundaries (gravity-wave radiative).
- 3. Symmetric lateral boundary condition (free-slip wall).
- 4. Periodic lateral boundary conditions.
- 5. Nested boundary conditions (specified).

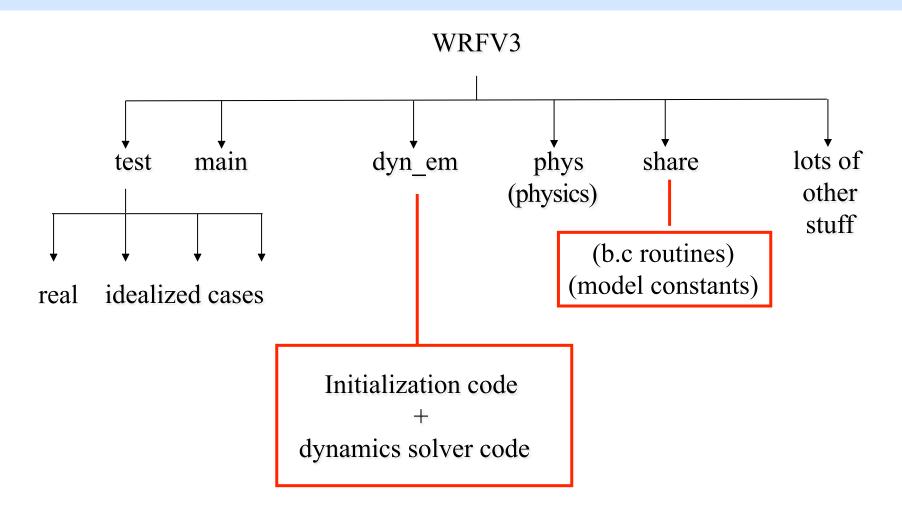
#### Top boundary conditions

1. Constant pressure.

#### Bottom boundary conditions

- 1. Free slip.
- 2. Various B.L. implementations of surface drag, fluxes.

#### Dynamics: Where are things?



#### WRF ARW Tech Note

A Description of the Advanced Research WRF Version 3 (June 2008, 2012 update) http://www.mmm.ucar.edu/wrf/users/pub-doc.html