

Update on Development of Nudging FDDA for Advanced Research WRF

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UPDATE: MM5 FDDA IN BATTLEFIELD **Rapidly Relocatable Nowcast-Prediction System (RRNPS) for US Army: MMS-Profiler**

- MM5-based system with FDDA run locally on the battlefield to provide Warfighter MET.
- Fielded to active Army units and approved for full rate production.
- Provides Local and Target Area MET
- Provides MET Messages every 15-30 minutes
- Provides as a minimum MET Parameters
 - Temperature, Humidity
 - Pressure
 - Wind Speed, Wind Direction
 - Target Area: Ceiling, Visibility, Precip Rate, Precip Type



**... RRNPS adapted for DOD DTRA in-house weather support
by Penn State (Titan Team)**

Flux-Form Equations in Mass Coordinate

Hydrostatic pressure coordinate:

hydrostatic pressure π

$$\eta = \frac{(\pi - \pi_t)}{\mu}, \quad \mu = \pi_s - \pi_t$$

Conserved state variables:

$$\mu, \quad U = \mu u, \quad V = \mu v, \quad W = \mu w, \quad \Theta = \mu \theta$$

Non-conserved state variable: $\phi = g z$

Flux-Form Equations in Mass Coordinate

Inviscid, 2-D
equations
without rotation:

$$\frac{\partial U}{\partial t} + \mu \alpha \frac{\partial p}{\partial x} + \frac{\partial p}{\partial \eta} \frac{\partial \phi}{\partial x} = - \frac{\partial U u}{\partial x} - \frac{\partial \Omega u}{\partial \eta}$$

$$\frac{\partial W}{\partial t} + g \left(\mu - \frac{\partial p}{\partial \eta} \right) = - \frac{\partial U w}{\partial x} - \frac{\partial \Omega w}{\partial \eta}$$

$$\frac{\partial \Theta}{\partial t} + \frac{\partial U \theta}{\partial x} + \frac{\partial \Omega \theta}{\partial \eta} = \mu Q$$

$$\frac{\partial \mu}{\partial t} + \frac{\partial U}{\partial x} + \frac{\partial \Omega}{\partial \eta} = 0$$

$$\frac{d\phi}{dt} = g w$$

Diagnostic
relations:

$$\frac{\partial \phi}{\partial \eta} = -\mu \alpha, \quad p = \left(\frac{R \theta}{p_0 \alpha} \right)^{\gamma}, \quad \Omega = \mu \dot{\eta}$$

Height/Mass-Coordinate Model, Time Integration

3rd Order Runge-Kutta time integration

advance $\phi^t \rightarrow \phi^{t+1}$

$$\phi^* = \phi^t + \frac{\Delta t}{3} R(\phi^t)$$

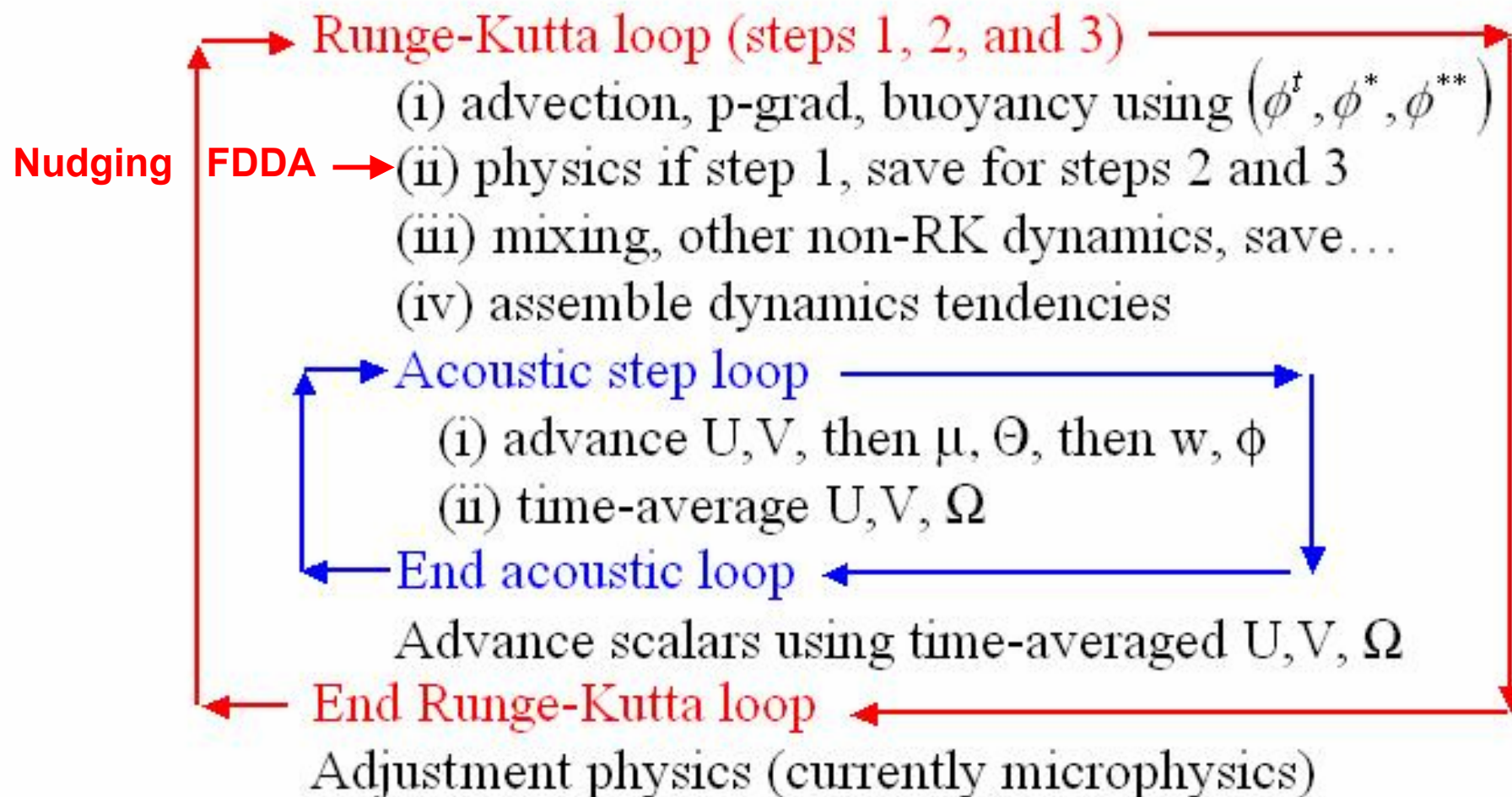
$$\phi^{**} = \phi^t + \frac{\Delta t}{2} R(\phi^*)$$

$$\phi^{t+1} = \phi^t + \Delta t R(\phi^{**})$$

Amplification factor $\phi_t = i k \phi$; $\phi^{n+1} = A \phi^n$; $|A| = 1 - \frac{(k\Delta t)^4}{24}$

WRF Mass-Coordinate Model Integration Procedure

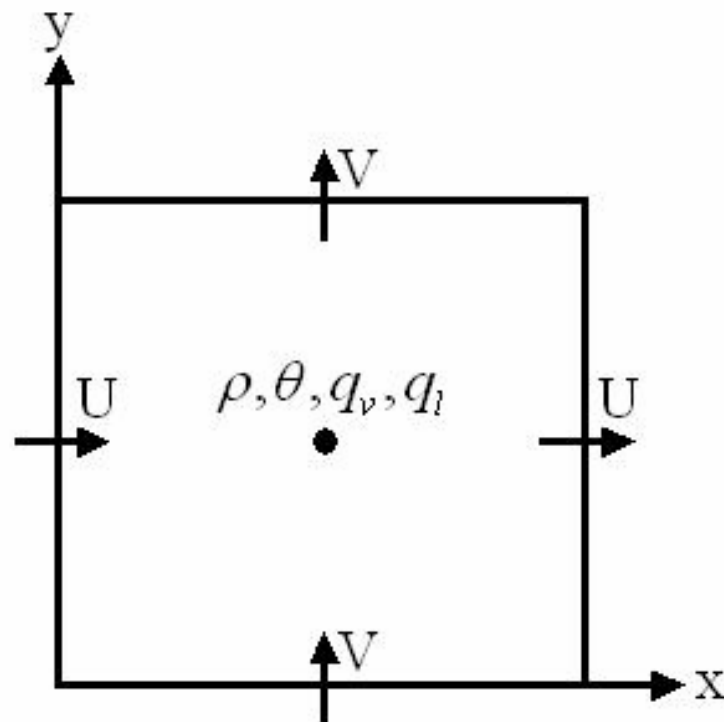
Begin time step



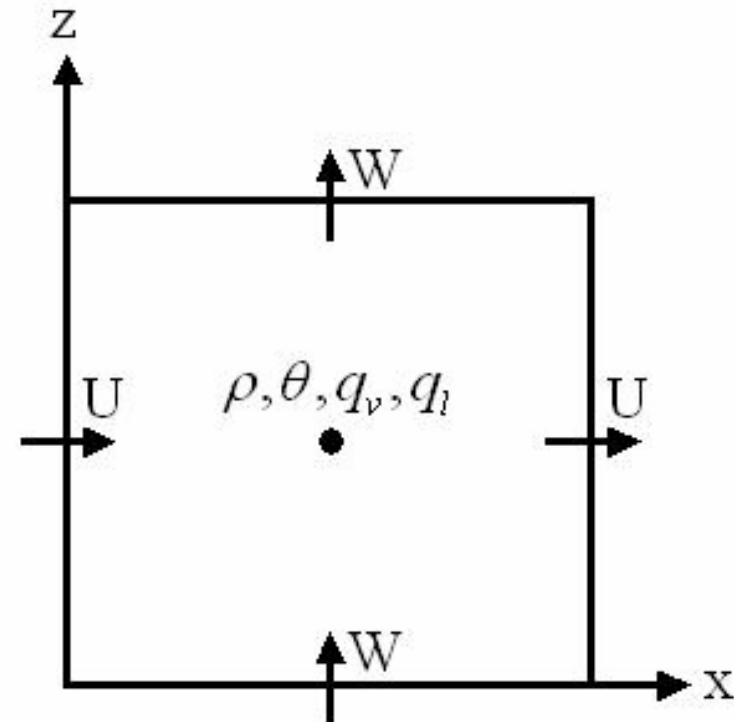
End time step

Height/Mass-coordinate model, grid staggering

C-grid staggering



horizontal



vertical

Note: Nudging FDDA on staggered grid while physics on non-staggered grid...

Nudging FDDA

$$\frac{\partial \alpha}{\partial t} = G \bullet (\alpha_{ob} - \alpha) + \dots$$

$$\int_0^t () dt \Rightarrow \alpha(t) = (\alpha_0 - \alpha_{ob}) \bullet e^{-Gt} + \alpha_{ob}$$

$$\alpha(t) = (\alpha_o - \alpha_{ob}) \bullet e^{-Gt} + \alpha_{ob}$$

$$\frac{1}{G} \equiv e - \text{folding time} \quad O(1h)$$

Nudging FDDA in WRF

For $\alpha = \Theta = \mu \bullet \theta$

$$\frac{\partial \Theta}{\partial t} = \dots + \mu \frac{\partial \theta}{\partial t} + \theta \frac{\partial \mu}{\partial t}$$

$$\begin{aligned} \frac{\partial \Theta}{\partial t} = \dots + \mu \bullet G_{\theta} \bullet W \bullet (\theta_{ob} - \theta) \\ + \theta \bullet G_{\mu} \bullet W \bullet (\mu_{ob} - \mu) \end{aligned}$$

where $W = w_{xy} \bullet w_{\eta} \bullet w_t$

3D Analyses from MM5 Frontend...

- “mm5_p_convert” (written by Wei Wang/NCAR)
- Converts multi-time pressure-level data from MM5 Frontend (REGRID, RAWINS, LITTLE_R) into HINTERP fields
 - Introduces MM5 frontend data into WRFSl-formatted output
 - Enables common initial conditions and lateral boundary conditions for “fair” comparison of MM5 and WRF simulations from fields based on the same surface and pressure-level analyses. (Note that there are still differences in the state variables and horizontal / vertical grid structures between the two models)
 - **Enables WRF analysis nudging towards frontend MM5 system (Rawins) analyses**
- Passes through to WRF common domain definitions and underlying static fields (lat, lon, terrain, land use, etc.)
- Requires special version of VINTERP to create input for REAL

Sfc Analyses from MM5 Frontend...

- **“wrfsfcfdda” (written by Tanya Otte /NOAA/ARL)**
- **Converts RAWINS/LITTLE_R “SFCFDDA” files to WRF I/O API**
- **Includes all SFCFDDA 2D fields, plus U- and V-component winds on C grid, PSFC, θ**
- **Files will be used for surface analysis nudging in WRF**
- **Files will also support soil moisture nudging option in Pleim-Xiu LSM**

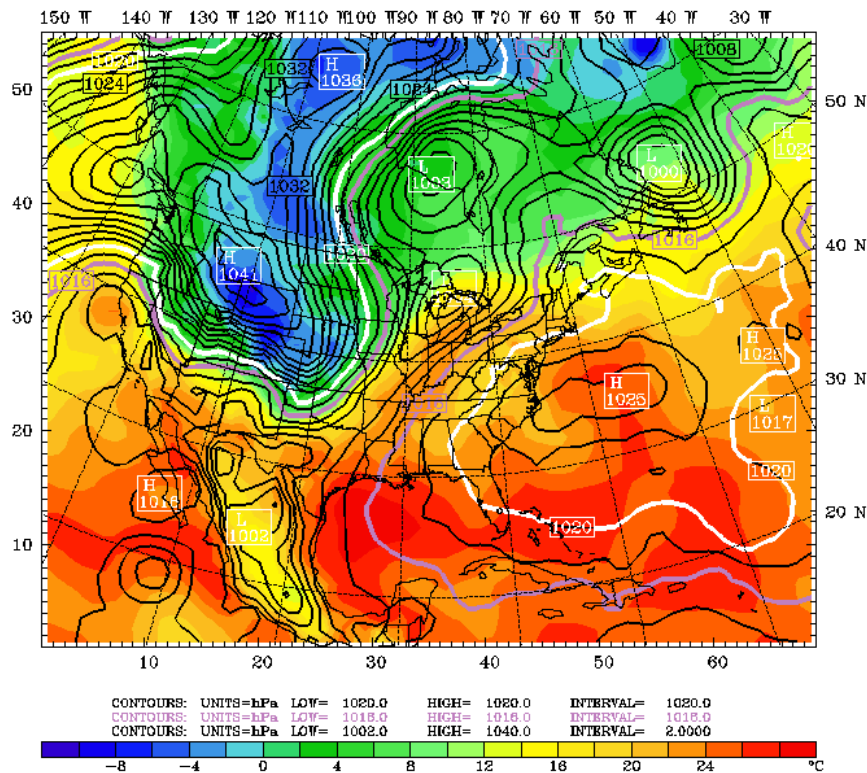
Preliminary Results

Demonstration of WRF Analysis Nudging:

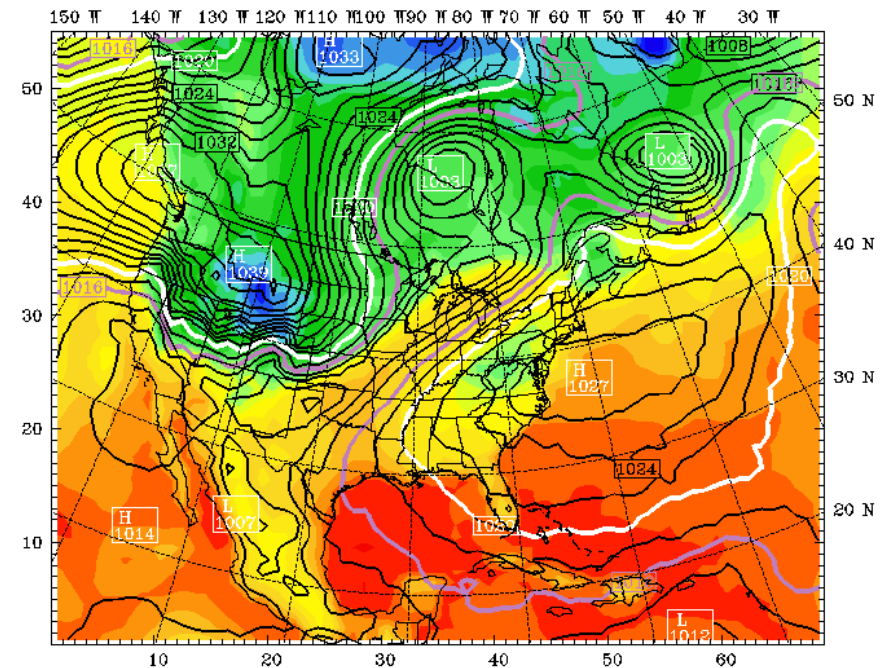
- Based on 12-hourly MM5 front-end 3D analyses...
- Nudge u, v, θ ($G = 3 \times 10^{-4} \text{ s}^{-1}$)
- Nudge q_v ($G = 1 \times 10^{-5} \text{ s}^{-1}$)
- Show results at 48 h for CAPTEX83 (18-20 September 1983)

Surface Temperature and Sea Level Pressure

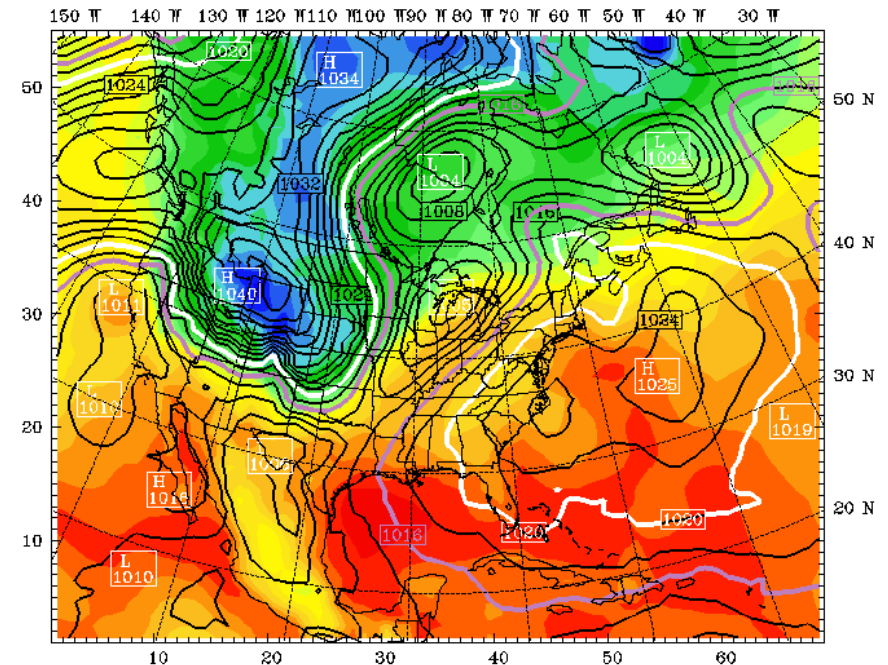
Dataset: mm5 RIP: mm5 interp Init: 1200 UTC Sun 18 Sep 83
 Fcst: 48.00 Valid: 1200 UTC Tue 20 Sep 83 (0900 LDT Tue 20 Sep 83)
 Temperature at k-index = 32
 Sea-level pressure
 Sea-level pressure
 Sea-level pressure



MM5
ANALYSIS



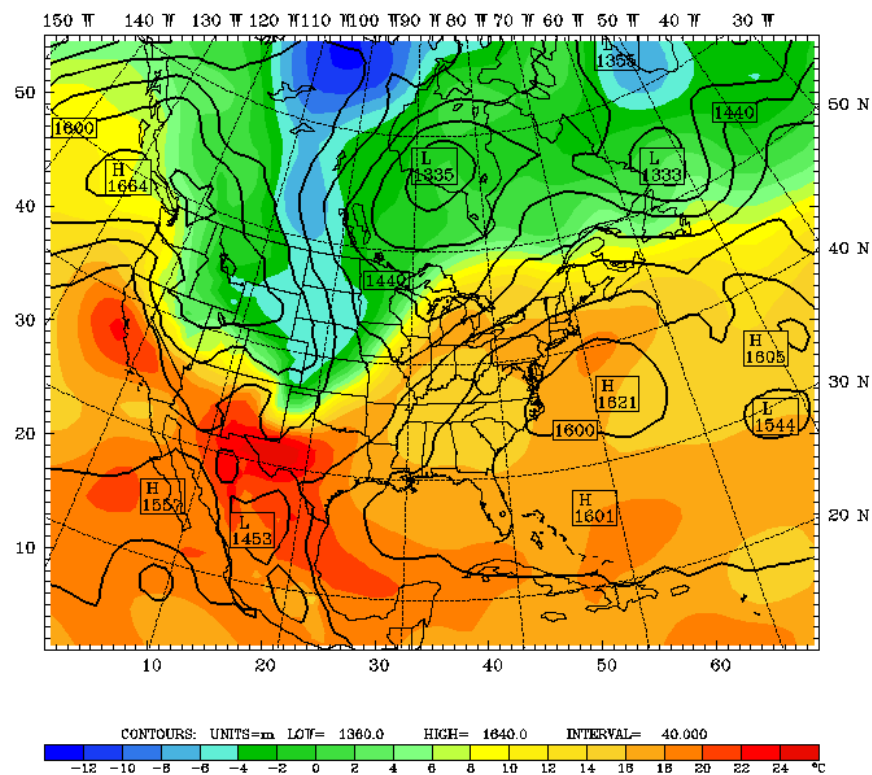
WRF NO FDDA



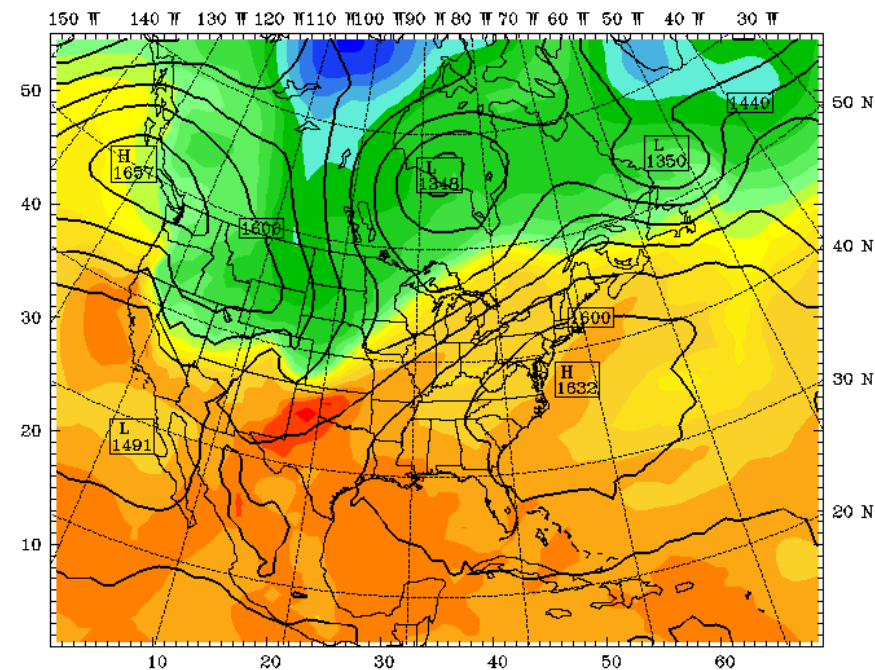
WRF FDDA

850 hPa Temperature and Geopotential Height

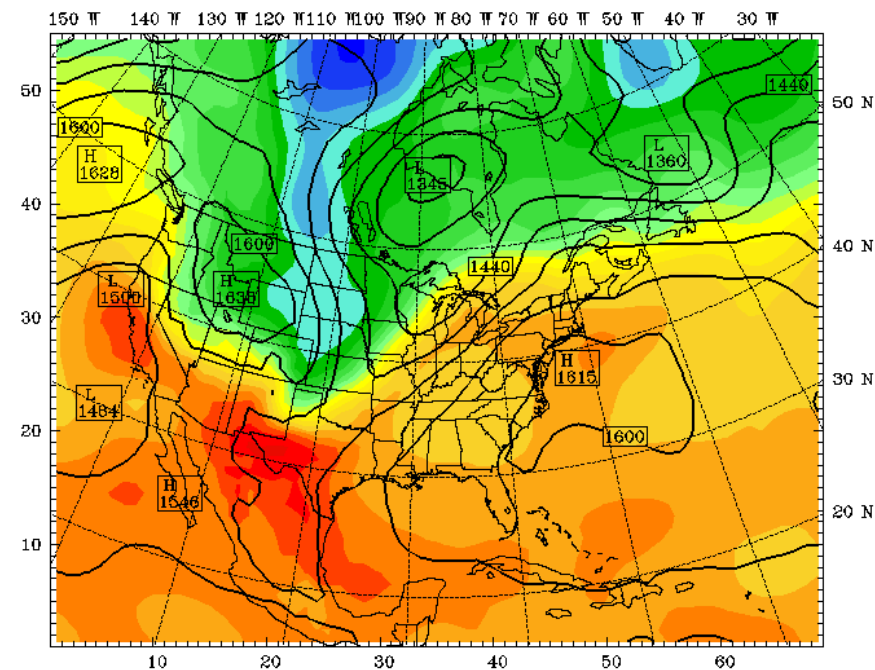
Dataset: mm5 RIP: mm5 interp Init: 1200 UTC Sun 18 Sep 83
Fest: 48.00 Valid: 1200 UTC Tue 20 Sep 83 (0900 LDT Tue 20 Sep 83)
Temperature at pressure = 850 hPa
Geopotential height at pressure = 850 hPa



MM5
ANALYSIS



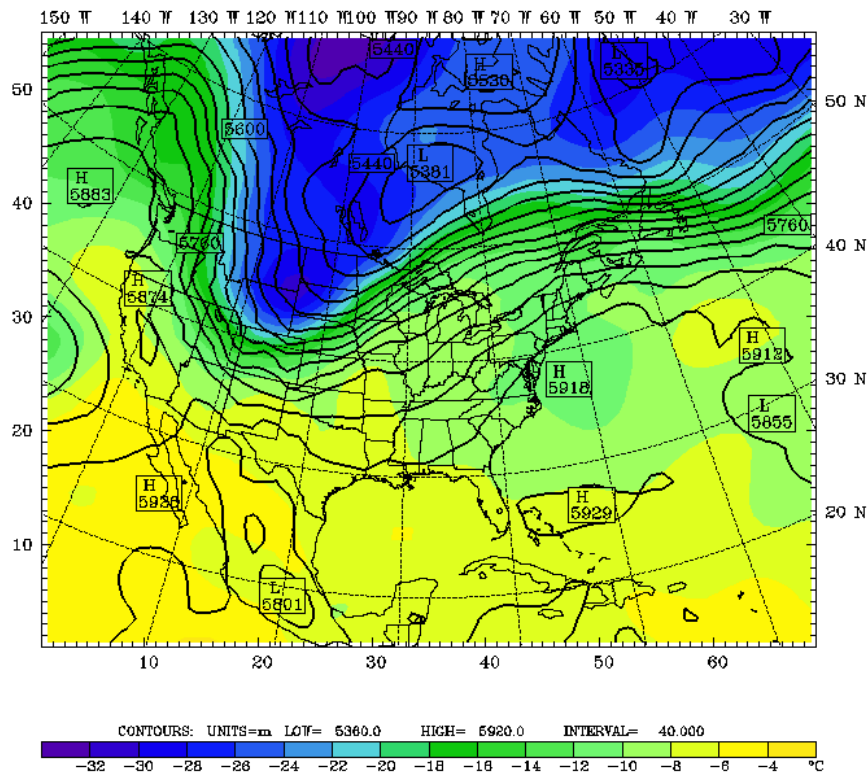
WRF NO FDDA



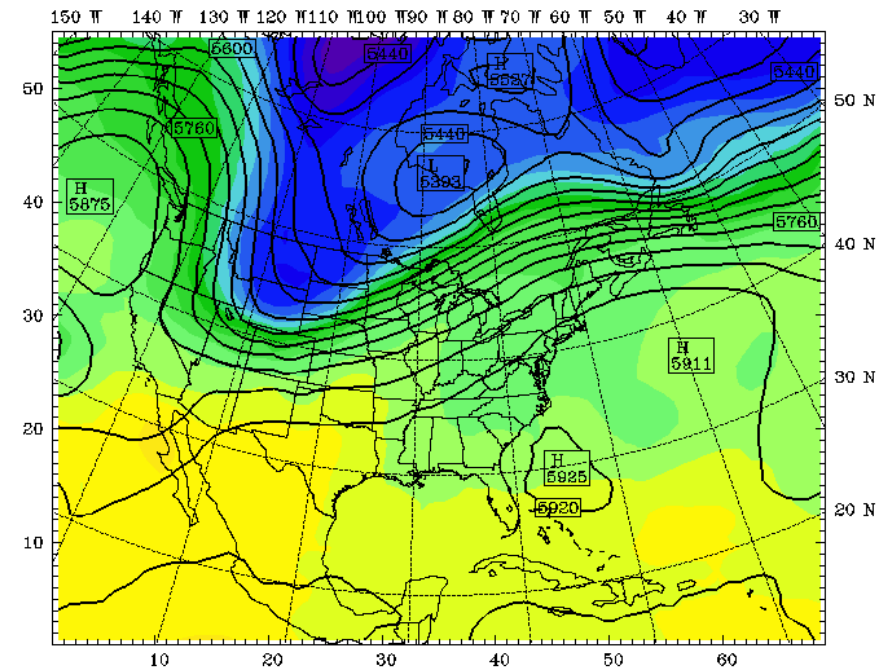
WRF FDDA

500 hPa Temperature and Geopotential Height

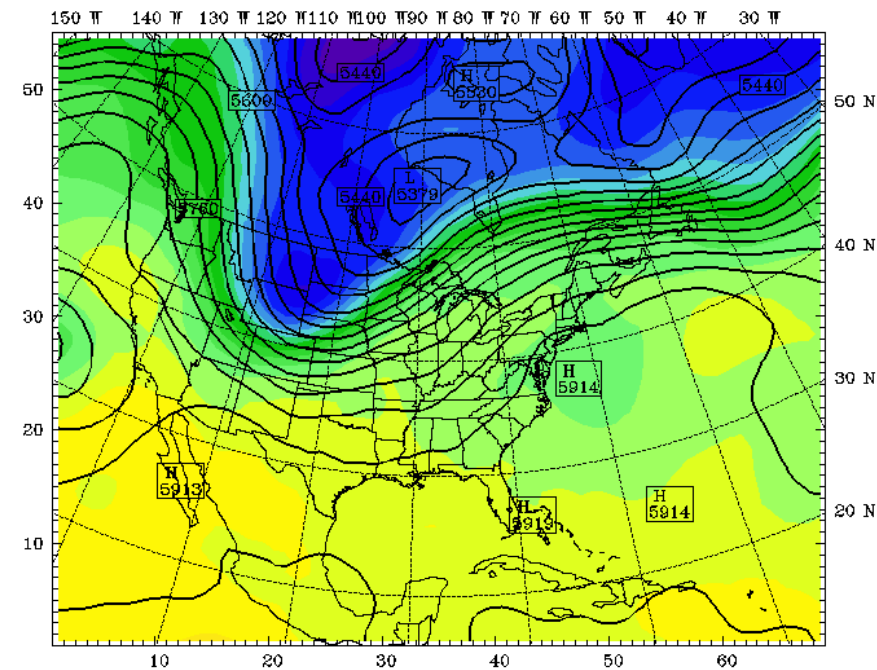
Dataset: mm5 RIP: mm5 interp Init: 1200 UTC Sun 18 Sep 83
Fcst: 48.00 Valid: 1200 UTC Tue 20 Sep 83 (0900 LDT Tue 20 Sep 83)
Temperature at pressure = 500 hPa
Geopotential height at pressure = 500 hPa



MM5 ANALYSIS



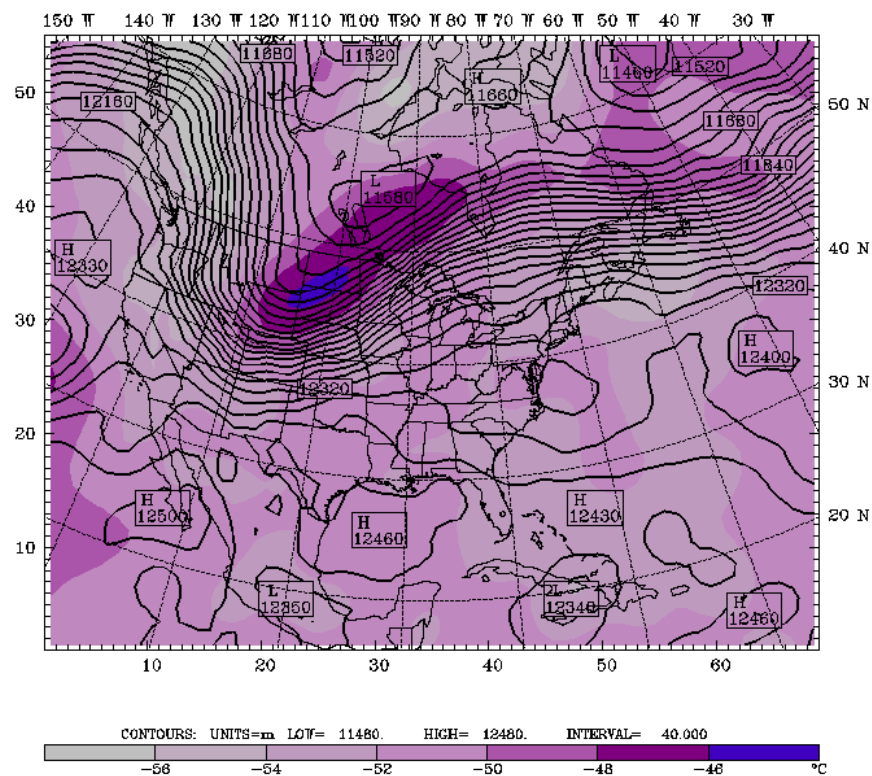
WRF NO FDDA



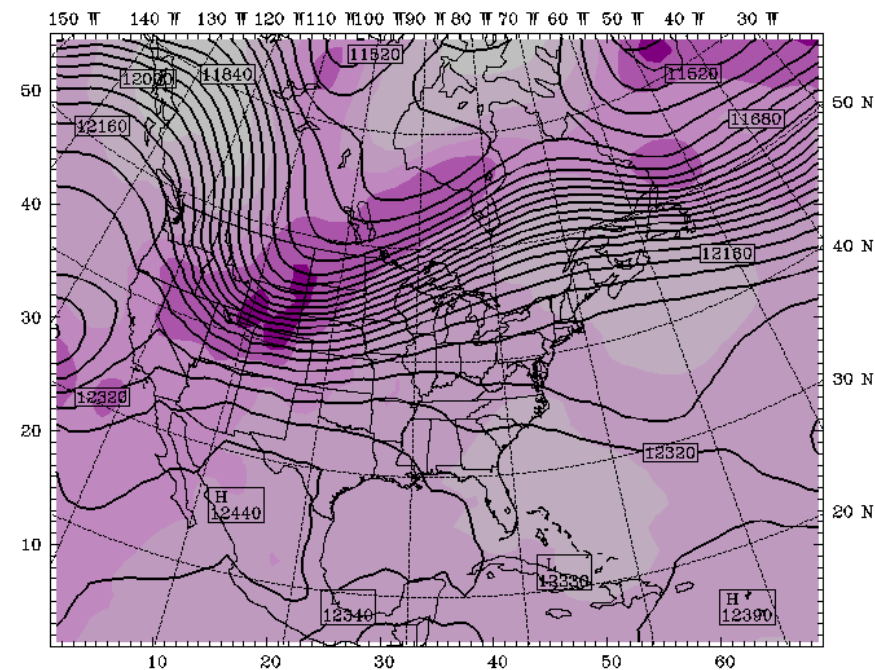
WRF FDDA

200 hPa Temperature and Geopotential Height

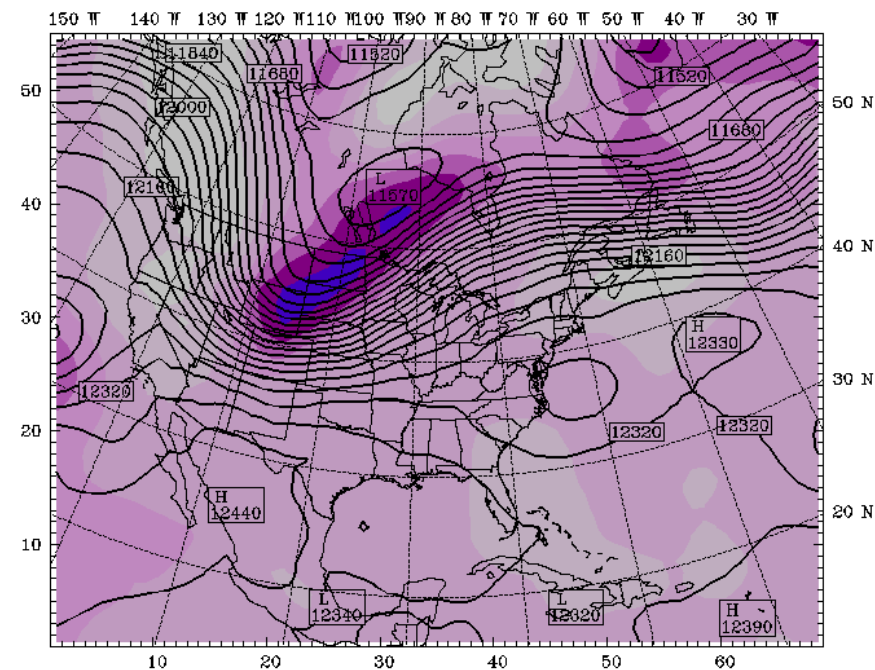
Dataset: mm5 RIP: mm5 interp Init: 1200 UTC Sun 18 Sep 83
Fcst: 48.00 Valid: 1200 UTC Tue 20 Sep 83 (0900 LDT Tue 20 Sep 83)
Temperature at pressure = 200 hPa
Geopotential height at pressure = 200 hPa



MM5
ANALYSIS



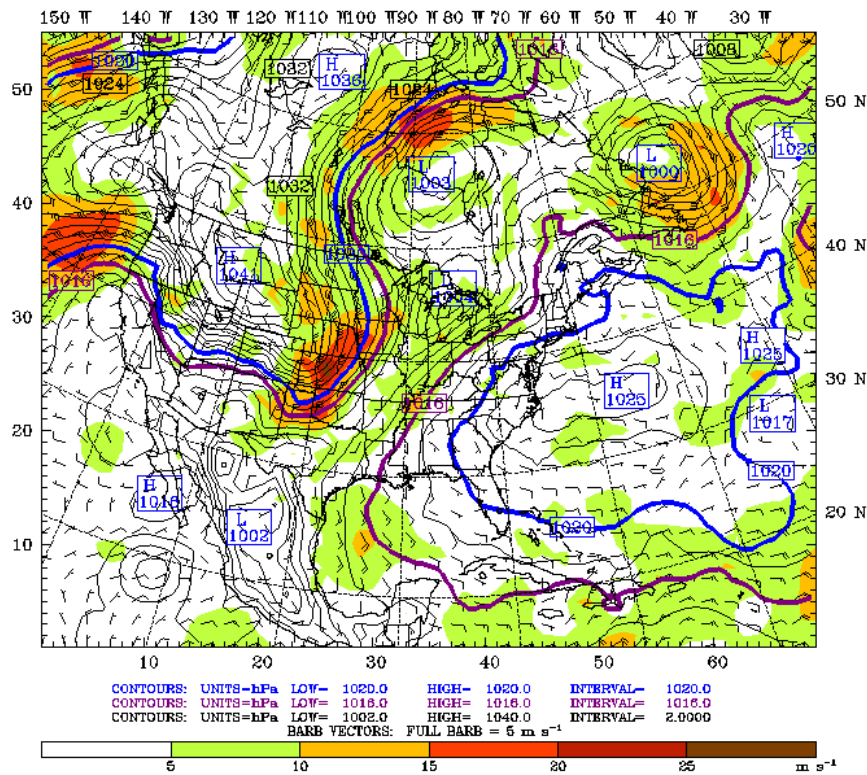
WRF NO FDDA



WRF FDDA

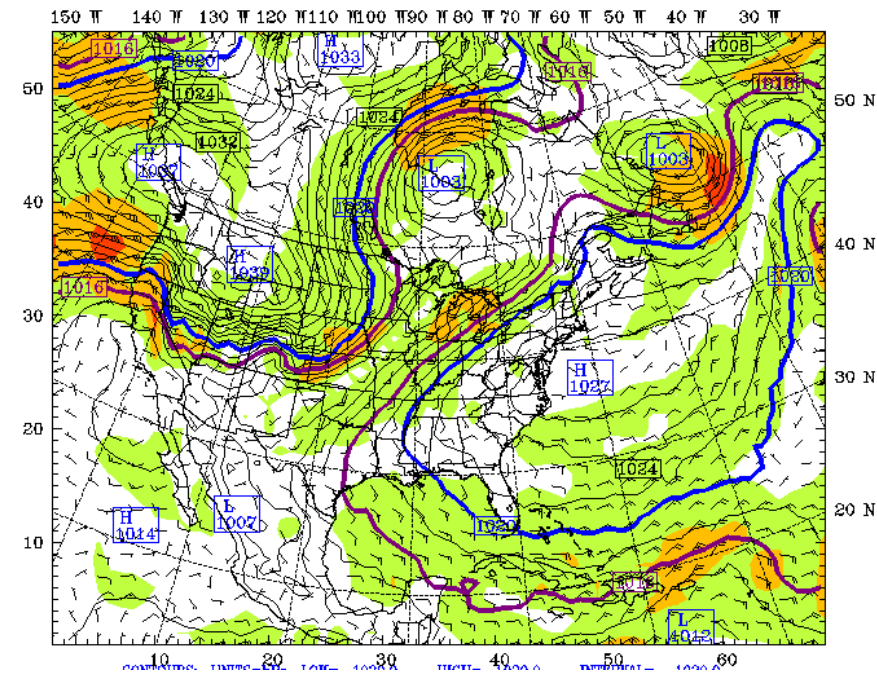
Surface Winds and Sea Level Pressure

Dataset: mm5 RIP: mm5 interp Init: 1200 UTC Sun 18 Sep 83
 Fcst: 48.00 Valid: 1200 UTC Tue 20 Sep 83 (0900 LDT Tue 20 Sep 83)
 Horizontal wind speed at k-index = 32
 Horizontal wind vectors at k-index = 32
 Sea-level pressure
 Sea-level pressure
 Sea-level pressure



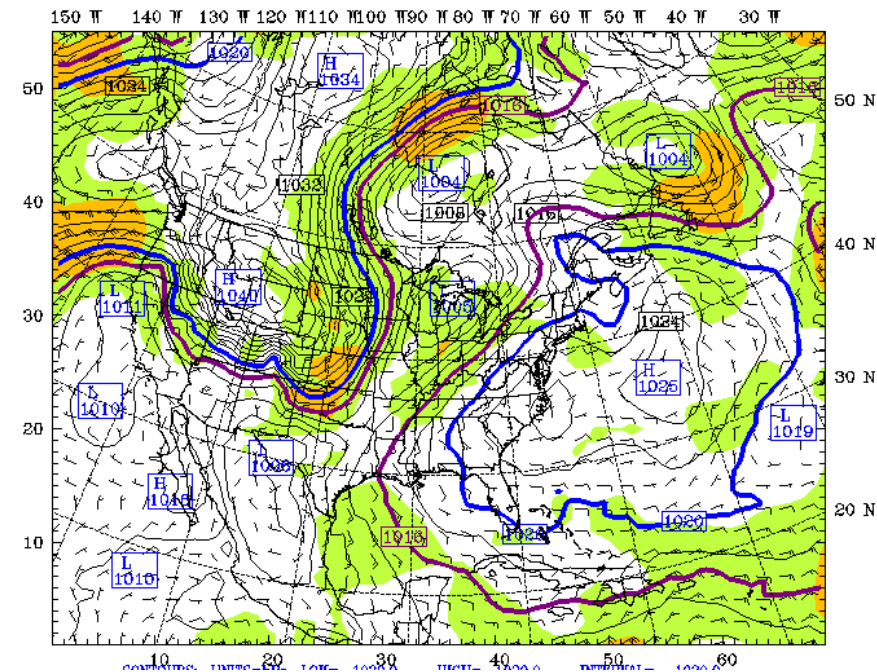
MM5
ANALYSIS

Sea-level pressure



WRF NO FDDA

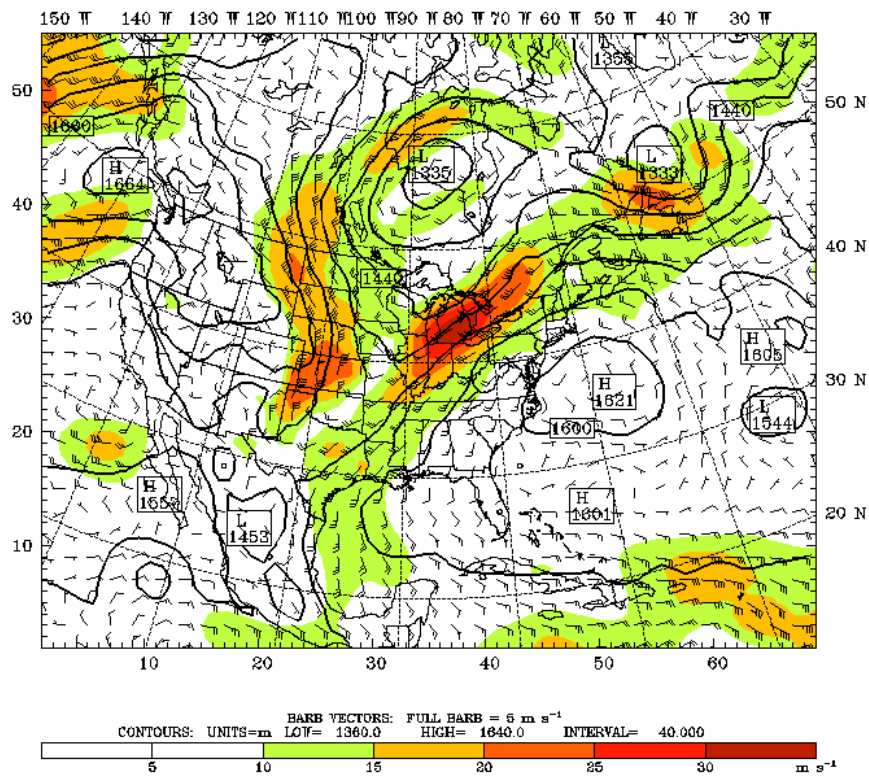
Sea-level pressure



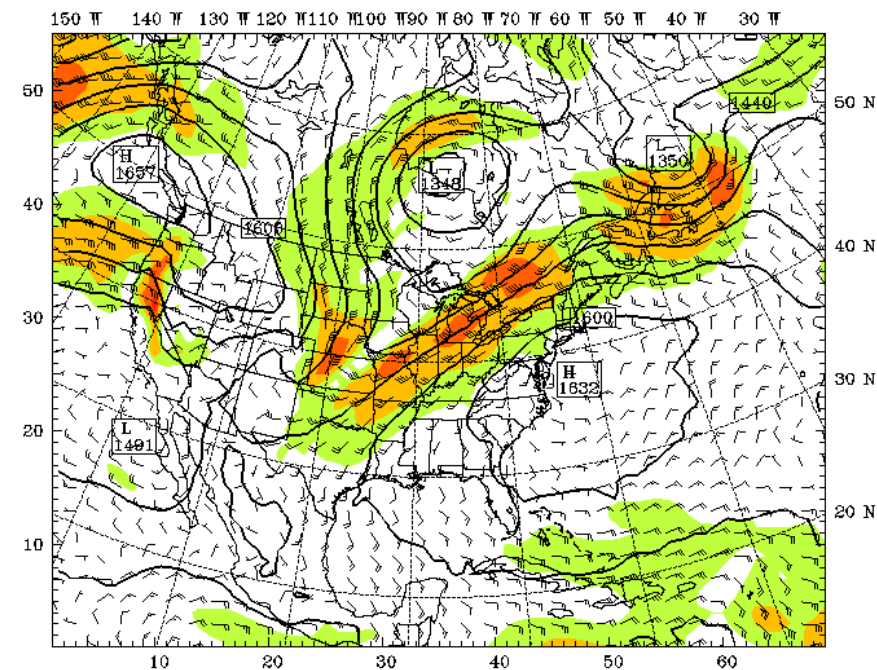
WRF FDDA

850 hPa Winds and Geopotential Height

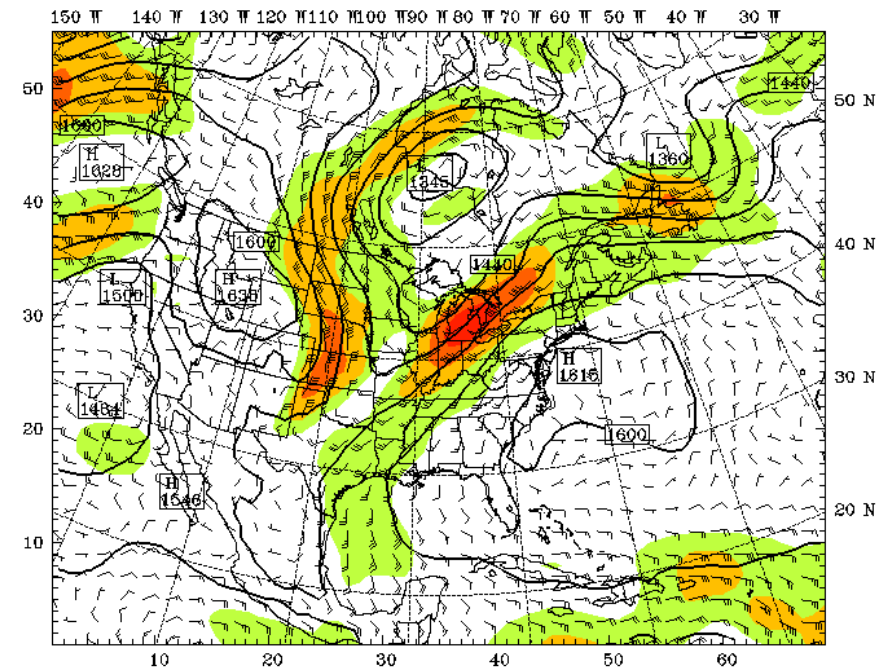
Dataset: mm5 RIP: mm5 interp Init: 1200 UTC Sun 18 Sep 83
 Fcst: 48.00 Valid: 1200 UTC Tue 20 Sep 83 (0900 LDT Tue 20 Sep 83)
 Horizontal wind speed at pressure = 850 hPa
 Geopotential height at pressure = 850 hPa
 Horizontal wind vectors at pressure = 850 hPa



MM5
ANALYSIS



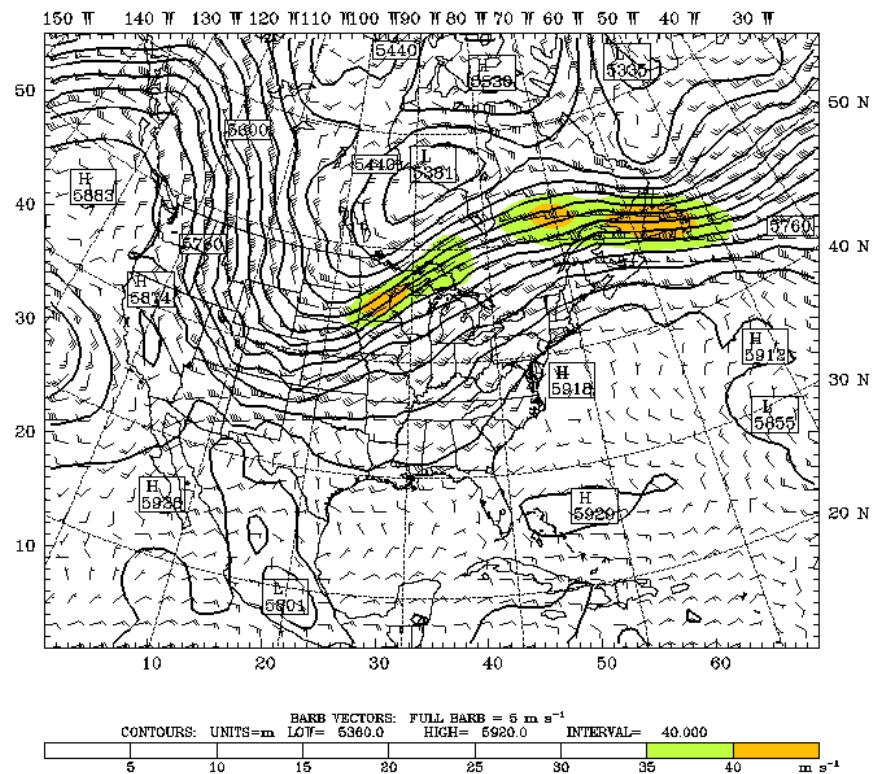
WRF NO FDDA



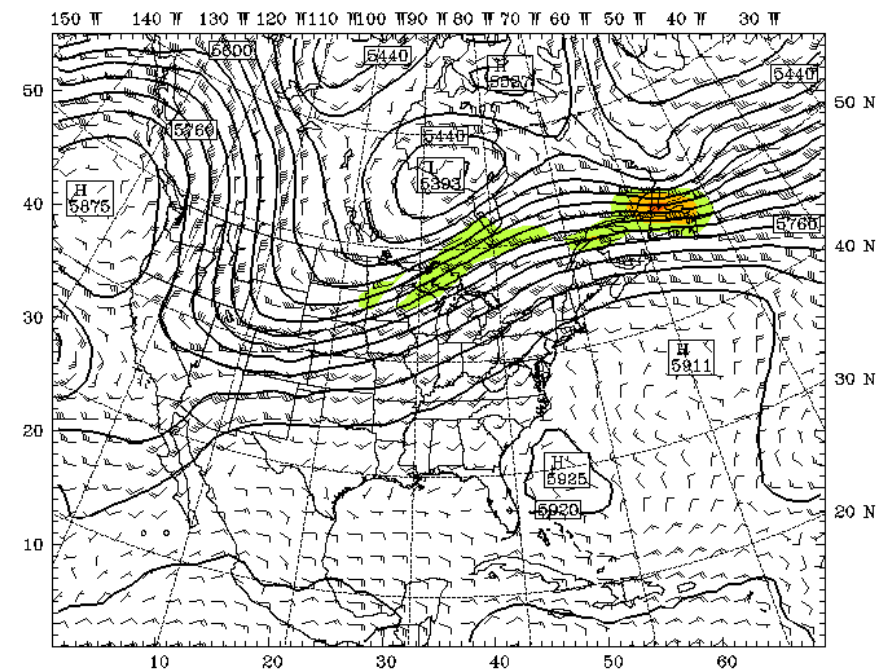
WRF FDDA

500 hPa Winds and Geopotential Height

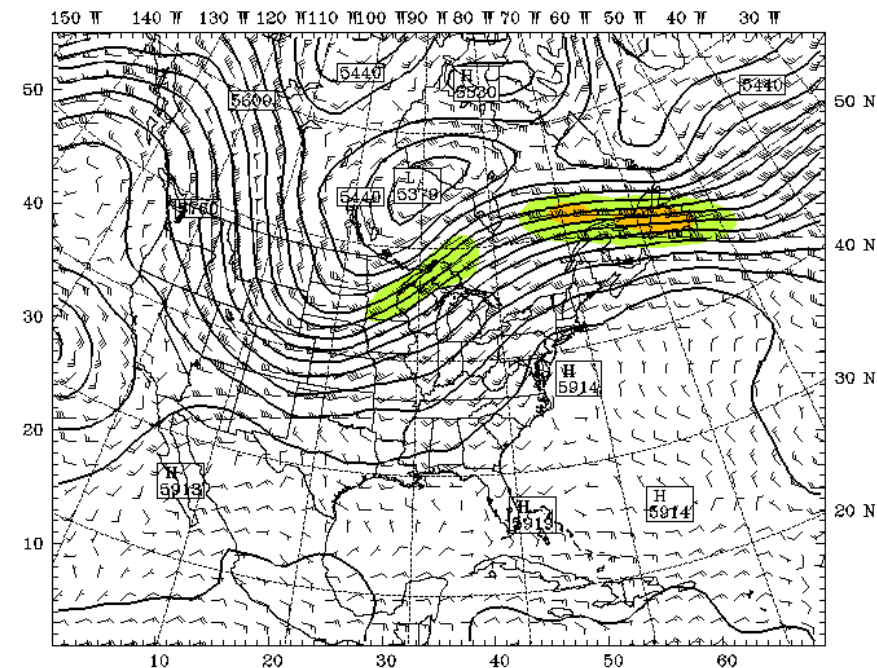
Dataset: mm5 RIP: mm5 interp Init: 1200 UTC Sun 18 Sep 83
 Fcst: 48.00 Valid: 1200 UTC Tue 20 Sep 83 (0900 LDT Tue 20 Sep 83)
 Horizontal wind speed at pressure = 500 hPa
 Geopotential height at pressure = 500 hPa
 Horizontal wind vectors at pressure = 500 hPa



MM5
ANALYSIS



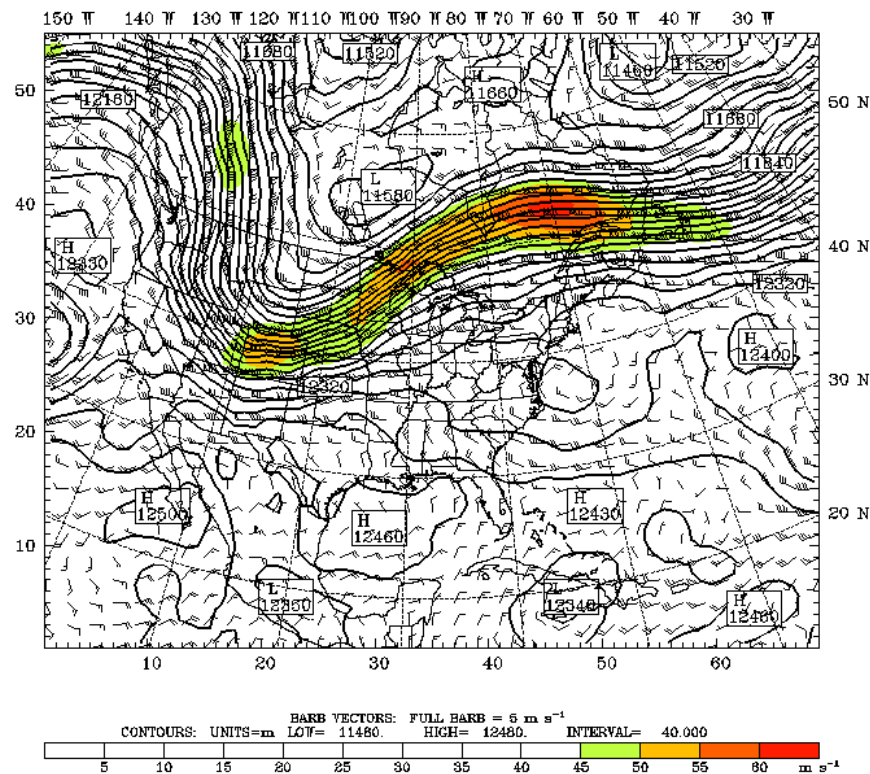
WRF NO FDDA



WRF FDDA

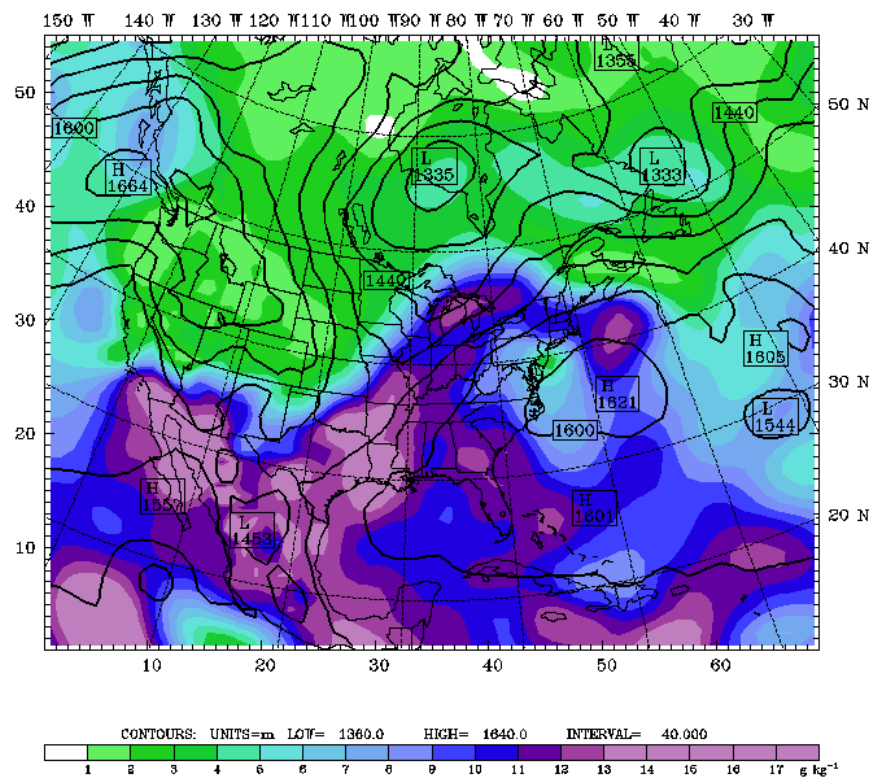
200 hPa Winds and Geopotential Height

Dataset: mm5 RIP: mm5 interp Init: 1200 UTC Sun 18 Sep 83
 Fcst: 48.00 Valid: 1200 UTC Tue 20 Sep 83 (0900 LDT Tue 20 Sep 83)
 Horizontal wind speed at pressure = 200 hPa
 Geopotential height at pressure = 200 hPa
 Horizontal wind vectors at pressure = 200 hPa

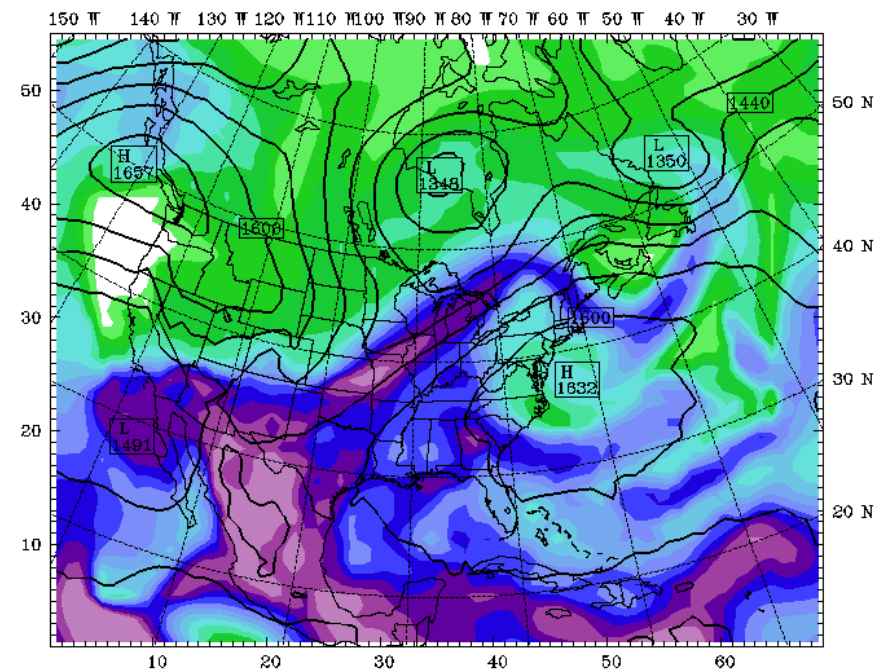


850 hPa Mixing Ratio and Geopotential Height

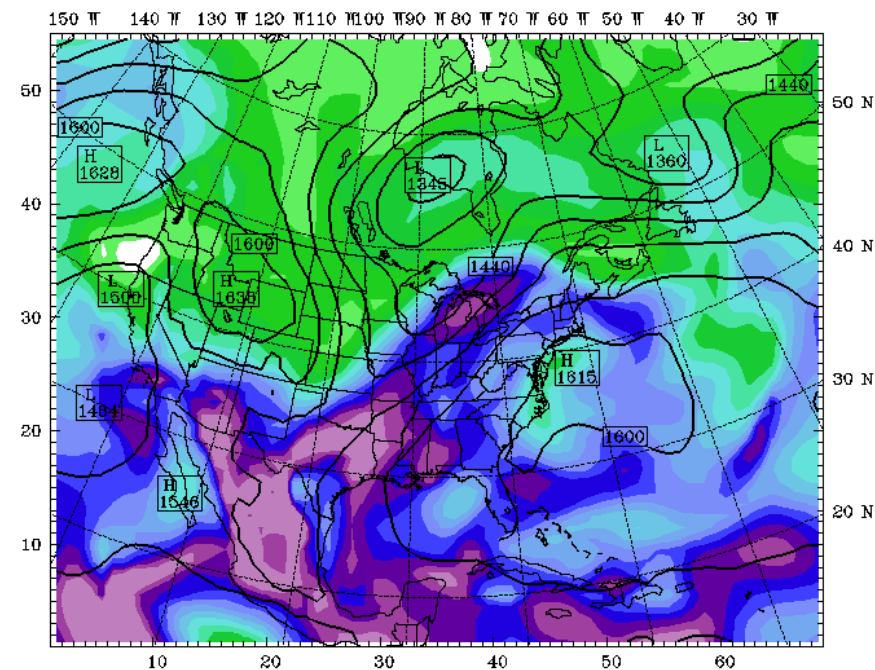
Dataset: mm5 RIP: mm5 interp Init: 1200 UTC Sun 18 Sep 83
 Fcst: 48.00 Valid: 1200 UTC Tue 20 Sep 83 (0900 LDT Tue 20 Sep 83)
 Water vapor mixing ratio at pressure = 850 hPa
 Geopotential height at pressure = 850 hPa



MM5
ANALYSIS

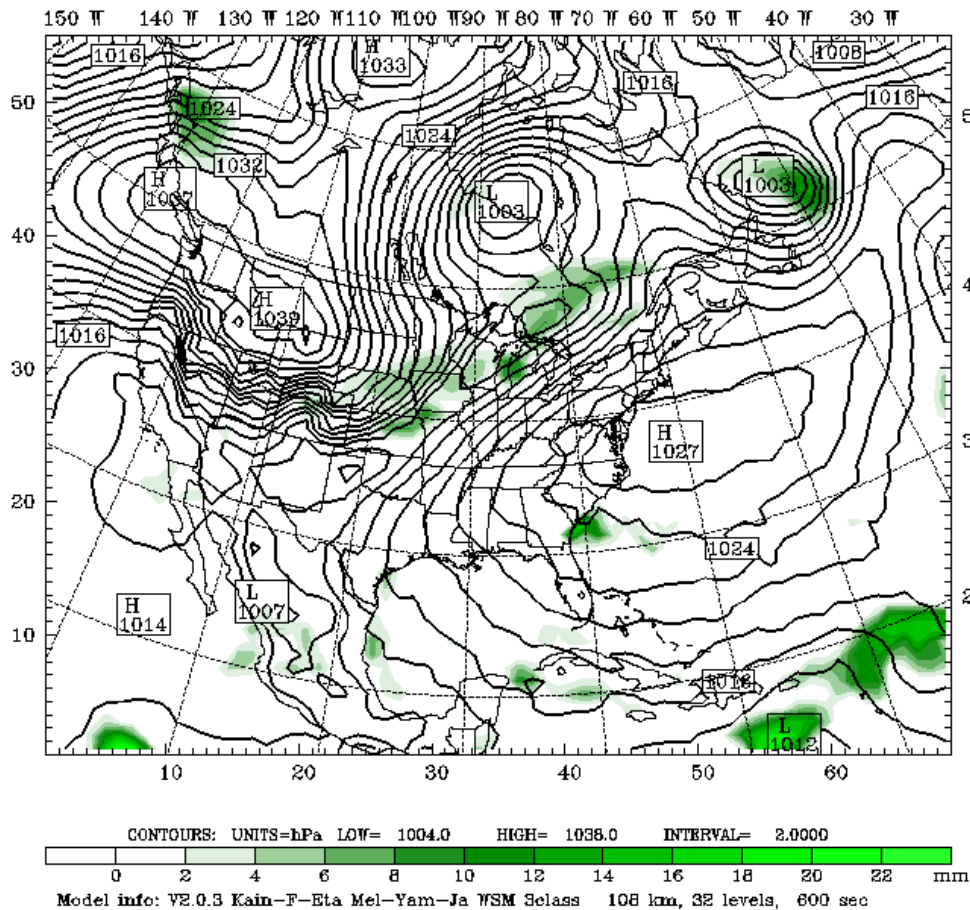


WRF NO FDDA

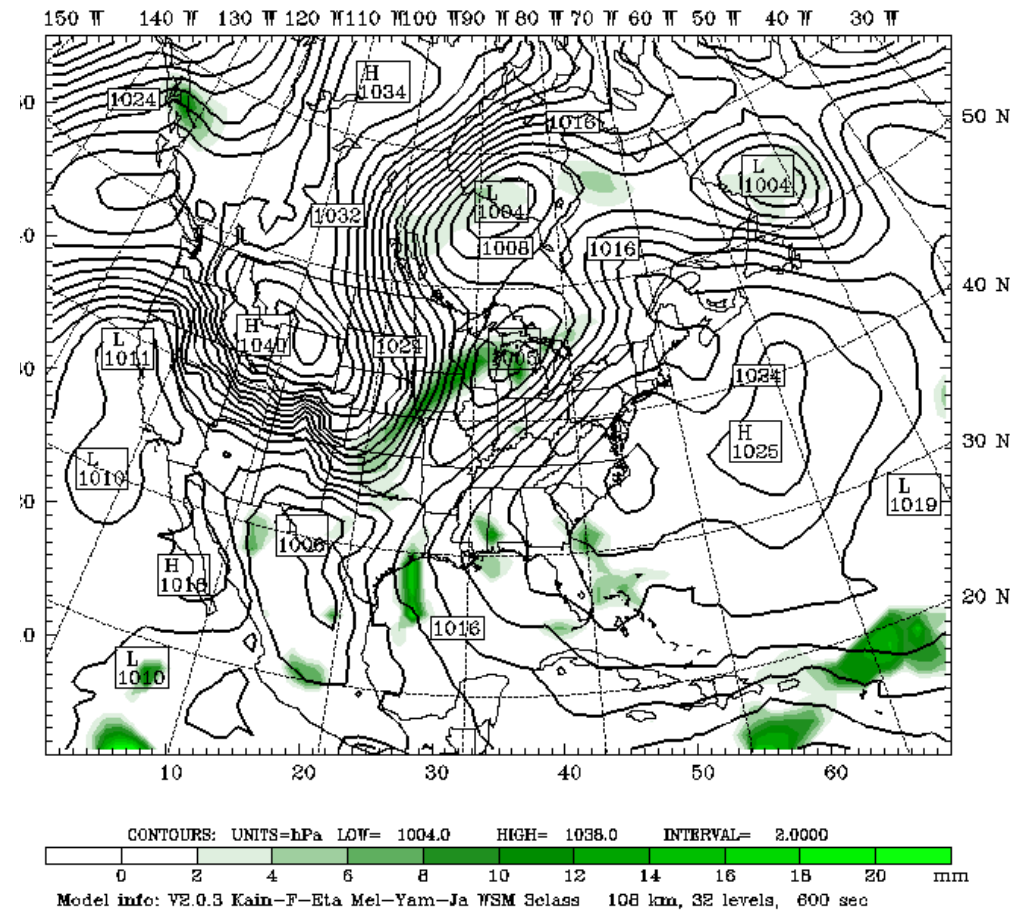


WRF FDDA

Precipitation and Sea Level Pressure



WRF NO FDDA



WRF FDDA

Summary

Analysis Nudging FDDA in WRF – ARW:

Preliminary capabilities:

3D analysis nudging of gridded fields (u , v , θ , q_v):

Analyses on WRF model surfaces (η)

- External gridded analyses processed through Real
- Real input files created in “converter code” from Rawins surface and pressure-level gridded analyses (MM5 frontend).
- Real also processes other gridded fields (SI, 3DVAR)
- (Standard version of Real had to be modified to output more than first time period...)

Currently uses linear temporal interpolations and uniform spatial weighting functions

Summary

Future capabilities:

More general temporal and spatial weighting functions, including use of PBL height, observation data densities, dynamic-initialization ramping functions, etc.

Surface analysis nudging using higher temporal resolution surface-gridded fields, applied at surface and throughout PBL (Stauffer et al. 1991).

- Requires another “converter” using Rawins sfcfdda files since 3DVAR cannot currently produce surface-only analyses at intermediate times...
- Enables Pleim-Xu LSM soil moisture nudging capability
- List of nudging variables to be expanded (e.g., μ , vertical motion, cloud water, etc.)

Acknowledgments

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- **Wei Wang (NCAR) and Annette Gibbs and Glenn Hunter (Penn State) have also contributed time and supporting software...**

Disclaimer

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Supplementary Slides



WRF Output to MM5 Output Format

- **“wrf2mm5” (written by Annette Lario-Gibbs / PSU)**
- **Reads WRF output and converts it to MM5 output format.**
- **Produces outputs for use in VEROBS (PSU verification software).**
- **wrf2mm5 output can be read by VEROBS, RIP4 and READV3.**

WRF Output to MM5 Output (cont'd)

- **wrf2mm5 currently writes out u, v, T, q, pp, pstar, convective rain, non-convective rain, terrain, mapscale factors, Coriolis, latitude, longitude, landuse, pbl height, and sigma_h.**
- **Can be easily modified to convert and write out other WRF variables for use in other post-processing programs.**

Moist Equations in Mass-Coordinate Model

Moist Equations:

$$\frac{\partial U}{\partial t} + \alpha \mu_a \frac{\partial p}{\partial x} + \frac{\alpha}{\alpha_a} \frac{\partial p}{\partial \eta} \frac{\partial \phi}{\partial x} = - \frac{\partial U u}{\partial x} - \frac{\partial \Omega u}{\partial \eta}$$

$$\frac{\partial W}{\partial t} + g \left(\mu_a - \frac{\alpha}{\alpha_a} \frac{\partial p}{\partial \eta} \right) = - \frac{\partial U w}{\partial x} - \frac{\partial \Omega w}{\partial \eta}$$

$$\frac{\partial \mu_a}{\partial t} + \frac{\partial U}{\partial x} + \frac{\partial \Omega}{\partial \eta} = 0$$

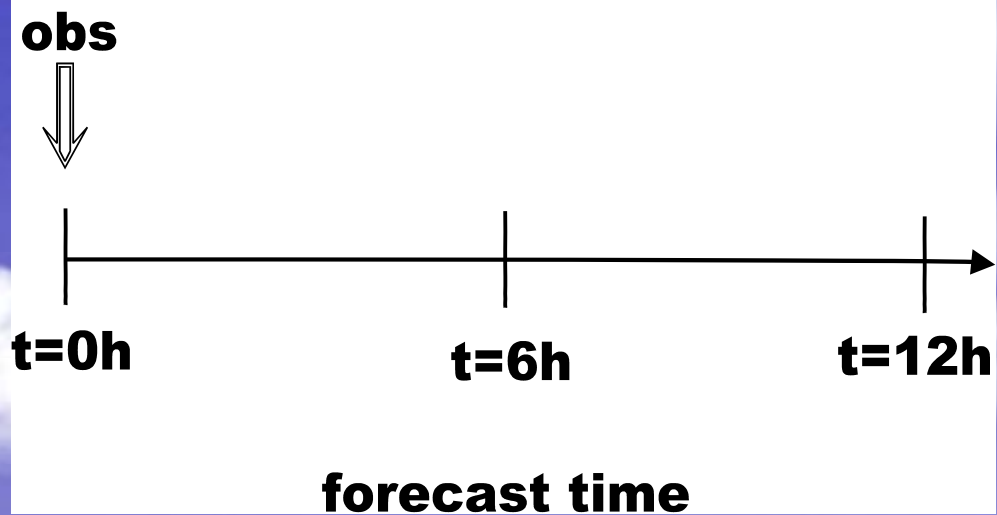
$$\frac{\partial (\mu_a q_{v,l})}{\partial t} + \frac{\partial U q_{v,l}}{\partial x} + \frac{\partial \Omega q_{v,l}}{\partial \eta} = \mu_a Q_{v,l}$$

Diagnostic relations:

$$\frac{\partial \phi}{\partial \eta} = -\alpha_a \mu_a, \quad p = \left(\frac{R \Theta}{p_o \mu_a \alpha_v} \right)^{\gamma}$$



Cold Start - Static Initialization





Running Start - Dynamic Initialization

