

**ON THE REPRESENTATION
OF SNOW IN
BULK MICROPHYSICAL PARAMETERIZATIONS**

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Why work with a “classic” single-moment 5-class bulk scheme?

[specifically, the Reisner et al. (1998) /
Thompson et al. (2004), or “R-T” scheme]:



As computer power increases, enhanced sophistication in cloud microphysics will always compete with the desire to:

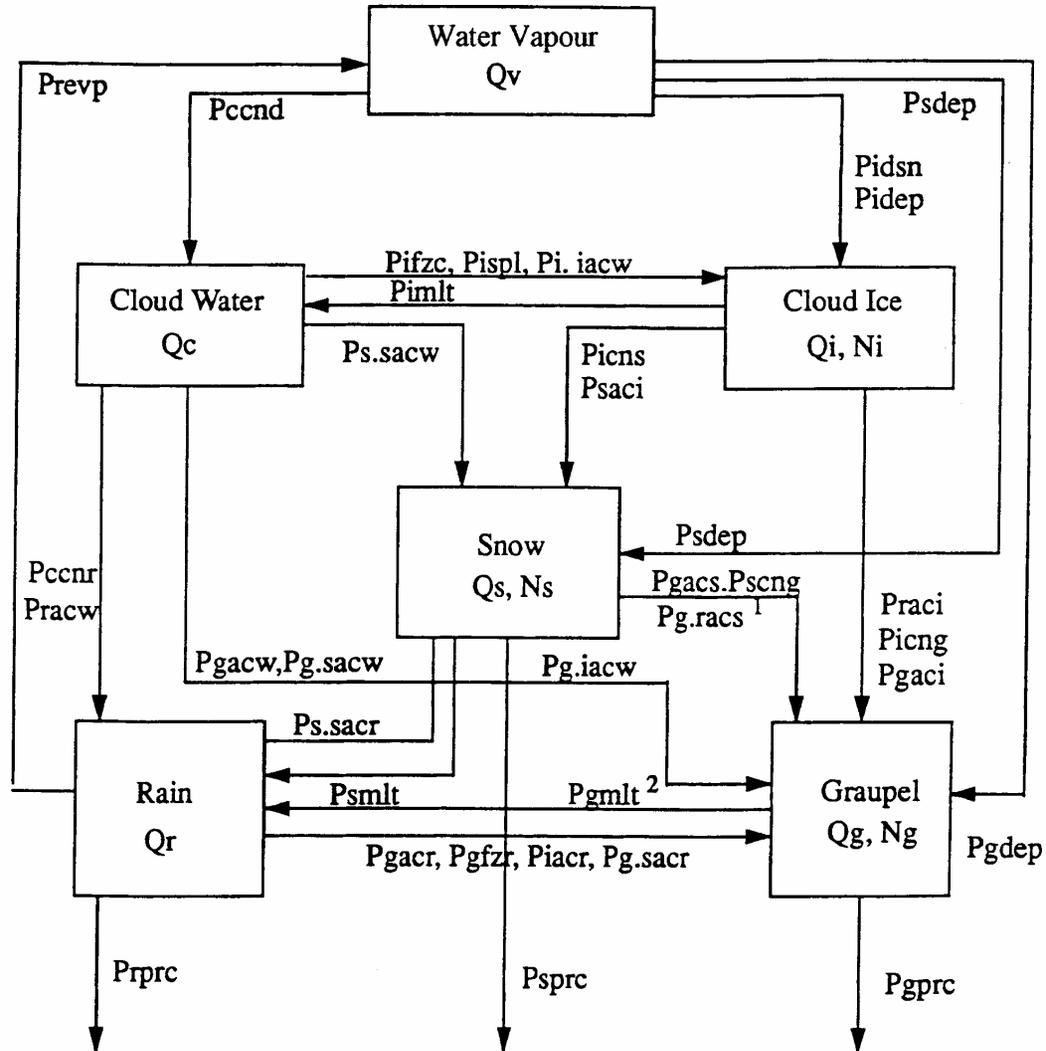
- **Increase resolution**
- **Enhance other physics schemes (radiation, PBL, LSM)**
- **Add ensemble members**
- **Improve data assimilation**

Why focus on clouds?

- For many models, the main source of precipitation is clouds

- Yet snow and ice are important in terms of distribution

from Reisner et al. (1998)



the snow:

CSs

nt in
d size

Three aspects of the representation of snow in bulk schemes:

1. **Size distribution**
2. **Shape and density assumptions (i.e., mass-diameter relationship)**
3. **Velocity-diameter relationship**

A case will be made for:

1. **Choosing a reasonable/relevant habit**
2. **Enforcing “habit consistency” throughout the scheme**
3. **Diagnosing (as in Meyers et al. 1997) or predicting habit variability**

1. Size distribution

$$\hat{N}_s(D) = N_{0s} \exp(-\lambda_s D)$$

Integrating the third moment over all sizes yields

$$\rho_{\text{air}} q_s = \frac{\pi N_{0s} \rho_{\text{snow}}}{\lambda_s^4} = f(N_{0s}, \lambda_s)$$

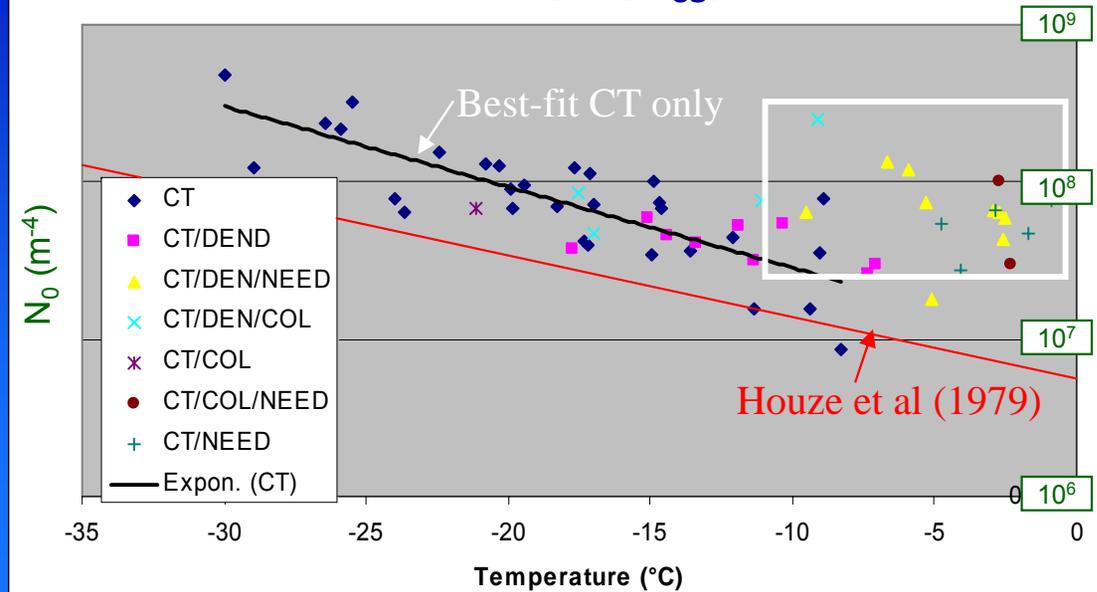
q_s is predicted;

specify N_{0s} , and solve for λ_s ;

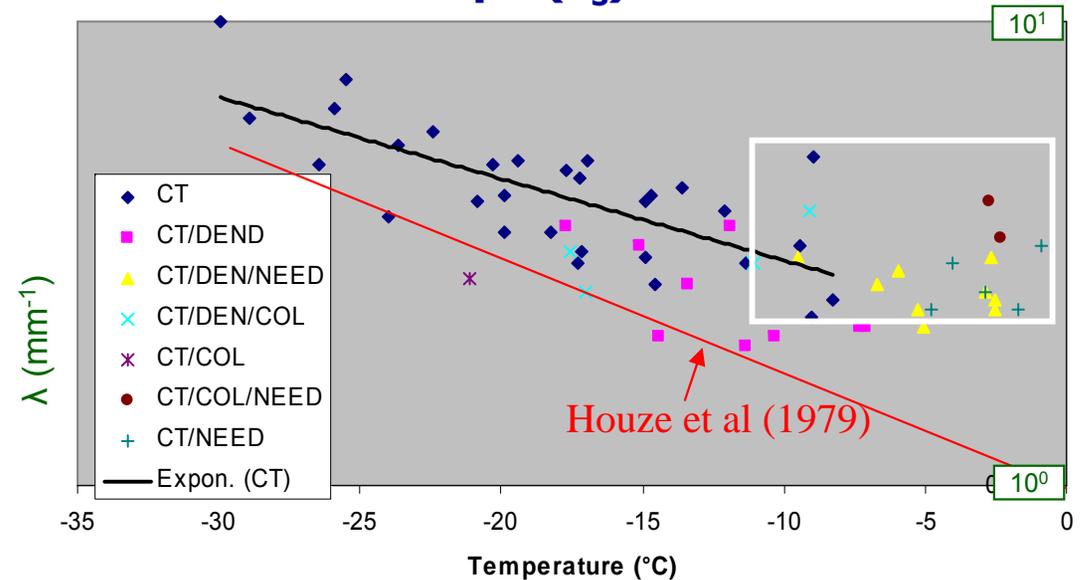
or alternatively, specify λ_s , and solve for N_{0s} .

Intercept and slope parameters measured by aircraft particle imagers throughout IMPROVE-1 and IMPROVE-2, as a function of temperature

Intercept (N_{0s}) vs. T



Slope (λ_s) vs. T



2. Snow particle shape and density

Many bulk schemes (R-T, Tao and Simpson 1993, Ferrier 1994) assume snow particles are spheres of constant density, implying a mass-diameter relationship of:

$$m(D) = \rho_{\text{snow}} (\pi / 6) D^3$$

However, observational and theoretical studies yield more general, habit-dependent power-law relationships of the form

$$m(D) = a_m D^{b_m} ,$$

which can also be implemented in bulk schemes (Cox 1988, Meyers et al. 1997).

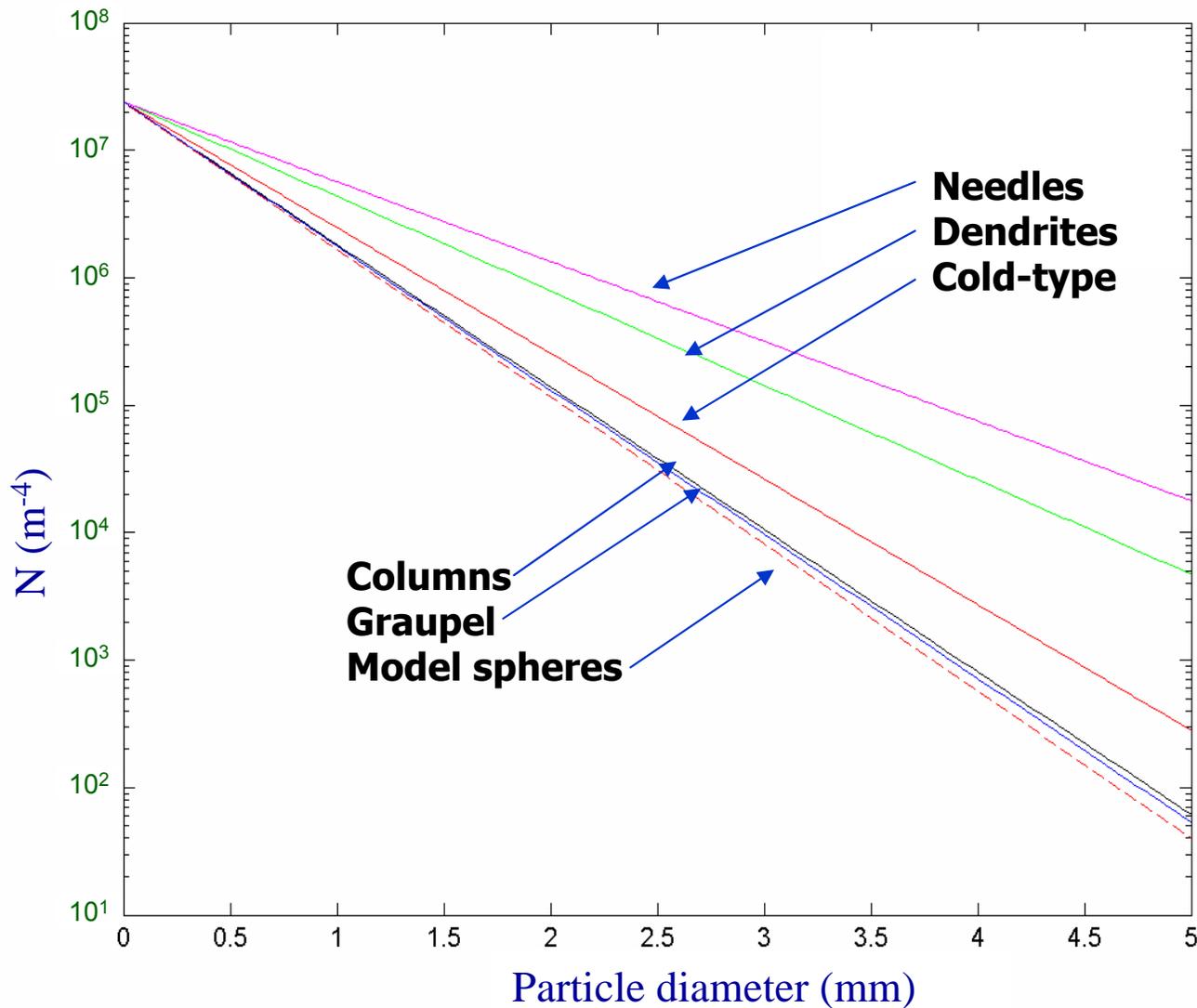
Constants in the m - D power law relationships for various crystal aggregate types (from Locatelli and Hobbs 1974), and for model snow spheres

Habit	a_m (mg mm^{-b_m)}	b_m
Dendrites	0.0141	2.19
Cold-type	0.0370	1.90
Needles	0.0092	2.01
Model spheres	0.0520	3.00

General expression for relationship between q_s , N_{0s} and λ_s :

$$\rho_{\text{air}} q_s = \frac{a_m N_{0s} \Gamma(b_m + 1)}{\lambda_s^{b_m + 1}}$$

Variation of spectral slope with particle habit (for fixed values of N_{0s} and q_s)



3. Snow fall speed

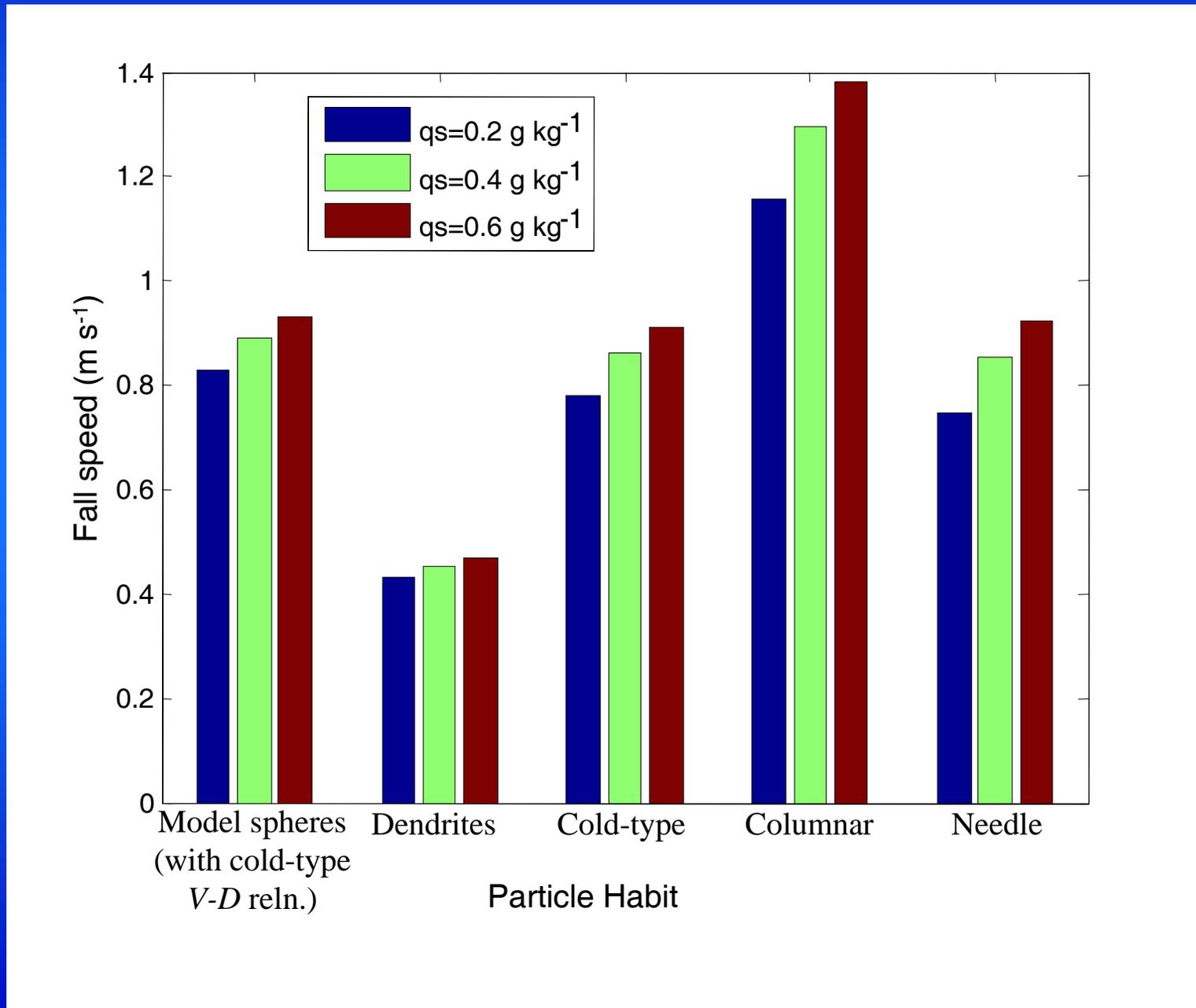
Observational and theoretical studies provide habit-dependent power-law relationship between the terminal fall speed of a particle and its diameter (a V - D relationship) of the form

$$V(D) = a_v D^{b_v} ,$$

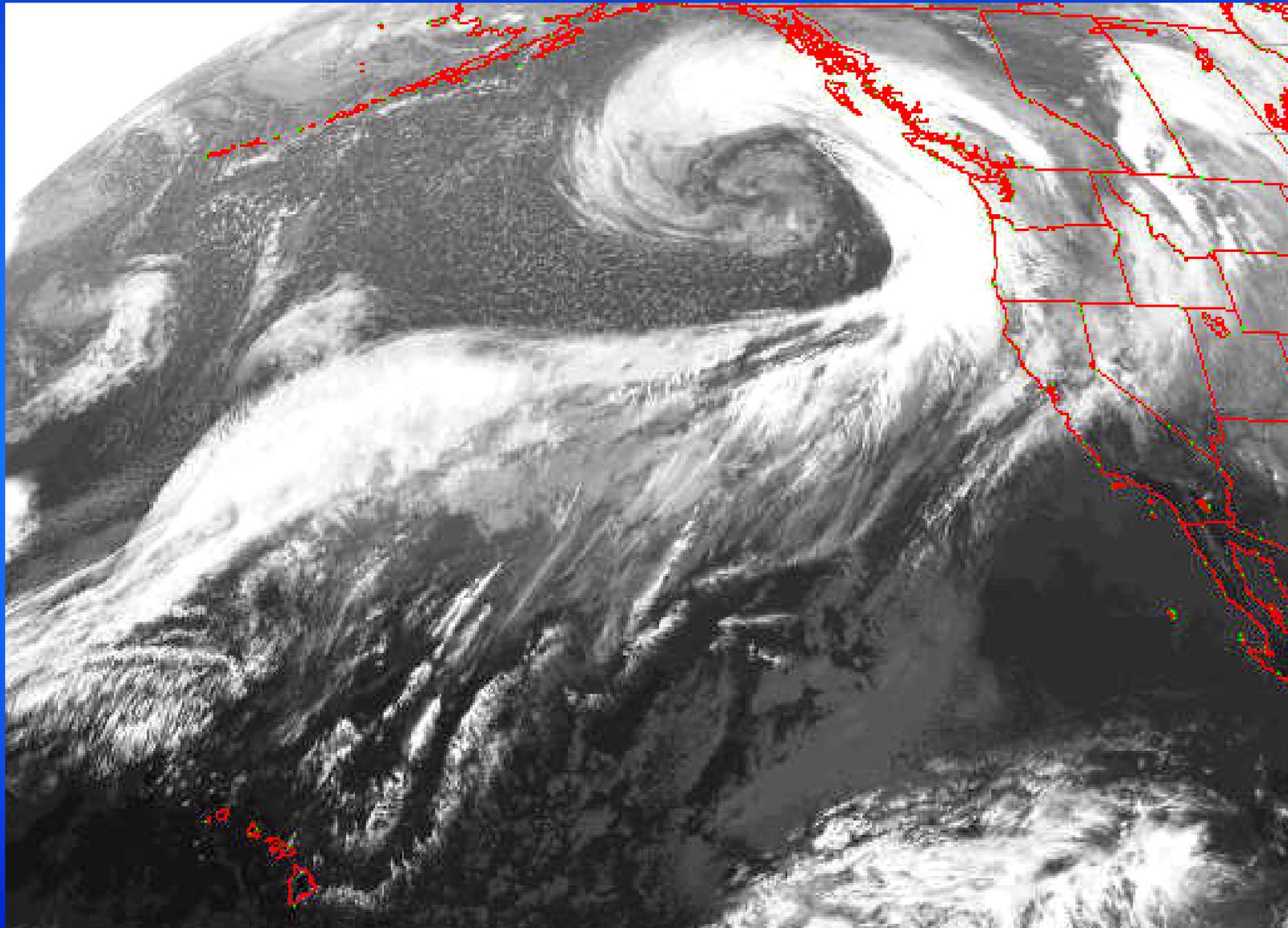
Combining with the exponential size distribution and the appropriate m - D relationship (for the same particle habit) and integrating, one obtains the *mass-weighted* terminal fall speed for snow particles of that habit:

$$\bar{V} = \frac{a_v \Gamma(b_m + b_v + 1)}{\lambda_s^{b_v} \Gamma(b_m + 1)}$$

Mass-weighted terminal fallspeed for various particle habits and snow mixing ratios



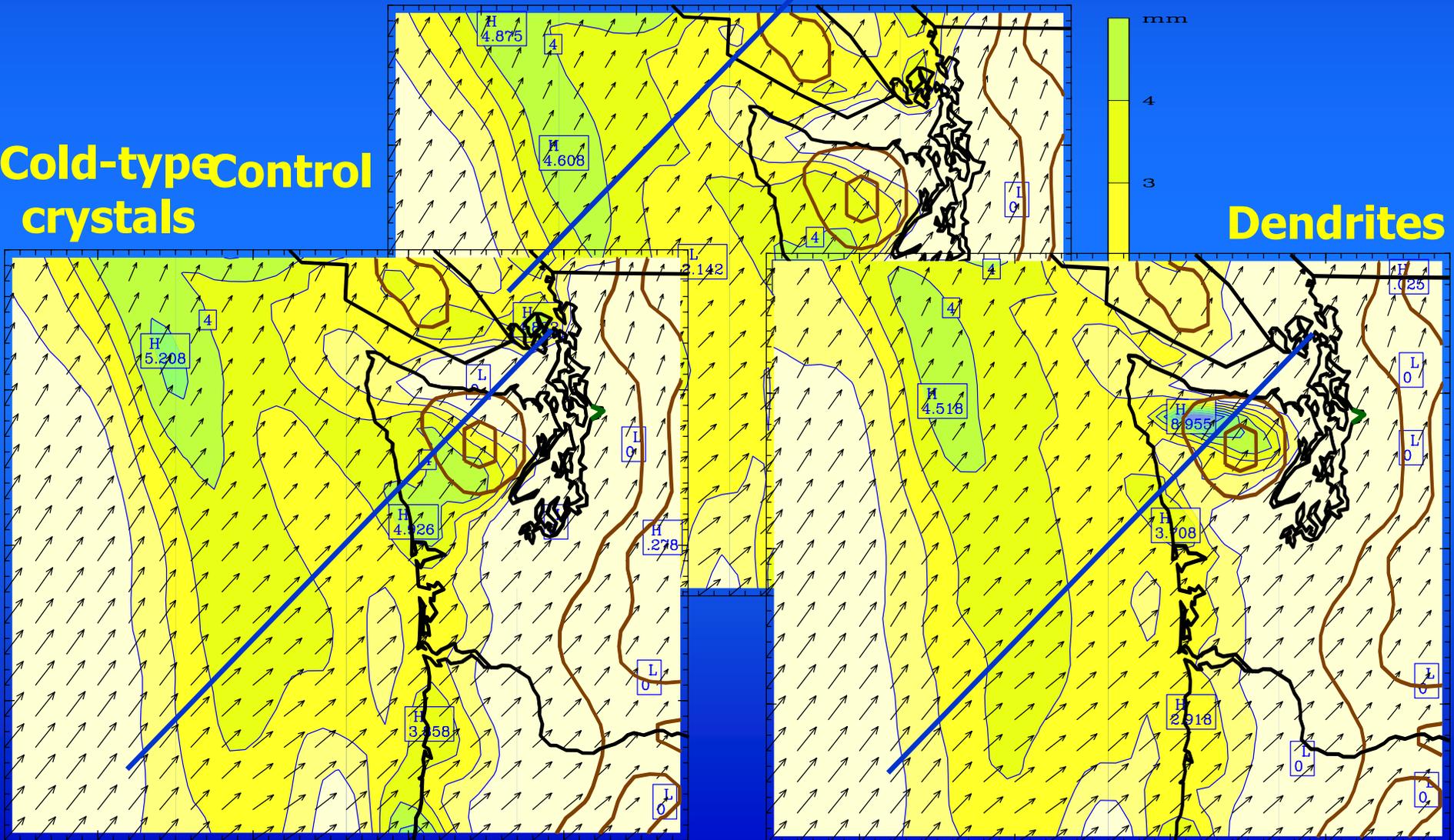
Example: Frontal rainband observed off the Washington coast during IMPROVE-1 (1-2 February 2001)



14-h MM5 forecast of 1-h precip, 12-km grid, R-T microphysics

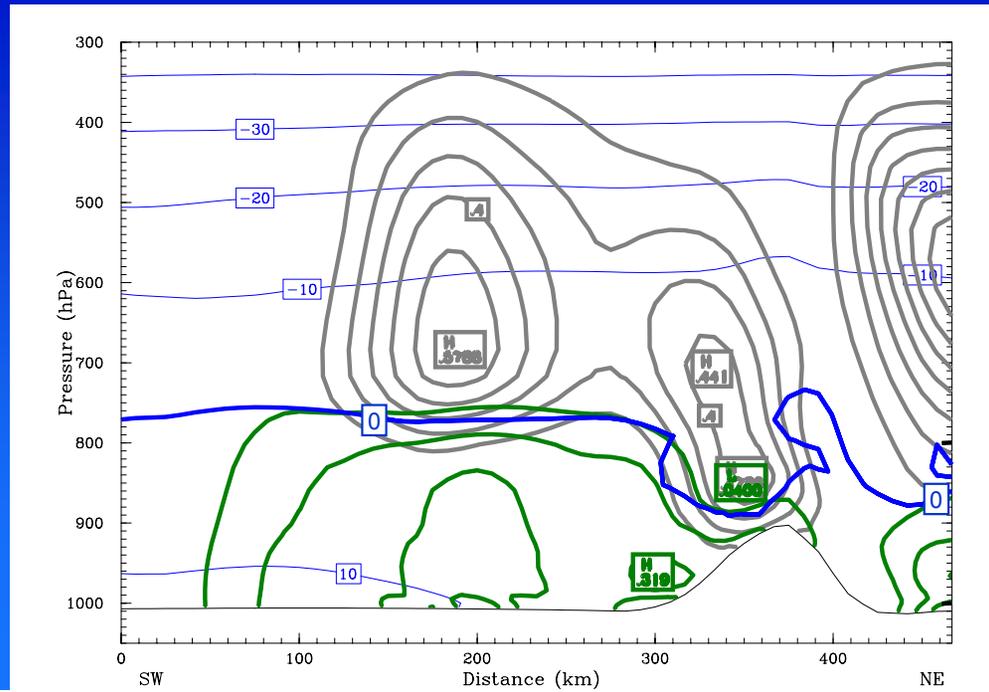
Cold-type
Control
crystals

Dendrites



Control

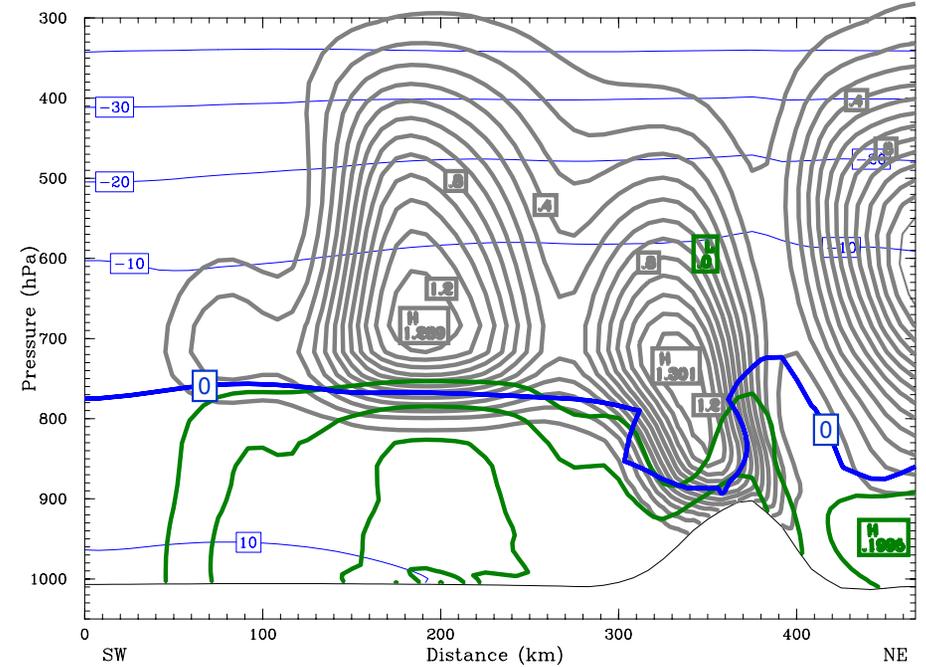
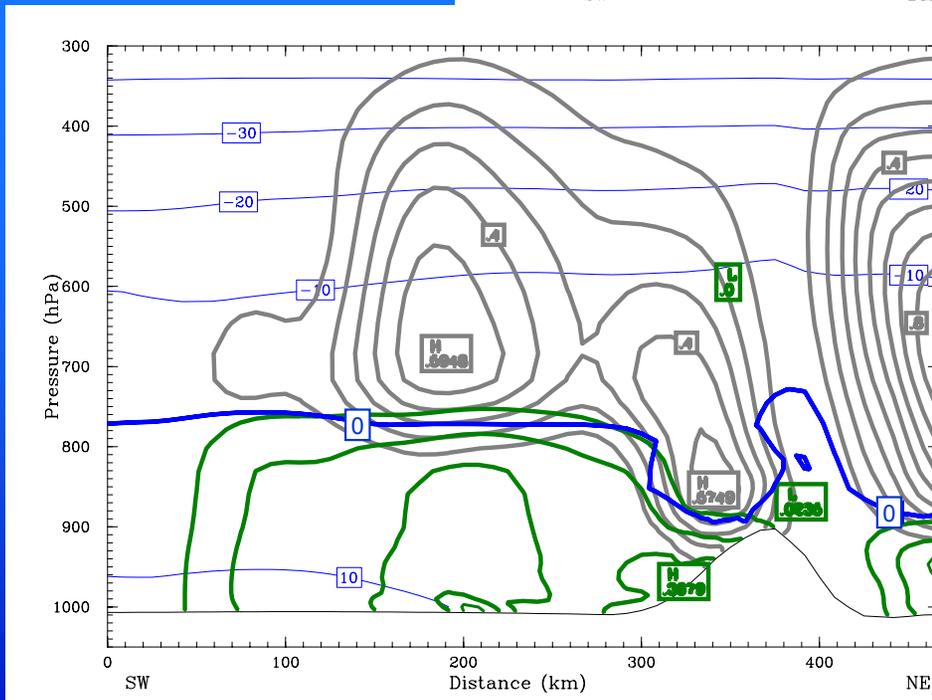
**Cold-type
crystals**



Contours:

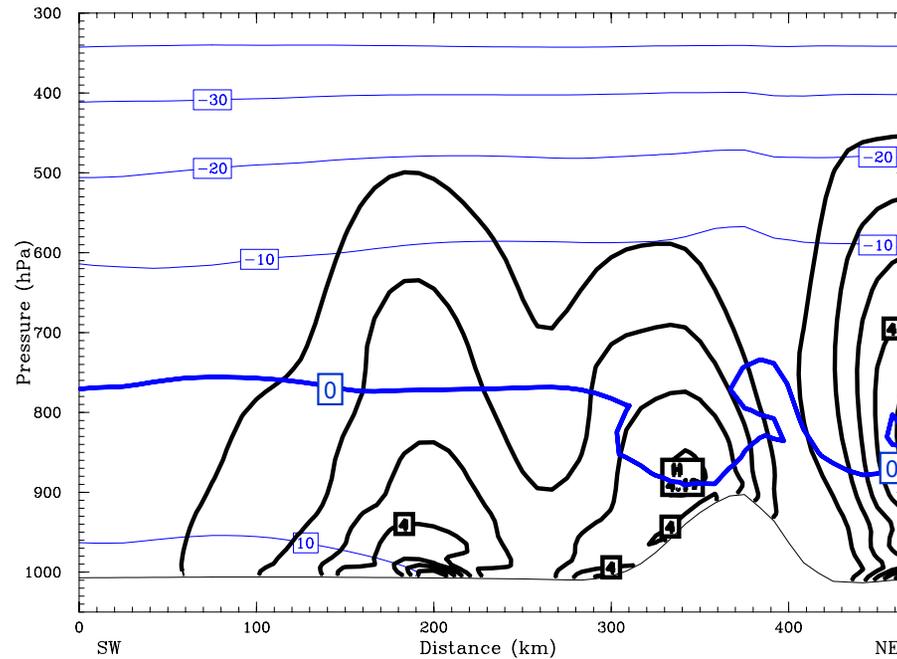
q_{snow} (g kg^{-1})
 q_{rain} (g kg^{-1})
 T ($^{\circ}\text{C}$)

Dendrites



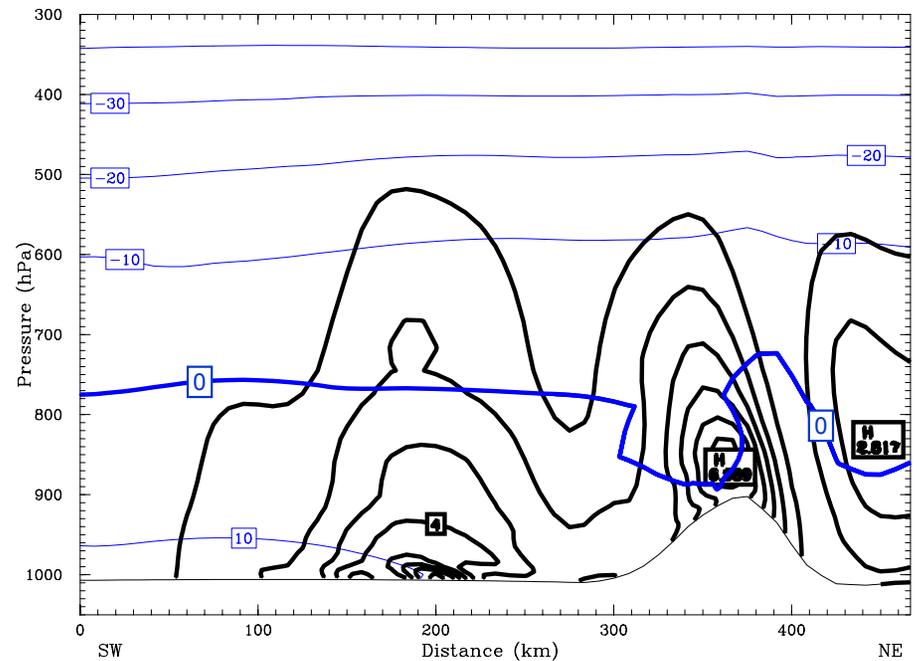
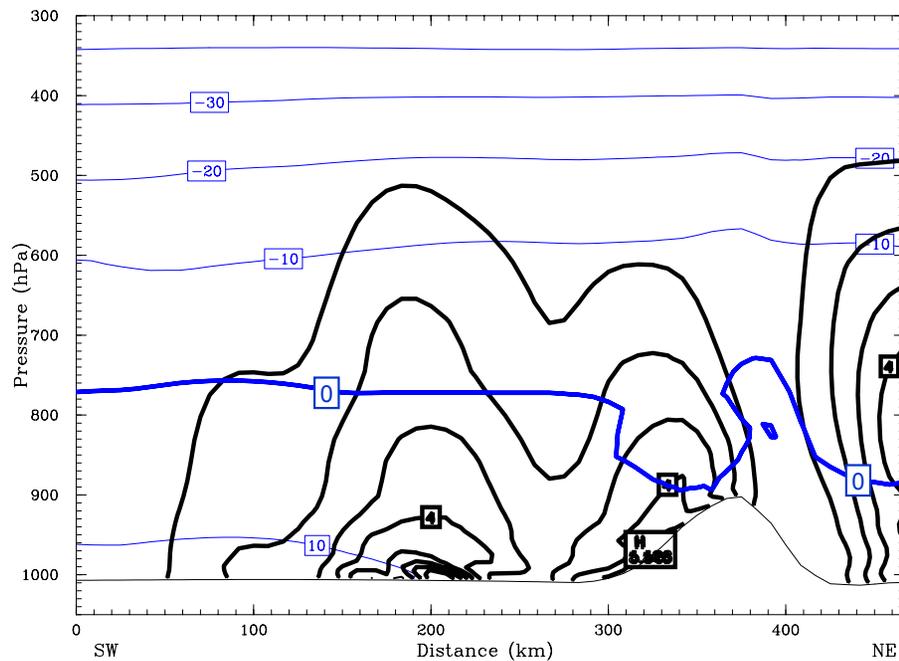
Control

**Cold-type
crystals**



Contours:
precip rate
(mm h⁻¹)
T (°C)

Dendrites

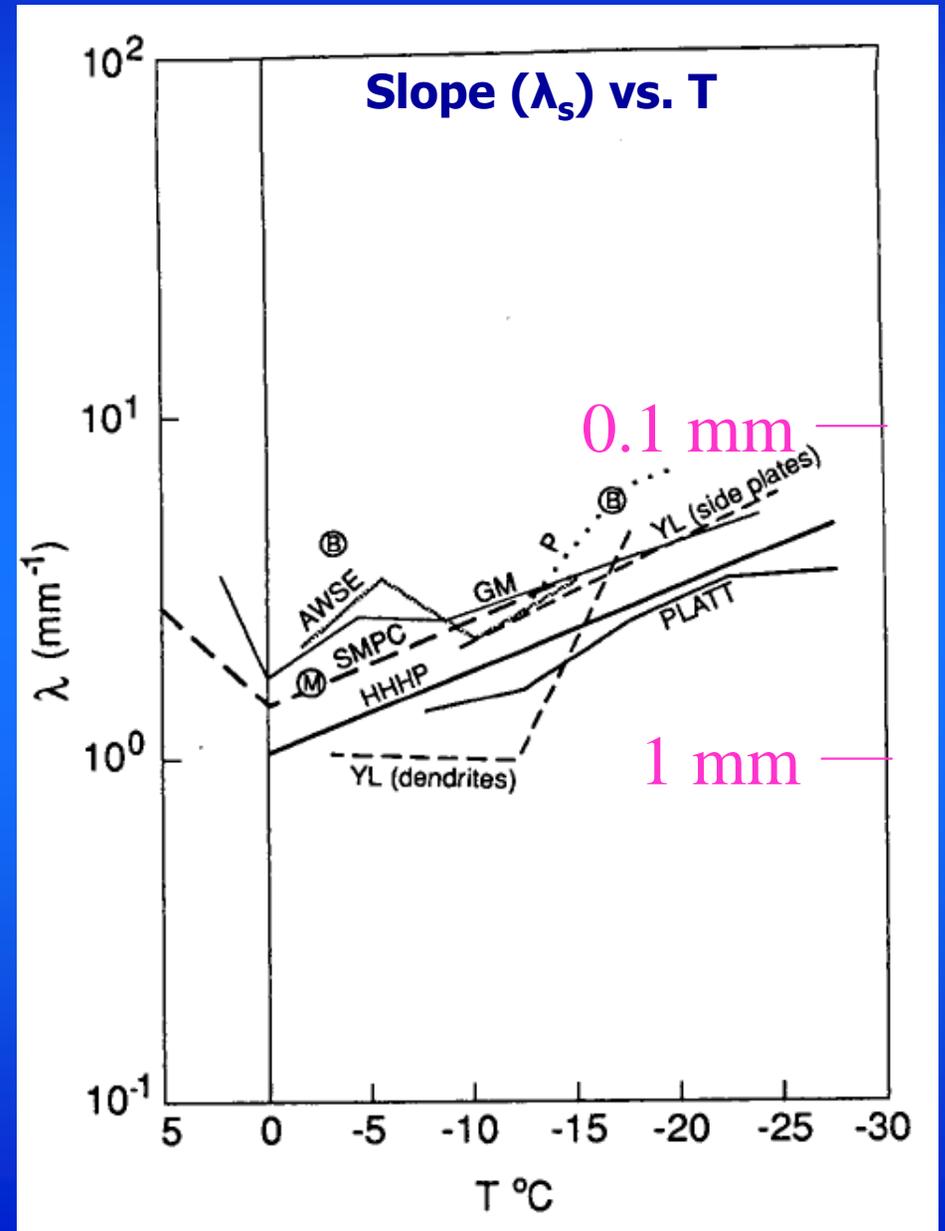
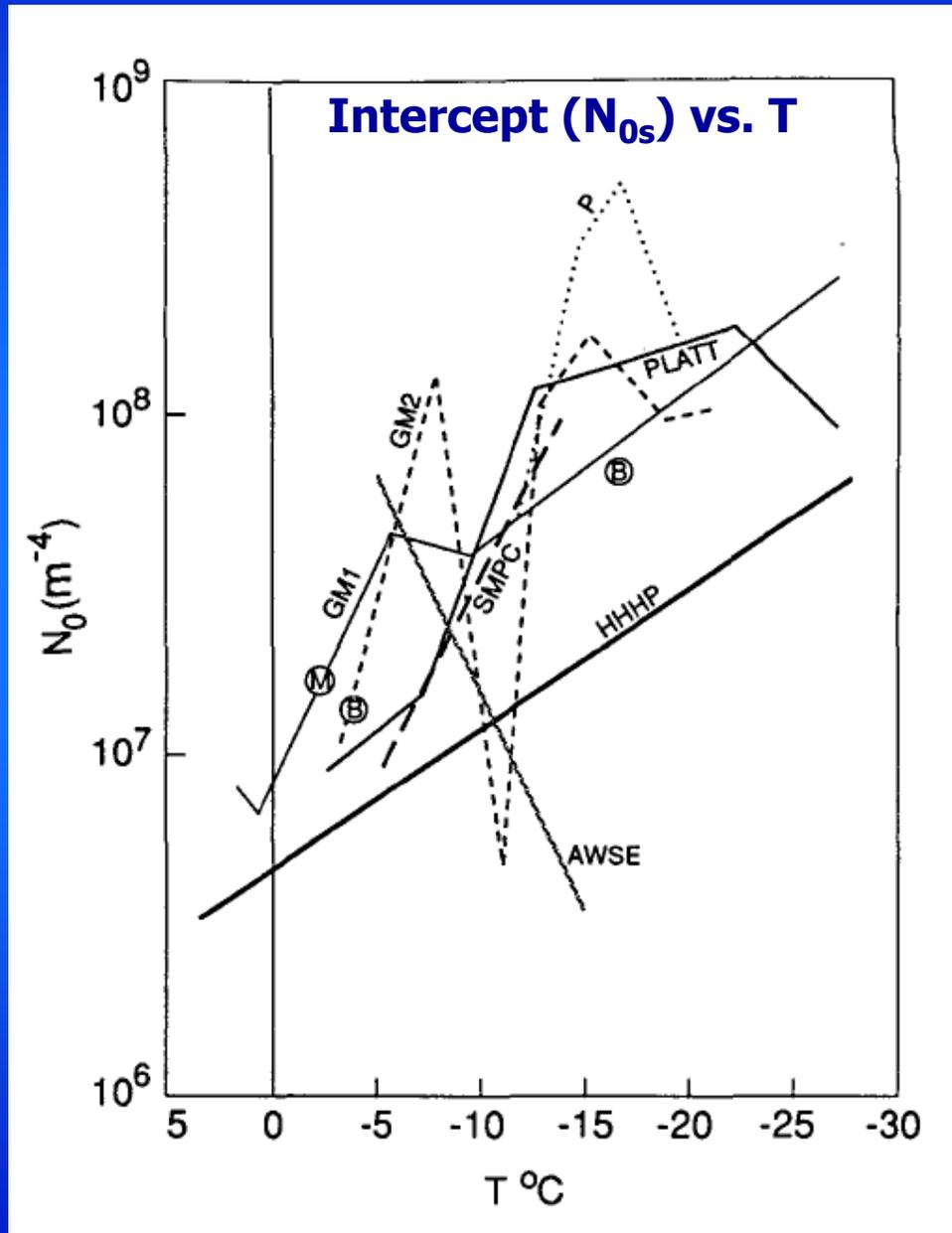


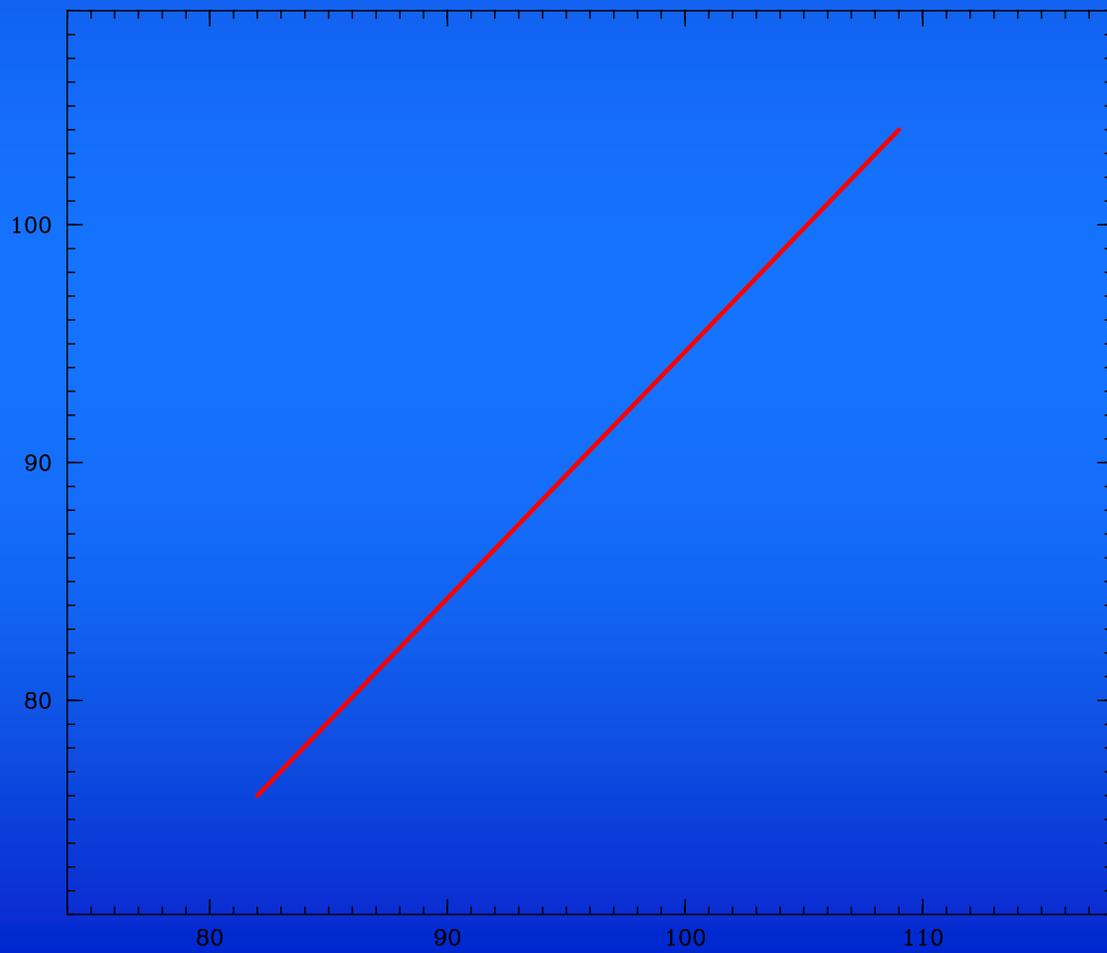
Recommendations / Future Work:

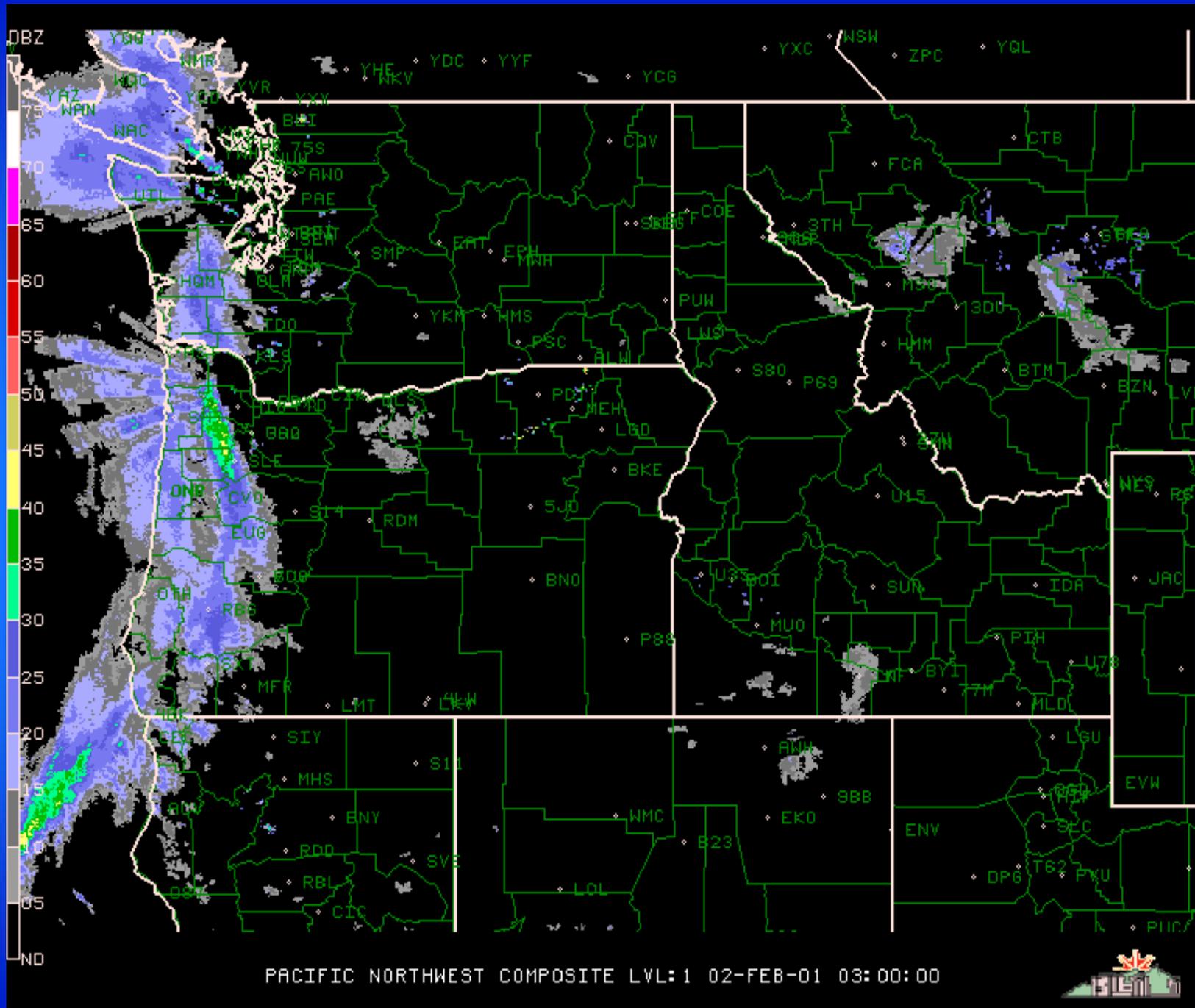
1. **Constant density spheres are not a good representation of most snow particle types.**
2. **Enforce “habit consistency” for the various habit-dependent aspects of the scheme (size distribution, *m-D* and *V-D* relationships, capacitance for depositional growth, etc.)**
3. **Examine ways to skew the distribution toward smaller particles when ice enhancement is active. Can this be done without going to a double-moment scheme?**
4. **Implement particle habit diagnosis (Meyers et al. 1997)**
5. **Develop habit *prognosis*, to test the effectiveness of the simpler habit *diagnosis*.**



Global ice particle spectra, Ryan (1996)







Papers submitted for a special "IMPROVE" issue of the *Journal of the Atmospheric Sciences:*

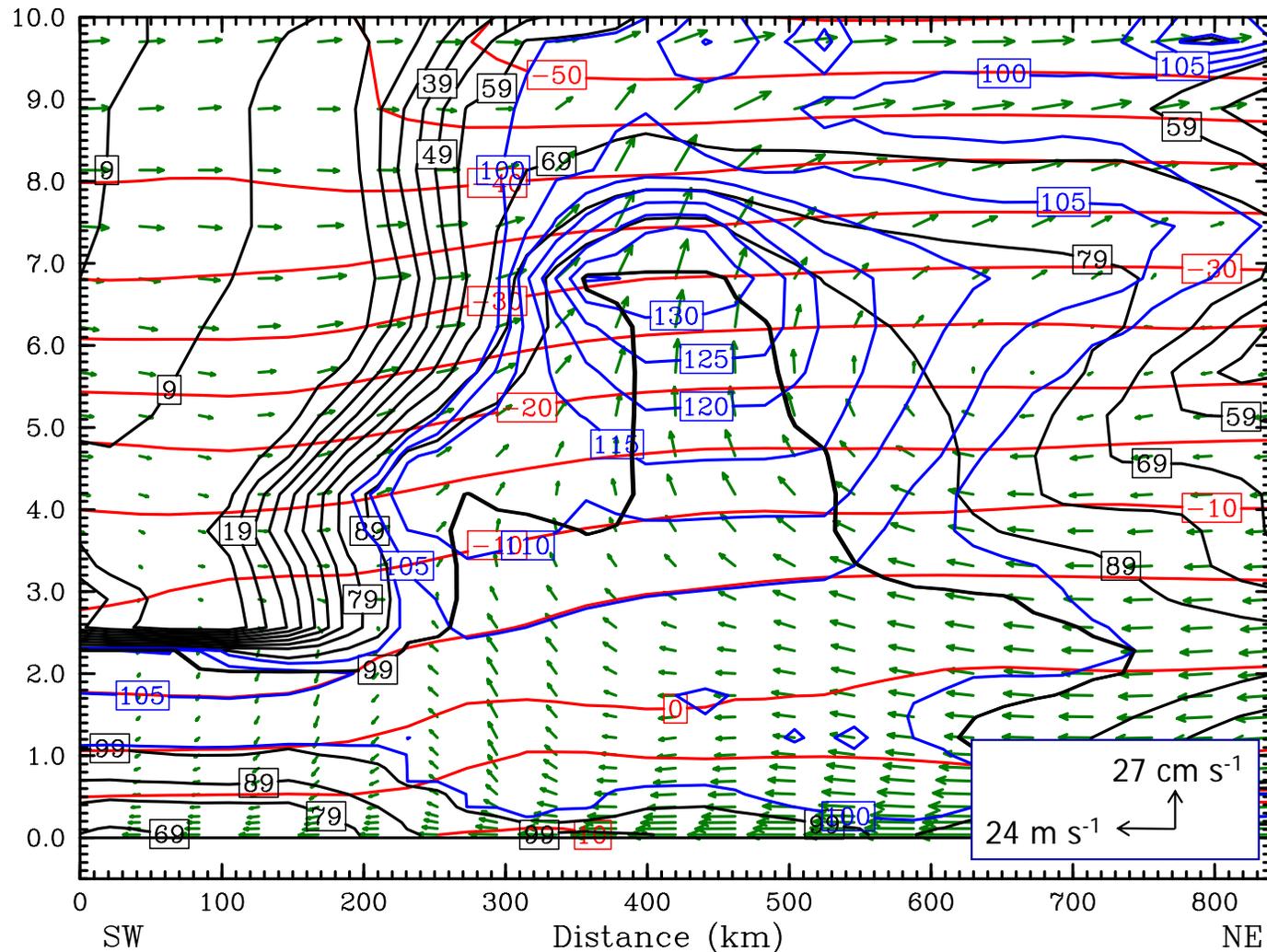
- Bond, N. A., B. F. Smull, M. T. Stoelinga, C. P. Woods, A. Haase, and J. D. Locatelli, "[The Evolution of a Cold Front over Quasi-2D Terrain: Coordinated Aircraft Observations of the 8-9 December 2001 Wide Cold Frontal Rainband during IMPROVE-2](#)"
- Colle, B. A., M. F. Garvert, J. B. Wolfe, and C. F. Mass, "[Microphysical Budgets and Sensitivity Studies for the 13-14 December 2001 IMPROVE-2 Event](#)"
- Evans, A. G., J. D. Locatelli, M. T. Stoelinga, and P. V. Hobbs, "[The IMPROVE-1 Storm of February 1-2, 2001. Part II: Cloud Structures and the Growth of Precipitation](#)"
- Garvert, M. F., B. A. Colle, and C. F. Mass, "[Synoptic and Mesoscale Evolution of the 13-14 December 2001 IMPROVE II Storm System and Comparison with a Mesoscale Model Simulation](#)"
- Garvert, M. F., C. P. Woods, B. A. Colle, C. F. Mass, P. V. Hobbs and J. B. Wolfe, "[Comparisons of MM5 Model Simulations of Clouds and Precipitation with Observations for the 13-14 December 2001 IMPROVE-2 Event](#)"
- Houze, R. A., and S. Medina, "[Turbulence as a Mechanism for Orographic Precipitation Enhancement](#)"
- Medina, S., B. F. Smull, and R. A. Houze, "[Airflow Patterns in Orographic Precipitation Events over the European Alps and the Oregon Cascades](#)"
- Ikeda, K, E. A. Brandes, and R. M. Rasmussen, "[Polarimetric Radar Observation of Multiple Freezing Levels](#)"
- Locatelli, J. D., M. T. Stoelinga, M. F. Garvert, and P. V. Hobbs, "[The IMPROVE-1 Storm of February 1-2, 2001. Part I: Development of a Forward-Tilted Cold Front and a Warm Occlusion](#)"
- Woods, C. P., M. T. Stoelinga, J. D. Locatelli, and P. V. Hobbs, "[Cloud Structures, Microphysical Processes and Synergistic Interaction between Frontal and Orographic Forcing of Precipitation during the December 13, 2001 IMPROVE-2 Event over the Oregon Cascades](#)"
- Yuter, S. E., D. Kingsmill, L. B. Nance, and M. Löffler-Mang, "[Observations of precipitation characteristics near and within the melting layer](#)"

Outline:

- Microphysical issues (as represented in the MM5's mixed phase scheme), from observations and modeling of IMPROVE case studies
- Hypotheses for important interactions between mesoscale processes and microphysics
- "Studies of opportunity": interesting features elucidated by the IMPROVE data set

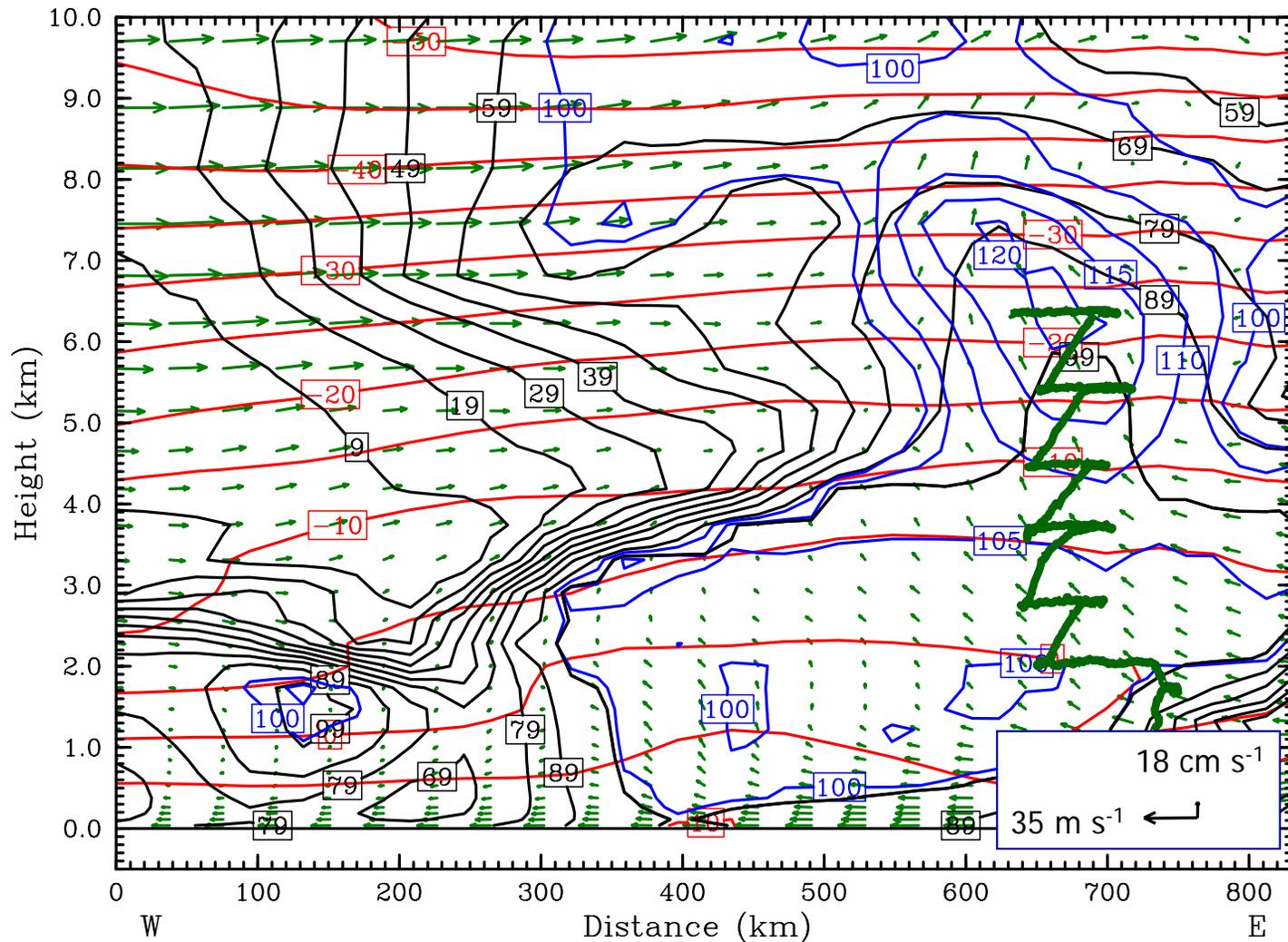
Evidence of excessive supersaturation with respect to ice in deep frontal clouds (Locatelli et al. 2004)

12 UTC 1 Feb 2001 (12-h fcst), 36-km simulation



Evidence of excessive supersaturation with respect to ice in deep frontal clouds

00 UTC 2 Feb 2001 (24-h fcst), 36-km simulation



Summary of observations from Convair-580 flight stack:

In regions where model indicated high ice supersaturation:

- measured RH was generally near ice saturation
- Negligible liquid water was detected
- Ice crystal habits were generally found to be sub-water-saturated types, or inconclusive (notably, no dendrites in the dendritic growth zone)

One possible problem with the Rutledge and Hobbs (1983) formulation for growth of snow by deposition (PSDEP):

Although the RH83 equation uses capacitance for a 2-D plate, it assumes the population is comprised of spherical particles.

For a given supersaturation, the mass of a growing particle as a function of time behaves as follows:

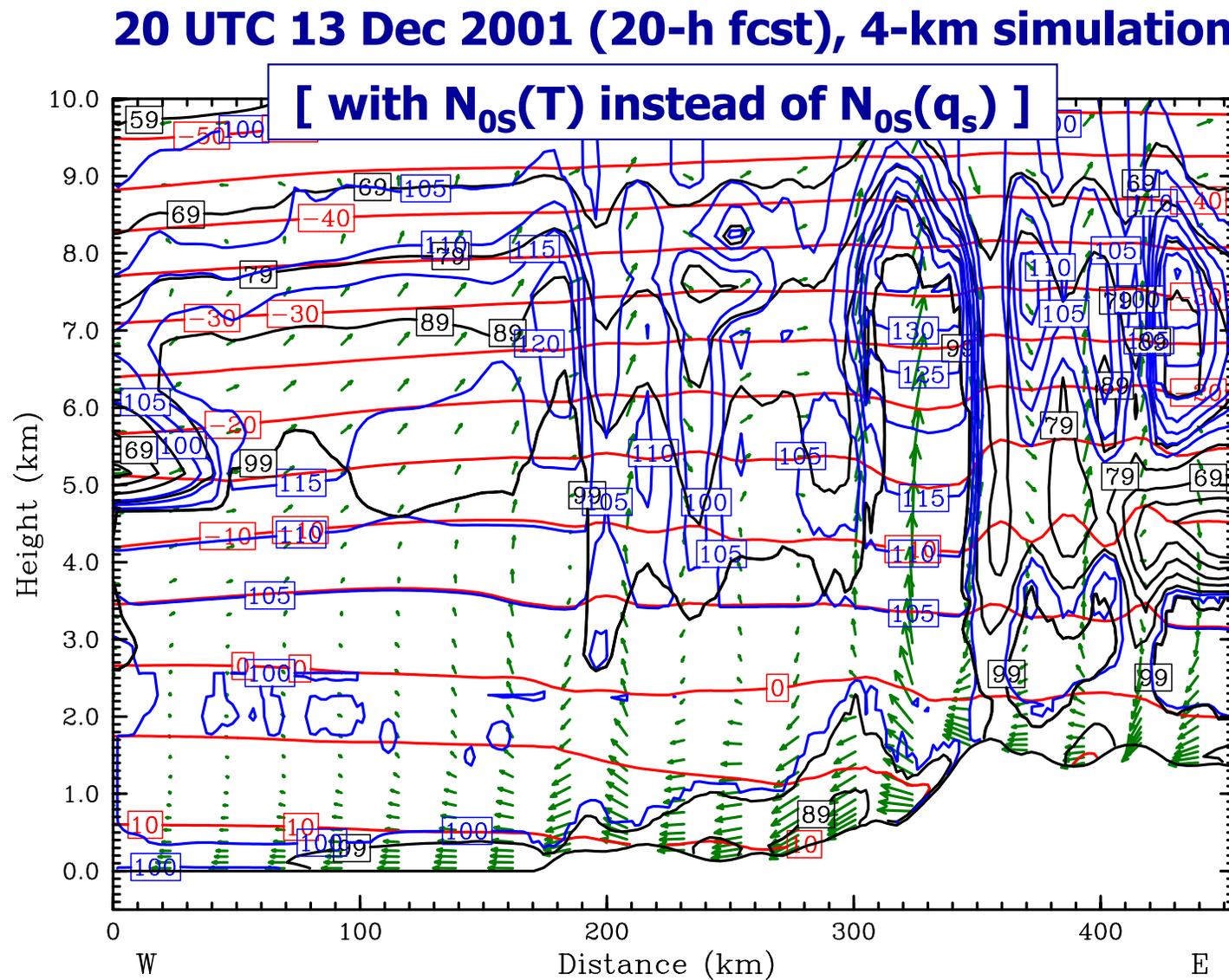
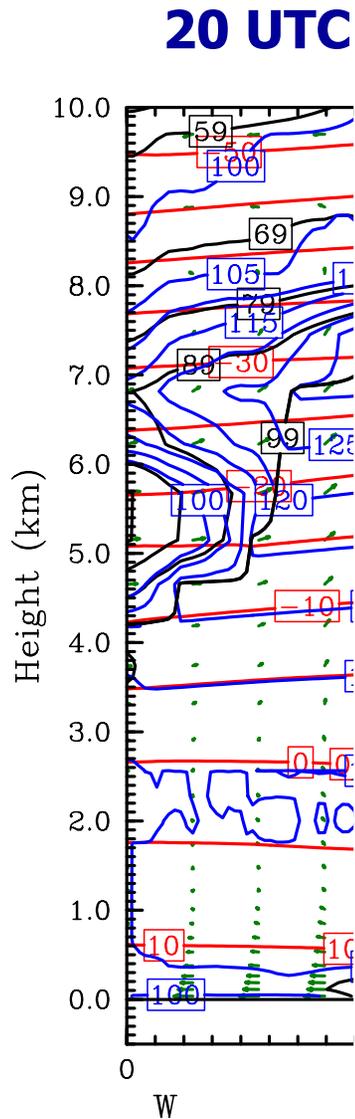
- 3-D growth (e.g., spherical particle): $m(t) \propto \frac{t^{3/2}}{\rho_s^{1/2}}$

- 2-D growth (e.g., plate, dendrite): $m(t) \propto \frac{t^2}{\rho_s}$

- 1-D growth (e.g., needle): $m(t) \propto \exp\left(\frac{\text{const} \times t}{\rho_s}\right)^{1/2}$

(Young 1993)

Growth of snow by deposition is also sensitive to the assumed snow particle size distribution parameters (Garvert et al. 2004)



Neither formulation for N_{0S} agrees with the “upside-down” behavior of N_{0S} that was observed in Convair-580 flight tracks during the 13-14 Dec 2001 case. (model spectra from 1.3-km MM5 simulation)

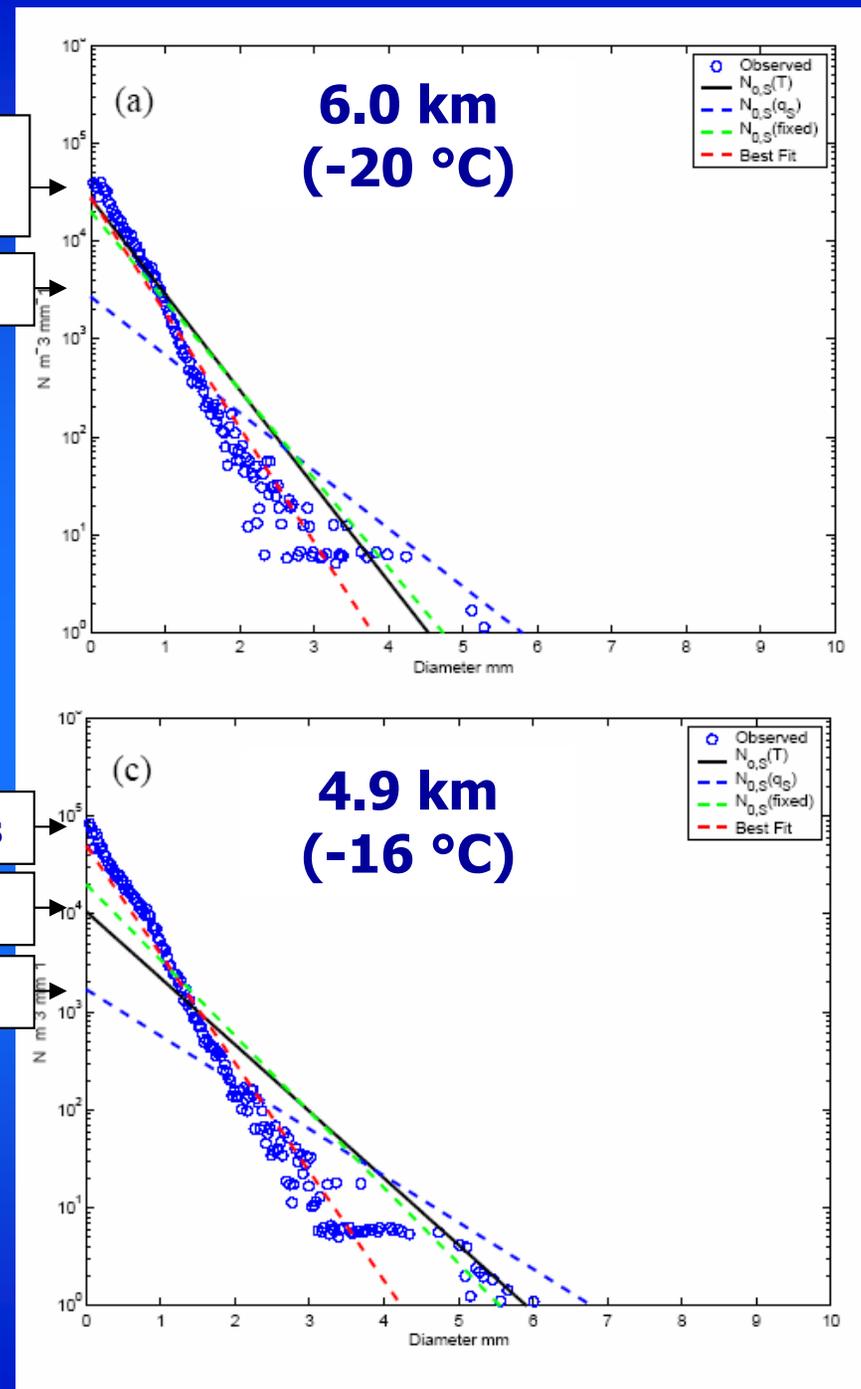
$N_{0S}(T),$
 $N_{0S} \text{ obs}$

$N_{0S}(q_s)$

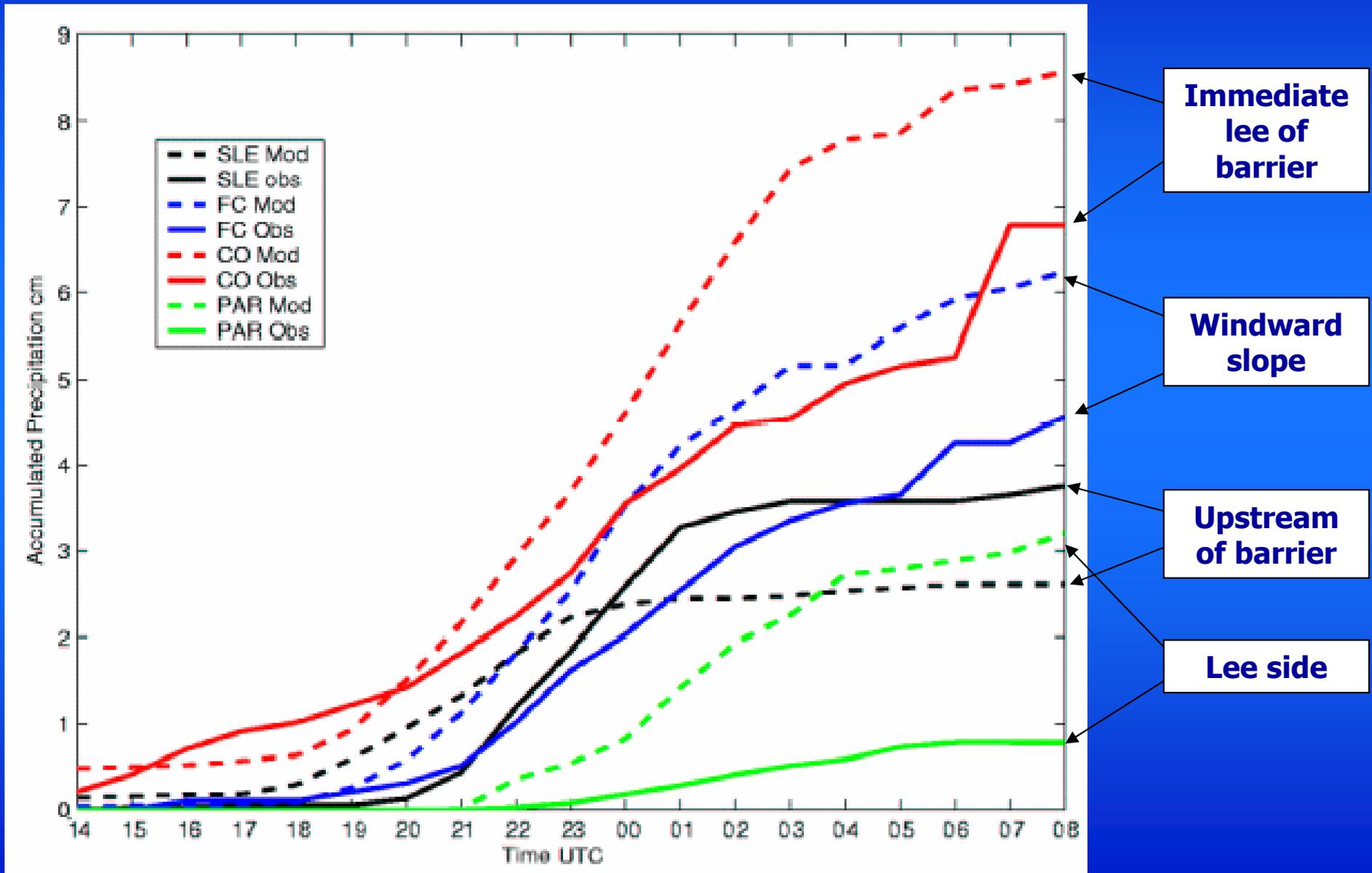
$N_{0S} \text{ obs}$

$N_{0S}(T)$

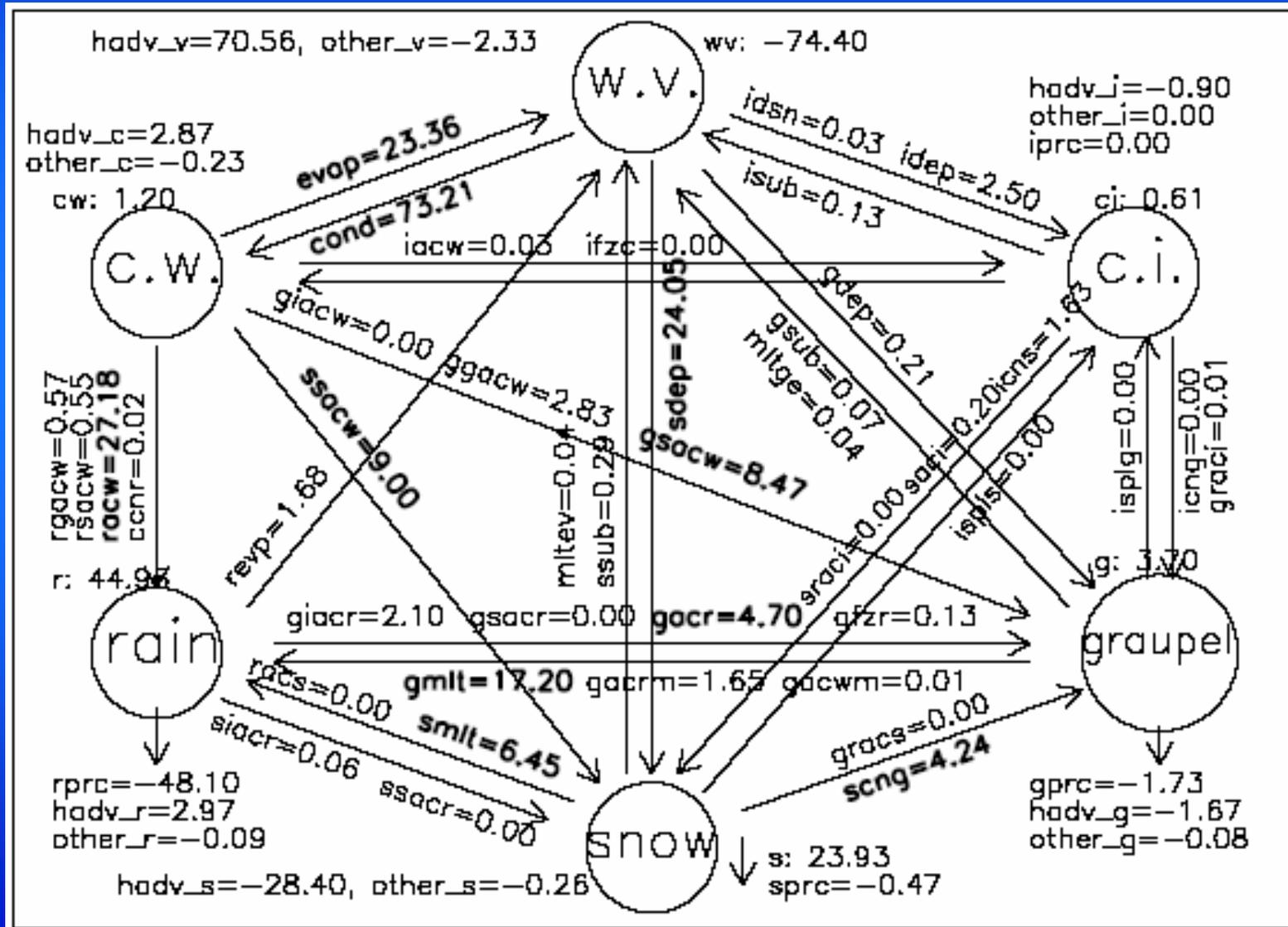
$N_{0S}(q_s)$



Storm total precipitation verification from the 1.3-km MM5 simulation (Garvert et al. 2004)



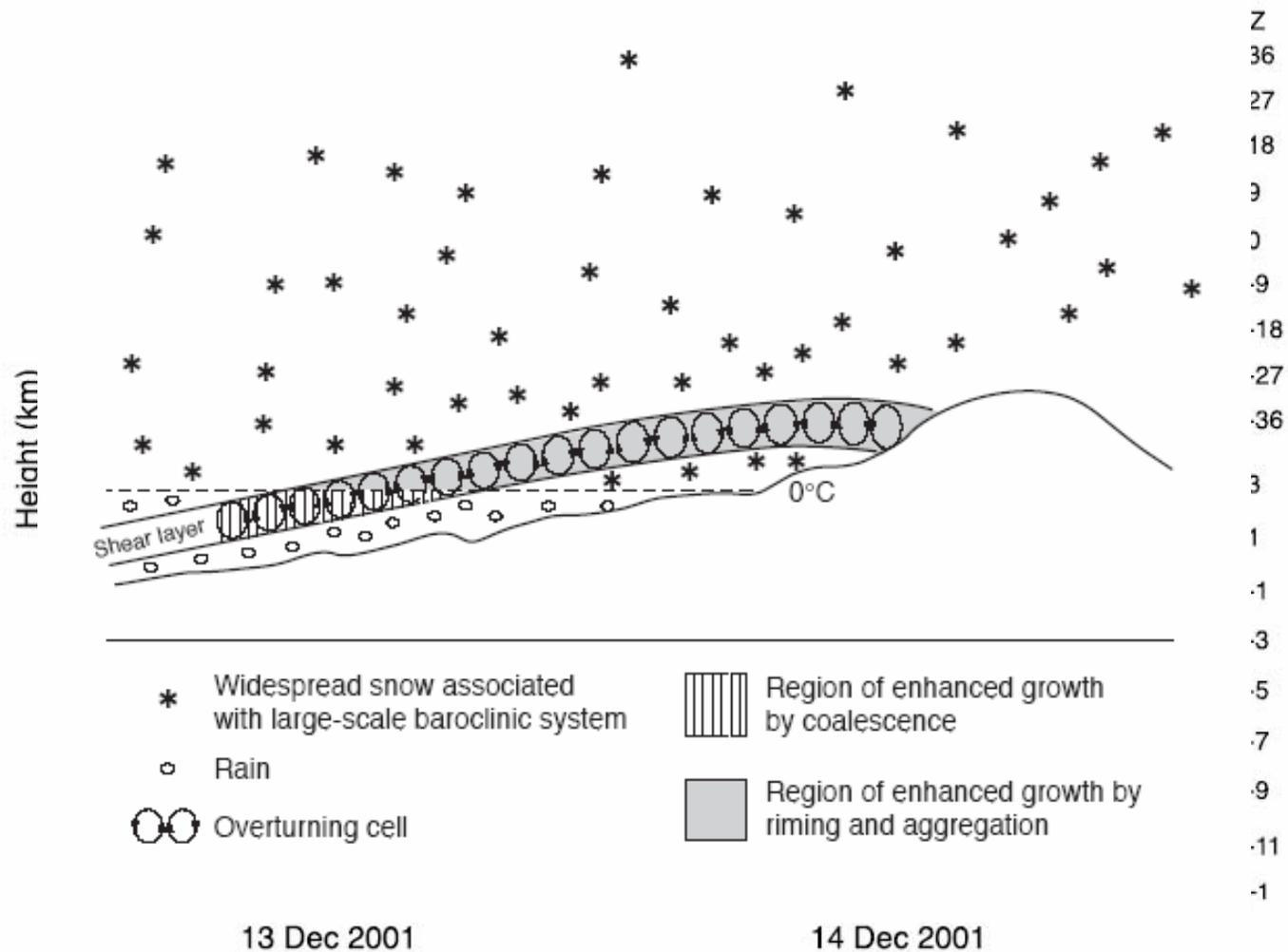
Water mass transfer budget of bulk microphysical scheme for simulation of 13-14 Dec 2001 case (Colle et al. 2004)



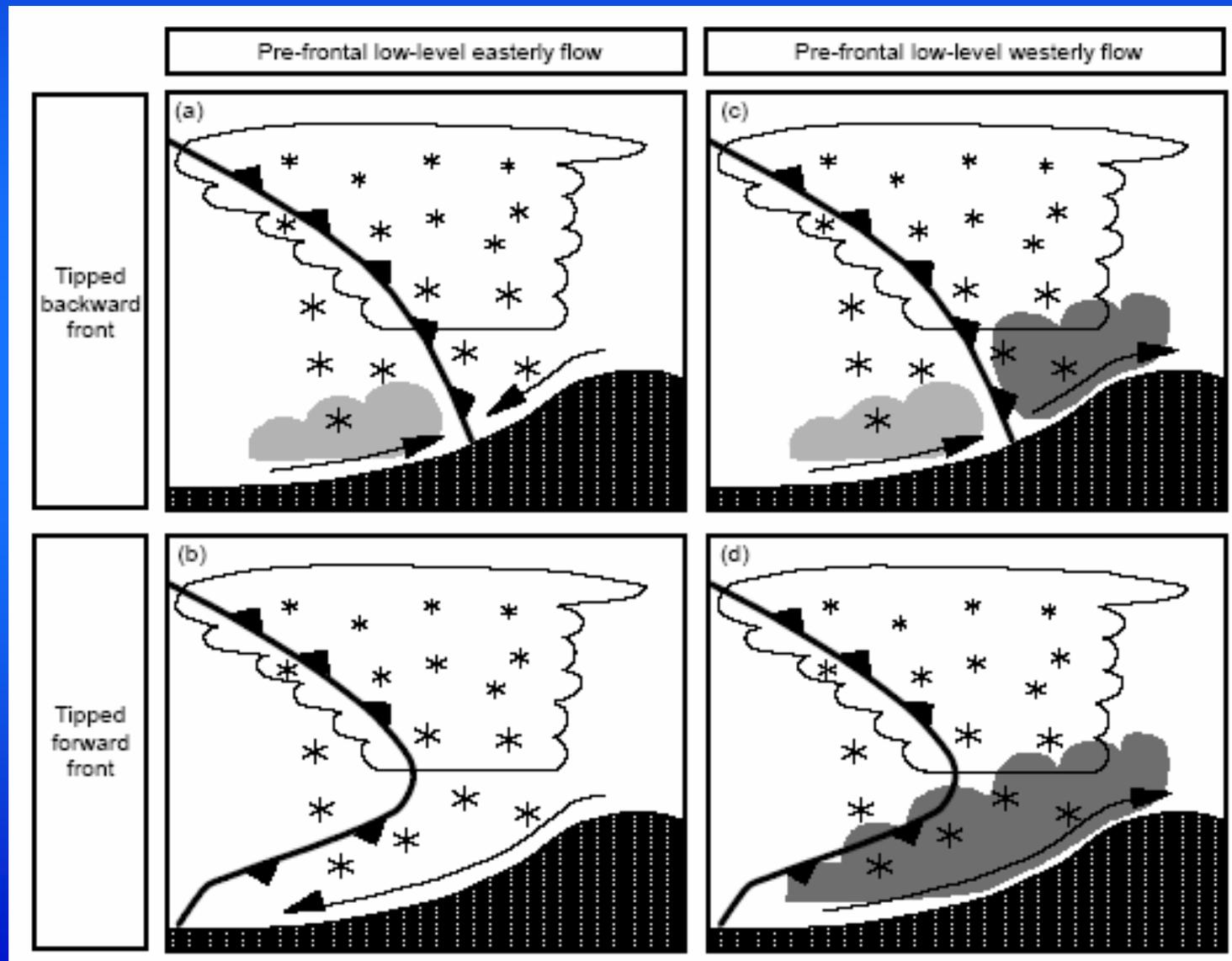
Turbulence as a Mechanism for Orographic Precipitation Enhancement (Houze and Medina 2004)

Hypotheses for important interactions between

Vertically pointing S-band (precipitation) radar in the upslope zone



Importance of frontal structure and prefrontal flow for maximizing interaction between frontal and orographic precipitation (Woods et al. 2004)



Double brightband within warm-frontal inversion zone (Ikeda et al. 2004)

Unique frontal precipitation phenomena elucidated by
the ground-based dual-polarized Doppler (S-Pol) radar

