Enhancing WRF-Solar to provide solar irradiance probabilistic forecasts

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Outline

1. Overview of WRF-Solar probabilistic forecasts

2. TL/AD Sensitivity test for WRF-Solar modules

- Methodology
- Application to FARMS
- Application to Thompson microphysics scheme
- 3. Summary

WRF-Solar probabilistic forecasts

Limitations of deterministic forecasts

1. Deterministic forecast can potentially result in incorrectly predicting clear sky (day 5)

2. Deterministic forecast does not inform us about how confident we are on the predictions

- What do we need
- 1. Ensemble based probabilistic forecast
- 2. Careful selection of relevant variables to perturb the ensembles
- 3. Calibration to provide unbiased forecasts with accurate ensemble spread



The ensemble perturbs temperature and winds which is not the optimal for solar irradiance forecasting

Approach



1. Developing stand alone version for five independent physics schemes

- FARMS radiation scheme
- NOAH LSM
- Thompson microphysics scheme
- MYNN boundary layer scheme
- Deng shallow cumulus scheme
- 2. Developing TL/AD codes for five independent physics schemes by TAF
- 3. Verify standalone TL/AD derivatives against finite difference approximations
- 4. Adjoint sensitivity test

"Identify variables that significantly influence the formation and dissipation of clouds and solar radiation"

FARMS (Fast-All-sky Radiation Model for Solar applications)

- New option for approximating solar radiation at the land surface with minimal loss of accuracy at high speed
- Using simplified clear-sky RT model (BIRD) and parameterized LUTs of cloud transmittances (*T*) and reflectances (*R*) from RRTM by functions of θ and cloud microphysical and optical properties
- Xie et al. (2016)



Concept of TL/AD model

- Tangent linear model, $\mathbf{M} = dY/dX$
- Adjoint model, \mathbf{M}^{T}
- Tangent linearity test

[Xiao et al., 2008 and Zhang et al., 2013]

$$\Phi(\lambda) = \frac{\|f(\mathbf{x} + \lambda) - f(\mathbf{x})\|}{\lambda \|\mathbf{M}_f(\mathbf{x})\|}, \lim_{\lambda \to 0} \Phi(\lambda) = 1$$

Adjointness test

[Errico, 2007]

$$\langle \mathbf{M}\mathbf{x}, \mathbf{y} \rangle = \langle \mathbf{x}, \mathbf{M}^{\mathrm{T}}\mathbf{y} \rangle$$
$$\langle \mathbf{M}d\mathbf{X}, d\mathbf{Y} \rangle = \langle d\mathbf{X}, \mathbf{M}^{\mathrm{T}}d\mathbf{Y} \rangle$$
$$\langle d\mathbf{Y}, d\mathbf{Y} \rangle = \langle d\mathbf{X}, \mathbf{M}^{\mathrm{T}}\mathbf{M}d\mathbf{X} \rangle$$
TLM output

TL/AD test results for FARMS

$$\Phi(\lambda) = \frac{\|f(\mathbf{x} + \lambda) - f(\mathbf{x})\|}{\lambda \|\mathbf{M}_f(\mathbf{x})\|}, \lim_{\lambda \to 0} \Phi(\lambda) = 1$$

,							
perturbation	p_pa	albdo	g	z	aod	alpha	w
0.100000000000000000	0.99999982364046653	1.01886477327702811	0.99170497407140060	1.00423356227456375	0.84627544382499353	1.01297889692556379	0.99833807655010926
0.010000000000000000	0.99999998236404184	1.00181589165434327	0.99916728630459746	1.00032648902005076	0.97815978028651190	1.00128749954634479	0.99983346520669115
0.00100000000000000	0.99999999823640414	1.00018093007685141	0.99991669640763297	1.00003156762032675	0.99770300975802800	1.00012864664708110	0.99998334308727627
0.00010000000000000	0.9999999982364041	1.00001808646025850	0.99999166931842286	1.00000314582246406	0.99976907579449122	1.00001286363222186	0.99999833427438476
0.00001000000000000	0.9999999998236404	1.00000180858059473	0.99999916692861877	1.00000031447272233	0.99997689522205787	1.00000128635289504	0.99999983342709504
0.0000100000000000	0.99999999999823640	1.00000018085740521	0.99999991669282964	1.00000003144617686	0.99999768939852632	1.00000012863518336	0.99999998334270607
0.0000010000000000	0.99999999999982364	1.00000001808573398	0.99999999166928264	1.0000000314460673	0.99999976893861689	1.00000001286351440	0.99999999833427057
0.0000001000000000	0.99999999999998236	1.00000000180857333	0.99999999916692826	1.0000000031446056	0.99999997689385049	1.0000000128634852	0.9999999983342706
0.000000010000000	0.999999999999999824	1.0000000018085733	0.99999999991669283	1.0000000003144606	0.9999999768938610	1.0000000012863195	0.99999999998334271
0.0000000010000000	0.9999999999999999982	1.0000000001808573	0.99999999999166928	1.0000000000314461	0.9999999976893978	1.0000000001286029	0.99999999999833427
0.0000000001000000	1.000000000000000000	1.0000000000180857	0.99999999999916693	1.0000000000031446	0.9999999997689515	1.0000000000128312	0.99999999999983343
0.0000000000100000	1.000000000000000026	1.0000000000018086	0.999999999999991669	1.0000000000003145	0.99999999999769068	1.00000000000012541	0.999999999999998334
							r
perturbation	tau_qv	tau_qi	tau_qs	re_qcloud	re_qice	re_qsnow	all
perturbation 0.10000000000000000	tau_qv 0.99976211964662838	tau_qi 1.01121693177192682	tau_qs 0.99704136860527521	re_qcloud 0.00054592688511941	re_qice 0.00041763418180853	re_qsnow 0.00000342324010777	all 0.00324914467627453
perturbation 0.10000000000000000 0.0100000000000000	tau_qv 0.99976211964662838 0.99999250625671401	tau_qi 1.01121693177192682 1.00117866173472181	tau_qs 0.99704136860527521 0.99970339809213327	re_qcloud 0.00054592688511941 0.00545926885119413	re_qice 0.00041763418180853 0.00417634181808530	re_qsnow 0.00000342324010777 0.00003423240107771	all 0.00324914467627453 0.00345786558440380
perturbation 0.1000000000000000 0.01000000000000000	tau_qv 0.99976211964662838 0.99999258625671401 0.99999941841740992	tau_qi 1.01121693177192682 1.00117866173472181 1.00011845260513306	tau_qs 0.99704136860527521 0.99970339889213327 0.99997033240185988	re_qcloud 0.00054592688511941 0.00545926885119413 0.05459268851194133	re_qice 0.00041763418180853 0.00417634181808530 0.04176341818085303	re_qsnow 0.00000342324010777 0.00003423240107771 0.00034232401077709	all 0.00324914467627453 0.00345786558440380 0.00367974446810941
perturbation 0.100000000000000 0.010000000000000 0.00100000000	tau_qv 0.99976211964662838 0.99999250625671401 0.99999941841740992 0.9999994352462062	tau_qi 1.01121693177192682 1.00117866173472181 1.00011845260513306 1.00001185114200591	tau_qs 0.997041368660527521 0.99970339809213327 0.99997033240185988 0.99999703316609273	re_qcloud 0.00054592688511941 0.00545926885119413 0.05459268851194133 0.54592688511941326	re_qice 0.00041763418180853 0.00417634181808530 0.04176341818085303 0.41763418180853029	re_qsnow 0.00000342324010777 0.00003423240107771 0.00034232401077709 0.00342324010777093	all 0.00324914467627453 0.00345786558440380 0.00367974446810941 0.00973564692016131
perturbation 0.1000000000000000 0.0100000000000000 0.00100000000	tau_qv 0.99976211964662838 0.99999250625671401 0.99999941841740992 0.99999994352462062 0.999999994352462062	tau_qi 1.01121693177192682 1.00117866173472181 1.00011845260513306 1.00001185114206591 1.000001185114206591	tau_qs 0.99704136860527521 0.99970339809213327 0.99997033240185988 0.99999703316609273 0.9999970331586832	re_qcloud 0.00054592688511941 0.00545926885119413 0.05459268851194133 0.54592688511941326 0.99448710487399171	re_qice 0.00041763418180853 0.00417634181808530 0.04176341818085303 0.41763418180853029 1.05846382261075610	re_qsnow 0.0000342324010777 0.0003423240107771 0.00034232401077709 0.00342324010777093 0.03423240107770930	all 0.00324914467627453 0.00345786558440380 0.00367974446810941 0.00973564692016131 0.05275784331725234
perturbation 0.1000000000000000 0.010000000000000 0.00100000000	tau_qv 0.99976211964662838 0.99999250625671401 0.99999941841740992 0.99999994352462062 0.9999999436929583 0.9999999943709793	tau_qi 1.01121693177192682 1.00117866173472181 1.00011845260513306 1.00001185114200591 1.00000118517303274 1.00000011851789161	tau_qs 0.99704136860527521 0.99970339809213327 0.99997033240185988 0.99999703316609273 0.99999970331586832 0.9999997033157942	re_qcloud 0.00054592688511941 0.00545926885119413 0.05459268851194133 0.54592688511941326 0.99448710487399171 0.99944518110118040	re_qice 0.00041763418180853 0.00417634181808530 0.04176341818085303 0.41763418180853029 1.05846382261075610 1.00569555430513386	re_qsnow 0.0000342324010777 0.00003423240107771 0.00034232401077709 0.00342324010777093 0.034232401077709305	all 0.00324914467627453 0.00345786558440380 0.00367974446810941 0.00973564692016131 0.05275784331725234 0.34844160934770783
perturbation 0.1000000000000000 0.0100000000000000 0.00100000000	tau_qv 0.99976211964662838 0.99999250625671401 0.99999941841740992 0.99999994352462062 0.99999999436929583 0.9999999994370148	tau_qi 1.01121693177192682 1.00117866173472181 1.00011845260513306 1.00001185114200591 1.0000011851789161 1.00000011851789164	tau_qs 0.99704136860527521 0.99970339809213327 0.99997033240185988 0.99999703316609273 0.99999970331586832 0.99999997033157942 0.9999999703315787	re_qcloud 0.00054592688511941 0.00545926885119413 0.05459268851194133 0.54592688511941326 0.99448710487399171 0.999444518110118040 0.99994448253066235	re_qice 0.00041763418180853 0.00417634181808530 0.04176341818085303 0.4176341818085303 1.05846382261075610 1.00569555430513386 1.00056808533263866	re_qsnow 0.0000342324010777 0.00003423240107771 0.00034232401077709 0.00342324010777093 0.34232401077709300 0.34232401077709305 1.00002053627502306	all 0.00324914467627453 0.00345786558440380 0.00367974446810941 0.00973564692016131 0.05275784331725234 0.34844160934770783 1.00012306741732932
perturbation 0.1000000000000000 0.0100000000000000 0.00100000000	tau_qv 0.99976211964662838 0.99999250625671401 0.99999941841740992 0.99999994352462062 0.99999999436929583 0.9999999943709793 0.999999999437116	tau_qi 1.01121693177192682 1.00117866173472181 1.00011845260513306 1.00001185114200591 1.00000118517303274 1.0000001185179504 1.0000000118517956	tau_qs 0.997041368660527521 0.99970339809213327 0.9999703316609273 0.99999970331586832 0.99999997033157942 0.9999999703315797 0.9999999970331579	re_qcloud 0.000545926885119413 0.005459268851194133 0.5459268851194133 0.54592688511941326 0.99448710487399171 0.9994448718110118840 0.99994448253066235 0.99999444789698367	re_qice 0.000417634181808530 0.004176341818085303 0.41763418180853029 1.05846382261075610 1.00565555430513386 1.00056808533263866 1.00005679386952391	re_qsnow 0.0000342324010777 0.00003423240107771 0.00034232401077709 0.00342324010777093 0.03423240107770930 0.34232401077709305 1.0000205525587496	all 0.00324914467627453 0.00345786558440380 0.00367974446810941 0.00973564692016131 0.05275784331725234 0.34844160934770783 1.00012306741732932 1.00001231128564923
perturbation 0.100000000000000 0.010000000000000 0.00100000000	tau_qv 0.99976211964662838 0.99999250625671401 0.99999994382462062 0.999999994352462062 0.9999999943709793 0.99999999943709793 0.9999999999437116 0.9999999999437112	tau_qi 1.01121693177192682 1.00117866173472181 1.00011852260513306 1.00001185114200591 1.00000118517303274 1.00000011851789161 1.00000001185179504 1.00000000118517956	tau_qs 0.99704136860527521 0.99970339809213327 0.99997033240185988 0.999999703316609273 0.99999970331586832 0.9999999703315787 0.9999999970331578	re_qcloud 0.00054592688511941 0.00545926885119413 0.05459268851194133 0.54592688511941326 0.99448710487399171 0.99944518110118040 0.9999444789698367 0.99999444789698357	re_qice 0.00041763418180853 0.00417634181808530 0.04176341818085303 0.41763418180853029 1.05846382261075610 1.00569555430513386 1.00066679386952391 1.00006567924035214	re_qsnow 0.0000342324010777 0.0003423240107771 0.00034232401077709 0.00342324010777093 0.03423240107770930 0.34232401077709305 1.0000205525587496 1.000002055254186516	all 0.00324914467627453 0.00345786558440380 0.00367974446810941 0.00973564692016131 0.05275784331725234 0.34844160934770783 1.00012306741732932 1.00001231128564923 1.00000123117398802
perturbation 0.100000000000000 0.010000000000000 0.00100000000	tau_qv 0.99976211964662838 0.99999250625671401 0.9999994382462062 0.99999994352462062 0.99999999435246207 0.9999999943709793 0.9999999999437116 0.999999999943711	tau_qi 1.01121693177192682 1.00117866173472181 1.00011845260513306 1.00001185174206591 1.00000118517303274 1.00000011851789161 1.000000001185179504 1.0000000011851795 1.0000000011851795	tau_qs 0.99704136860527521 0.99970339809213327 0.99997033240185988 0.99999703316609273 0.99999970331586832 0.9999997033157942 0.999999970331579 0.9999999970331579 0.9999999970331579	re_qcloud 0.00054592688511941 0.00545926885119413 0.05459268851194133 0.54592688511941326 0.99448710487399171 0.999448253066235 0.9999944478063367 0.99999944478613725 0.9999994447857811	re_qice 0.00041763418180853 0.00417634181808530 0.04176341818085303 0.41763418180853029 1.05846382261076610 1.00569555430513386 1.00056808533263866 1.00005679386952391 1.00000567924035214 1.0000056792256925	re_qsnow 0.0000342324010777 0.0003423240107771 0.00034232401077709 0.00342324010777093 0.3423240107770930 1.0000205525587496 1.00000205525587496 1.0000002055434929	all 0.00324914467627453 0.00345786558440380 0.00367974446810941 0.00973564692016131 0.05275784331725234 0.34844160934770783 1.00012306741732932 1.0000123117398802 1.0000012311735302
perturbation 0.1000000000000000 0.010000000000000 0.00100000000	tau_qv 0.99976211964662838 0.99999250625671401 0.99999941841740992 0.99999994352462062 0.99999999943769793 0.99999999994371148 0.99999999999437116 0.99999999994371 0.99999999994371	tau_qi 1.01121693177192682 1.00117866173472181 1.00011845260513306 1.00001185114200591 1.00000118517303274 1.00000011851789161 1.00000001185179504 1.0000000011851795 1.0000000011851796 1.000000000118518	tau_qs 0.99704136860527521 0.99970339809213327 0.99997033240185988 0.999999703316609273 0.9999999703315787 0.99999997033157942 0.9999999970331579 0.9999999970331579 0.9999999997033158 0.999999997033158 0.99999999703315	re_qcloud 0.00054592688511941 0.00545926885119413 0.05459268851194133 0.5459268851194133 0.99448710487399171 0.99944518110118040 0.99994448253066235 0.9999944478678613725 0.9999994447857811 0.99999994447857811	re_qice 0.000417634181808530 0.004176341818085303 0.4176341818085303 0.41763418180853029 1.05569555430513386 1.000569555430513386 1.0005679386952391 1.0000056792405214 1.000000567922254925	re_gsnow 0.0000342324010777 0.00003423240107771 0.00034232401077709 0.00342324010777093 0.3423240107770930 1.00002053627502306 1.00000205525887496 1.00000020554186516 1.0000002055434929 1.00000002055434929	all 0.00324914467627453 0.00345786558440380 0.00367974446810941 0.00973564692016131 0.05275784331725234 0.34844160934770783 1.00012306741732932 1.000012311785802 1.0000012311785302 1.0000001231178544
perturbation 0.1000000000000000 0.010000000000000 0.0010000000000	tau_qv 0.99976211964662838 0.99999250625671401 0.99999941841740992 0.99999994352462062 0.999999999436929583 0.99999999994370116 0.9999999999437116 0.99999999994371 0.99999999994371 0.999999999994371	tau_qi 1.01121693177192682 1.00117866173472181 1.00011845260513306 1.00001185174206591 1.00000011851789161 1.00000001185179504 1.00000000118517956 1.000000000118517956 1.0000000001185180 1.00000000001185180 1.000000000011852	tau_qs 0.99704136860527521 0.99970339809213327 0.9999703316609273 0.99999970331586832 0.99999997033157942 0.9999999703315787 0.9999999970331579 0.9999999997033158 0.9999999999703316 0.9999999999703316	re_qcloud 0.000545926885119413 0.0545926885119413 0.5459268851194133 0.5459268851194133 0.99448710487399171 0.999444518110118040 0.9999444518110118040 0.99999444789698367 0.9999994447857811 0.99999994447857811 0.99999999444785781	re_qice 0.000417634181808530 0.004176341818085303 0.4176341818085303 0.41763418180853029 1.05846382261075610 1.00569555430513386 1.000569555430513386 1.00005679386952391 1.00000567924035214 1.0000005679224035 1.0000005679224227 1.000000567922408	re_gsnow 0.0000342324010777 0.00003423240107771 0.000342324010777093 0.0342324010777093 0.34232401077709305 1.0000205525587496 1.000002055543656 1.0000000255434929 1.000000025543656 1.0000000025543657	all 0.00324914467627453 0.00345786558440380 0.00367974446810941 0.00973564692016131 0.05275784331725234 0.34844160934770783 1.00012306741732932 1.00001231128564923 1.00000123117398802 1.00000012311785302 1.0000001231178984 1.000000012311798

2. Adjointness test

1. Linearity test

Val_TL 177428010441.853279159389844692656 Val_AD 177428010441.853279159389844692656

 $\langle d\mathbf{Y}, d\mathbf{Y} \rangle = \langle d\mathbf{X}, \mathbf{M}^T \mathbf{M} d\mathbf{X} \rangle$

- Tangent linear forecast approximates well the derivative of the nonlinear model solution as the perturbations decreased and approach zero.
- Adjoint code is developed correctly with the tangent linear code.

Sensitivity test for FARMS



Tangent linear model gives the derivative of forecast variables w.r.t. model state variables.

The error of each model-state variable

The error of GHI w.r.t each model-state variable

P_ERROR = 1000.0, ALBEDO_ERROR = 0.1, Z_ERROR = 0.001, AOD_ERROR = 0.1, ALPHA_ERROR = 0.5, W_ERROR = 10., TAU_QC_ERROR = 37.8, TAU_QI_ERROR = 2.0, TAU_QS_ERROR = 31.6, RE_QC_ERROR = 4.2828965E-06, RE_QI_ERROR = 1.8598472E-05, RE_QS_ERROR = 2.1256968E-04

Sensitivity test result for FARMS



- In clear sky, GHI is sensitive to albedo, aod, w, and g and less sensitive to p and DNI is very sensitive to aod and alpha (Ångström wavelength exponent).
- In cloudy sky, GHI is sensitive to cloud optical depth and less sensitive to effective radius. DNI shows small sensitivity to cloud variables, because DNI tends to attenuate fast if there is a cloud.

Thompson microphysics scheme

- Processes controlling formation of cloud droplets and ice crystals, and their growth and fallout as a surface precipitation
- Thompson et al. (2004) (2008)
- Important outputs
- Hydrometeors mixing ratio
 Number concentration
 Effective radius
 Re_qc Re_qi Re_qs

Tangent linearity test result

perturbation	pii	p	av	ni	nr	th
0.1000000000000000	29.12026251452843614	1.00000080868057415	0.88252174368814363	0.99999805785627547	0.99999497867708051	1.00128868656308209
0.0100000000000000	4.63732994181417238	1.0000008086788871	4221.80608905632988580	0.99999980546347224	0.99999949774467703	1.00010906271534277
0.0010000000000000	1.39942238411864841	1.0000000808678378	45186.75732615917270445	0.9999998054313366	0.99999994977323686	1.00001081974271796
0.0001000000000000	0.99967320622910260	1.0000000080867493	144196.24922916645081677	0.9999999805428124	0.99999999497731138	1.00000108110223898
0.0000100000000000	0.99996519006617278	1.0000000008086406	13426.90232938601181683	0.9999999980542780	0.99999999949773101	1.00000010810149680
0.0000010000000000	0.99999649722187581	1.0000000000808297	0.99873757368969613	0.9999999998054278	0.99999999994977310	1.0000001081006235
0.000001000000000	0.99999964950387523	1.0000000000080486	0.99987345683297629	0.9999999999805428	0.9999999999497731	1.0000000108100531
0.000000100000000	0.99999996494820387	1.00000000000007705	0.99998734266891684	0.99999999999980543	0.99999999999949773	1.0000000010810047
0.000000010000000	0.99999999649479849	1.00000000000000427	0.99999873423673883	0.99999999999998054	0.999999999999997	1.0000000001081000
0.000000001000000	0.99999999964947957	0.99999999999999999699	0.99999987342337234	0.999999999999999805	0.999999999999999498	1.0000000000108095
0.0000000001000000	0.99999999996494789	0.999999999999999626	0.9999998734233422	0.999999999999999981	0.999999999999999950	1.0000000000010805
0.0000000000100000	0.9999999999649473	0.9999999999999999622	0.9999999873423339	0.9999999999999999998	0.999999999999999995	1.0000000000001076
perturbation		qc	qr	qi	q	s qg
0.000000000010000000000	1.000002730194700	91743457 1.0000	00784252376445529653	0.99981157525696905115314	37.1052498206959178277220	4 239256243.40504912474784572891045
0.000000000001000000000	1.00000000213448	99935915 0.9999	99982279203363897683	0.99998115889208196461107	0.9996413992744851928700	4 0.99427010326095451218421
0.000000000000100000000	1.00000000021341	38495380 0.9999	99998227919636322747	0.99999811590209594349521	0.9999641129664208796467	3 0.99942094530561036044225
0.0000000000000000000000000000000000000	1.000000000002130	62351526 0.9999	99999822791956631603	0.99999981159033854263204	0.9999964110267264855978	2 0.99994203299382740560471
0.0000000000000000000000000000000000000	1.000000000000209	54737205 0.9999	99999982279195593155	0.99999998115903514381686	0.9999996410999731867965	4 0.99999420268311420799683
0.0000000000000000000000000000000000000	1.0000000000000017	43978490 0.9999	99999998227919558432	0.99999999811590352727758	0.9999999641099703237562	9 0.99999942026214783280643
0.0000000000000000000000000000000000000	0.9999999999999998	22894251 0.9999	99999999822791955865	0.99999999981159035285760	0.9999999964109967624259	0.99999994202615311172572
0.0000000000000000000000000000000000000	0.999999999999999	30944905 0.9999	99999999982279194006	0.99999999998115903529840	0.9999999996410996735383	0.99999999420261464193263
0.0000000000000000000000000000000000000	0.999999999999999	13783073 0.9999	99999999998227924355	0.99999999999811590364896	0.9999999999641099673125	0.99999999942025810306582
0.0000000000000000000000000000000000000	0.999999999999999	95632141 0.9999	99999999999822606518	0.99999999999981159156856	0.999999999964109964688	0.9999999994197961872795
0.0000000000000000000000000000000000000	0.999999999999999	11421704 0.9999	799999999999995704902	0.999999999999998117134816	0.9999999999996410905017	4 0.9999999999369346852715
0.0000000000000000000000000000000000000	1.0000000000000018	16866288 1.0000	0000000000086362292	0.99999999999999843364601	0.9999999999999640460641	4 0.99999999999399672578662

Tangent linearity test for Thompson scheme

				$\lambda \parallel \mathbf{M}$	$\ f(\mathbf{x})\ \lambda \to 0$	- () -
perturbation	pii	р	qv	ni	nr	th
0.10000000000000000	29.12030523556387637	1.00000080868272916	0.88252219607973746	0.99999805778299295	0.99999497867754053	1.00128845923923615
0.01000000000000000	4.63733555290297041	1.0000008086810423	4221.80833022473431091	0.99999980545616871	0.99999949774472302	1.00010906120903525
0.00100000000000000	1.39942289284096050	1.0000000808680533	45186.78117493344075776	0.9999998054240355	0.99999994977324146	1.00001081959714770
0.00010000000000000	0.99967319690782009	1.0000000080867708	144196.32538407285628561	0.9999999805420823	0.99999999497731184	1.00000108108773024
0.00001000000000000	0.99996518924224179	1.0000000008086427	13426.90942341354219545	0.9999999980542050	0.99999999949773106	1.00000010810004641
0.00000100000000000	0.99999649714037468	1.0000000000808299	0.99873757342351134	0.9999999998054205	0.99999999994977310	1.00000001080991732
0.000001000000000	0.99999964949573388	1.0000000000080486	0.99987345680685796	0.9999999999805420	0.99999999999497731	1.0000000108099081
0.0000001000000000	0.9999996494738983	1.00000000000007705	0.99998734266631015	0.99999999999980542	0.99999999999949773	1.0000000010809902
0.000000010000000	0.9999999649471708	1.00000000000000427	0.99999873423647821	0.99999999999998054	0.999999999999994977	1.0000000001080985
0.000000001000000	0.9999999964947143	0.99999999999999999699	0.99999987342334628	0.9999999999999999805	0.99999999999999998	1.00000000000108094
0.0000000001000000	0.9999999996494708	0.999999999999999626	0.9999998734233161	0.99999999999999999	0.999999999999999999	1.00000000000010805
0.0000000000100000	0.9999999999649464	0.9999999999999999622	0.9999999873423313	0.999999999999999999	0.9999999999999999999	1.00000000000001076
0.00000000000010000	0.99999999999964940	0.9999999999999999607	0.9999999987342331	1.000000000000000004	1.000000000000000000	1.0000000000000000103
0.00000000000001000	0.99999999999996488	1.000000000000000197	0.9999999998734233	1.000000000000000031	1.000000000000000007	1.000000000000000000
0.00000000000000100	0.99999999999999642	0.999999999999998714	0.9999999999873423	0.999999999999999412	1.000000000000000096	0.9999999999999999999
0.00000000000000000	0.9999999999999999958	0.9999999999882345	0.99999999999987342	1.0000000000001514	0.99999999999998794	1.000000000000000000
0.00000000000000000	0.9999999999999999999	0.99999999999552101	0.99999999999998734	0.99999999999987412	1.00000000000007701	1.00000000000000283
nerturbation		ar	ai	0.5		2]]
a 10000000000000000	281 34456142445849957	2 10384750267052870	0 01155896842249986	45 0 00007252360161562	49 0 64451134823791261	0 42439858362708435
0 0100000000000000000	285 07351077066334083	0 18030861218548039	0 01962119699687656	0 00016194838274708	6 41388513857499314	0.42407000002700400
0.001000000000000000	7,01276622189808159	0.10590235623146618	0.46592783694438773	0.00092599355963521	6.46600229774844385	11,40722340930796670
0.000100000000000000	1,22939532370324930	0.28109304050254447	0.36232576571379455	0.00118431146783223	10.53809087584880070	35,24932022568506997
0.00001000000000000	1.01705652312390459	0.47164075033815304	0.23392497022670649	0.00205343008589638	34.23268992810648346	3.56390895313794714
0.00000100000000000	1,00486681475522106	0.55338043995902427	0.10126584533535047	0.00625424963418540	0.00636956549368435	0.01291551336322019
0.00000010000000000	1,10127365042464094	0,99790315794997332	0,07712704232194833	0.03092310448595279	0.01681313348501246	0.03299373225120408
0.000000100000000	1.00002134551779328	6.69528236582946477	0.52626318402452369	0.14225343371521997	0.04660269625648190	0.15339259214172173
0.000000010000000	1.00000213453166396	0.99823565407643765	0.82915048689990875	0.41889089884757768	0.13094162244810964	0.42599349556284316
0.000000001000000	1.00000021345296088	0.99982286898670179	0.98108518736584234	0.78868988323508999	0.34511667924968418	0.79138650865320306
0.0000000001000000	1.0000002134528967	0.99998227990163307	0.99811457668207070	0.96680649238488845	0.71099777998462236	0.96744208306705779
0.0000000000100000	1.0000000213452454	0.99999822792015984	0.99981157890917568	0.99644065249002359	0.94800422337681784	0.99675941884231901
0.0000000000010000	1.0000000021344805	0.99999982279131581	0.99998115917301595	0.99964139927177141	0.99427010324258760	0.99992655630504401
0.0000000000001000	1.0000000002134040	0.99999998227912447	0.99999811593019329	0.99996411296614925	0.99942094528733811	1.00024589065633193
0.0000000000000000000	1.0000000000212964	0.9999999822791227	0.9999981159314832	0.99999641102669932	0.99994203297556467	1.00027785060379990
0.0000000000000000000000000000000000000	1.0000000000020856	0.9999999982279112	0.9999998115931612	0.99999964109997047	0.99999420266485243	1.00028104686398169
0.00000000000000000	1,00000000000001645	0.99999999998227900	0.9999999811593162	0.99999996410997005	0.99999942024388615	1,00028136649265454

 $\Phi(\lambda) = \frac{\|f(\mathbf{x} + \lambda) - f(\mathbf{x})\|}{\|f(\mathbf{x} + \lambda) - f(\mathbf{x})\|}, \lim \Phi(\lambda) = 1$

- Same perturbations were applied to all input variables. If hydrometeors are less than 1.e-12, we did not perturb that layer.
- When input values are much larger than perturbation (P, Ni, and Nr), it tends to reach model precision quickly.
- Tangent linear forecast approximates well the derivative of the nonlinear model solution as the perturbations decreased and approach zero.

Sensitivity test for Thompson scheme

- Cases are provided by WRF simulation (4/15 4/16 2018)
- 9 km horizontal resolution (600 x 354), 45 vertical layers

$$\frac{\partial \mathbf{Y}}{\partial X} \cdot \bigtriangleup \mathbf{X} = \bigtriangleup \mathbf{Y}$$

- 1. Constant error TH
- 2. Value of variable itself Ni
- 3. Standard deviation of each variable on each layer
 - Qc, Qi, Qr, Qs, Qg, Nr
 - Qv, Pi, P



Comparing sensitivity

Input

$\left(\frac{\partial Y}{\partial X} \cdot \Delta X\right)$	$/\overline{Y}$
ΔX	median

		QV	QC	QR	QI	QS	QG	NI	NR	тн	PII	Р
	QV	0.98	0	0	0	0	0	0	0	0	0	0
	QC	4.521	0.276	0	0	0	0	0	0	-1.323	-0.354	0.054
	QR	0	0	1.74	0	0	0	0	0.023	0	0	0
	QI	0.258	0	0	1.549	0	0	0	0	0	0	0
	QS	0.008	0	0	0	1.734	0	0	0	-0.004	0	0
ł	QG	0	0	0	0	0	1.811	0	0	0	0	0
	NI	0	0	0	0	0	0	0.04	0	0	0	0
	NR	0	0	0	0	0	0	0	0.92	0	0	0
	тн	0	0	0	0	0	0	0	0	0.01	0	0
	REQC	1.37	0.08	0	0	0	0	0	0	-0.43	-0.12	0.02
	REQI	0.36	0	0	80.98	0	0	-0.12	0	-0.12	-0.02	0
	REQS	0.02	0	0	0	329.16	0	0	0	0	0	0
	RAINNC	0	0	0.004	0	0	0	0	0	0	0	0

Output

Sensitivity analysis





Summary

 WRF-Solar was the first NWP model specifically designed to provide solar irradiance forecast tailored for solar energy applications.



- New developments focused on improving the cloud-aerosol-radiation physics by ensemble based probabilistic forecasts.
- Adjoint sensitivity analysis of physics packages is used for finding key variables and parameters controlling the surface irradiance. In this study, it was applied to FARMS and Thompson schemes.
- This will lead to select optimal ensemble members and reduce forecast errors by providing more accurate probabilistic forecasts.